# The Aggregate Effects of Labor Market Concentration* 

Miren Azkarate-Askasua and Miguel Zerecero ${ }^{\dagger}$<br>Toulouse School of Economics<br>JOB MARKET PAPER

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#### Abstract

What are the efficiency and welfare effects of employer and union labor market power? We use data of French manufacturing firms to first document a negative relationship between employment concentration and wages and labor shares. At the micro-level, we identify the effects of employment concentration thanks to mass layoff shocks to competitors. Second, we develop a bargaining model in general equilibrium that incorporates employer and union labor market power. The model features structural labor wedges that are heterogeneous across firms and potentially generate misallocation of resources. We propose an estimation strategy that separately identifies the structural parameters determining both sources of labor market power. Furthermore, we allow different parameters across industries which contributes to the heterogeneity of the wedges. We show that observing wage and employment data is enough to compute counterfactuals relative to the baseline. Third, we evaluate the efficiency and welfare losses from labor market distortions. Eliminating employer and union labor market power increases output by $1.6 \%$ and the labor share by 21 percentage points translating into significant welfare gains for workers. Workers' geographic mobility is key to realize the output gains from competition.


JEL Codes: J2, J42, D24
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## 1 Introduction

There is growing evidence, especially for the United States, linking lower wages to labor market concentration. ${ }^{1}$ Indeed, if this concentration reflects monopsony power in the labor market, standard theory predicts that establishments mark down wages by paying workers less than their marginal revenue product of labor. On the other hand, if labor market institutions enable workers to organize and have a say over the wage setting process, bargaining can mitigate, or even reverse, the effect of establishments' market power on wages.

In this paper we quantify the efficiency and welfare losses from labor market power in the French manufacturing sector. The French case stands out over other developed countries, especially with respect to the U.S., for having regulations that significantly empower workers over employers. ${ }^{2}$ We therefore provide a framework that incorporates both, employer and union labor market power. Our main result is that, holding the total labor supply constant, removing employer and workers' labor market power increases French manufacturing output by 1.6 percent. Even if productivity and output gains are relatively small, distributional effects are important as the labor share increases by 21 percentage points and the aggregate wage rises by 45 percent. This wage increase translates into median expected welfare gains of 42 percent for workers.

We proceed in three steps. First, we establish empirically that, within a same firm, establishments with higher local employment shares pay lower wages for same occupations. We identify this effect by using a competitors national mass layoff shock as an external source of variation to an establishment's local employment share. Second, in line with the previous empirical result and the French labor institutional setting, we build and estimate a model where labor market power arises from: (i) employers that face upward sloping labor supplies, and (ii) workers that bargain over the wages. Third, we use the model to quantify the efficiency and welfare consequences of employers and workers' labor market power.

We start by documenting the link between concentration and wages/labor shares. We use data on French manufacturing firms from 1994 to 2007. Employer labor market power is related to the notion of local labor markets. We define those as a combination of commuting zone, industry, and occupation, and measure concentration at the local labor market level using the Herfindahl-Hirschman Index. ${ }^{3}$ We find that concentrated industries have on average lower labor shares. Passing from the first to the third quartile of local labor market concentration, the labor share is reduced by 1 percentage point.

At the establishment-occupation level, our proxy for the strength of labor market power is the employment share within the local labor market. To explore a link between concentration and labor payments, we need to overcome the potential endogeneity of the employment share and the wages. Therefore, we instrument employment shares with negative employment shocks or mass layoffs to competitors. Identification comes from residual within a firm-occupation-year variation across local labor markets. Depending on the specification, the estimated elasticity ranges from -0.17 to -0.04 . That is, a 1 percentage point increase of employment share lowers the establishment wage by up to 0.17 percent. ${ }^{4}$

After presenting the reduced form evidence, we build a general equilibrium model that incorporates two

[^1]elements: employer and union labor market power. First, we borrow from the trade and urban economics literature (e.g. Eaton and Kortum, 2002; Ahlfeldt et al., 2015) and assume workers have stochastic preferences to work at different workplaces. Heterogeneity of workers' tastes implies individual establishment-occupations face an upward sloping labor supply curve which gives rise to employer labor market power. In the absence of bargaining, as there is a discrete set of establishment-occupations per local labor market, employers act strategically and compete for workers in an oligopsonistic fashion. Wages are therefore paid with a markdown which is a function of the perceived labor supply elasticity. Similarly to Atkeson and Burstein (2008), this elasticity in turn depends on the employment share within the local labor market. The framework without bargaining is similar to Berger et al. (2019) under Bertrand competition. The second element is collective wage bargaining. We assume wages are set at the establishment-occupation level and workers force a wage setting process where they bargain over the status-quo scenario, the oligopsonistic competition outcome. In doing so, they internalize that if bargaining were to fail establishments compete oligopsonistically on the local labor market. Workers' ability to extract rents over that outside option depends on their bargaining power in a reduced form Nash bargaining.

This wage-setting process leads to a distortion that is reflected in a wedge between the equilibrium negotiated wage and the marginal revenue product of labor. This wedge summarizes both sides of market power as it is a combination of both, a markdown due to the oligopsony power, and a markup due to wage bargaining. The smaller this wedge is, the larger the market power of employers relative to workers and vice-versa. Heterogeneity of the labor wedge across establishments distorts relative wages and potentially generate misallocation of resources that decrease aggregate output. Heterogeneity comes from two sources: (i) the dependence of the markdown on industry specific labor supply elasticities and employment shares; and (ii) the across industry differences in the markup due to diversity of bargaining powers. Our model nests as special cases both a full bargaining setting or a model with oligopsonistic competition only.

Our framework features a large number of different prices, the establishment-occupation wages plus the product prices. We show how to solve for the general equilibrium of the model in two steps. We solve first for wages in each local labor market normalizing aggregate prices. Second, we show how to build industry level fundamentals and solve for aggregate prices. This two-step procedure eases the solution because the model can be rewritten at the industry level. ${ }^{5}$ We provide an analytical characterization of the equilibrium at the industry level and along the way prove the existence and uniqueness of the equilibrium. This allows us to use the model to back out fundamentals that rationalize the observed data and perform counterfactuals on actual data without worrying about multiple equilibria.

After the model set-up, we discuss how to identify and estimate the model parameters. We have two types of parameters: the ones related to the labor supply and bargaining, and the ones related to technology. Regarding the labor supply, we assume that workers face a sequential decision: in a first stage, they observe their preferences for different local labor markets and choose the one that maximizes their expected utility; in a second stage, they observe their preferences to work for different employers and choose the establishment. Therefore, these labor supplies depend on two key parameters that jointly determine the magnitude of employers' labor market power: a within local labor market elasticity and an across local labor market elasticity.

[^2]They govern, respectively, the intensity of how workers respond to changes in establishment wages within a local labor market, and how workers react to changes in average utilities (which are in turn a function of establishment wages) across local labor markets.

The main challenge is to separately identify the union bargaining powers from the within and across local market labor supply elasticities. We propose a strategy to estimate the labor supply elasticities that is independent from the underlying wage setting process. Therefore, our identification strategy is readily applicable to set-ups with or without bargaining. In the first step we estimate the across local labor market elasticity and the inverse labor demand elasticity adapting the identification through heteroskedasticity of Rigobon (2003). We use the insight that the across local labor market elasticity is the only relevant elasticity for the establishments that are alone in their local labor markets, the full monopsonists. Their local labor market equilibrium boils down to a standard system representing the labor supply and demand equations. Ordinary least squares estimates present the traditional problem of other price-quantity systems as the estimated elasticities are biased towards zero. Rather than instrumenting to get exogenous variation in labor supply and demand, we identify using a restriction on the variance-covariance of structural shocks across occupations and their heteroskedasticity. ${ }^{6}$ The identifying assumption is that the covariances between the labor demand and supply shifters, productivities and amenities respectively, are the same across occupations but not the variances. To gain intuition, let's fix the labor demand constant and assume different variances of the labor supply shifter, the amenity, across occupations. Increasing the variance of the labor supply shifter helps to identify the other side of the market, the labor demand.

In a second step we estimate the within local labor market labor supply elasticities by directly estimating the labor supply equation. We instrument for the wages by using revenue productivities as labor demand shifters and estimate by conditioning on within local labor market variation. This requires the inverse labor demand elasticity estimated in the first step. Finally, we calibrate the industry specific technology parameters (capital and labor elasticities) and bargaining powers to match the capital and labor shares.

Once the parameters are identified, we back out model primitives to perform counterfactuals. Ideally, we would like to have the distribution of fundamentals, in particular of physical productivities, at the establishment-occupation level that rationalizes the observed data on wages and employment. We back out amenities to match employment shares. However, the model only allows us to identify revenue productivity, which is a function of two objects: the physical productivity and the price of the good. These unobserved prices are equilibrium objects and the inability to identify the non-parametric distribution of productivities has prevented most studies (e.g. Hsieh and Klenow, 2009) from conducting full blown general equilibrium counterfactuals.

We show that the general equilibrium counterfactual can be computed using only revenue productivities. We do that by writing the model in terms of relative changes with respect to the current equilibrium. This approach, borrowed from the trade literature, allows us to solve for changes of equilibrium variables relative

[^3]to a baseline scenario. ${ }^{7}$ We are able to do that because changes in revenue productivities are completely driven by changes in prices and not the physical productivity part which is fixed.

We quantify the efficiency losses of employers and workers' labor market power by removing those distortions in a counterfactual economy while keeping workers' preferences fixed. This is a counterfactual scenario where employers are price takers and workers have no bargaining power. We find that output increases by 1.6 percent while the labor share rises by 21 percentage points. This increased labor share goes together with wage gains that in turn translate into 42 percent median welfare gains for workers. Removing the heterogeneity of wedges improves the allocation of labor by increasing the employment of more productive establishments. The counterfactual gains in the labor share suggest that employer labor market power is stronger than the one of the unions. This is a consequence of the estimated low labor supply elasticities that are in the range lower than the estimates of Berger et al. (2019) for the U.S.

Additionally, we find that geographic mobility is the key margin of adjustment to achieve the baseline counterfactual productivity gains, rather than within local labor market or within industry mobility. The intuition behind this is that there are a handful of concentrated and productive firms in the rural areas and removing labor market power increases their wage and employment more relative to the urban areas. We find that labor market distortions account for 13 percentage points - about a third - of the urban/rural wage gap. Consequently, the total employment decreases in urban areas relative to the baseline, which changes the geographical composition of manufacturing employment in France.

Finally, we incorporate two extensions to the model. First, we introduce an endogenous labor force participation decision by assuming that workers may voluntarily stay out of the labor force. Output gains in this case are slightly higher than in the baseline because wage gains increase the labor force participation. Second, we allow for agglomeration forces within the local labor market that also improve the output gains from the baseline counterfactual.

Literature. This paper speaks to several strands of the literature. First, and most closely related, is the literature on employer labor market power. Several empirical papers have documented the importance of labor market concentration on wages, employment and vacancies (Benmelech et al., 2018; Azar et al., 2017, 2018). These focus on aggregate measures of concentration as the Herfindahl-Hirschman Index. Our contribution to this empirical literature is to focus on establishment level concentration and use exogenous variations to show the existence of employer labor market power in France. We argue that firms having mass layoffs constitute a quasi-natural variation on the employment shares of the non-shocked establishments. This allows us to causally identify the effect of the employment share at the local labor market, our proxy of the strength of employer labor market power, on wages.

This paper also contributes to structural work on employer labor market power. We depart from the traditional monopsony power framework (e.g. Burdett and Mortensen, 1998; Manning, 2011; Card et al., 2018; Lamadon et al., 2018) by having heterogeneous markdowns and by extending it to allow for wage bargaining. The paper is complementary to Jarosch et al. (2019) in the sense that they consider employer labor market power in a search framework. We contribute to those papers by incorporating unions. In contemporaneous and independent work, Berger et al. (2019) build a structural model with oligopsonistic competition in local

[^4]labor markets. We share the objective of measuring the efficiency effects of labor market distortions and reach similar quantitative conclusions, but our contribution differs from theirs in several dimensions: (i) our framework nests theirs as an special case without bargaining; (ii) we incorporate occupations and use them for the identification of the structural parameters; (iii) we allow for differences in structural parameters across industries. In particular, within local labor market elasticities and bargaining powers are diverse across industries. Importantly, this adds heterogeneity to the labor wedges and employment misallocation; (iv) on the empirical evidence, they instrument with tax changes across states in the U.S. whereas we use labor shocks to competitors; (v) we show that counterfactuals can be computed without the need to back out underlying productivities and we perform the counterfactuals using actual establishment data.

Second, the paper is related to the literature on Nash bargaining. We take the axiomatic approach (Osborne and Rubinstein, 1990) rather than the sequential or strategic approach (Binmore et al., 1986; Stole and Zwiebel, 1996; Brügemann et al., 2018) with offers and counter-offers. In our framework, collective bargaining happens at the establishment-occupation level and the employer cannot discriminate against different workers. Therefore collective bargaining applies universally even if only a subset of workers is unionized. Regarding the union bargaining power, our estimates relate to the estimates for manufacturing from Cahuc et al. (2006) in a framework with on the job search.

Third, the paper relates to the literature on imperfect competition in general. Our approach is similar to Edmond et al. (2018) and Morlacco (2018) in trying to quantify the effect of heterogeneous market power on aggregate output. They study, output and intermediate input market powers respectively while we focus on the effects of labor market power. Karabarbounis and Neiman (2013) documented the falling trend of the labor share and Barkai (2016) and Gutiérrez and Philippon (2016) the rising trend of the profit share for different countries. Output market power has been pointed out as an explanation for the decline of labor payments out of GDP (e.g. De Loecker and Eeckhout, 2017, 2018). Contrary to the evidence on output market power, other studies suggest that employer labor market power is not the driver behind the decreasing trends of the U.S. labor share (e.g. Lipsius, 2018; Berger et al., 2019). The focus of this paper is therefore not on labor share trends but on the effects employer and union labor market power in a given cross section of firms, markets and industries.

Our model builds on the trade (Eaton and Kortum, 2002) and urban economics (Redding, 2016; Ahlfeldt et al., 2015) literature. The establishment perceived elasticity has the same functional form as the perceived demand elasticities in Atkeson and Burstein (2008) under Bertrand competition. Diversity of perceived elasticities is the main source of heterogeneity of the labor wedge and is at the origin of resource misallocation as emphasized by Hsieh and Klenow (2009) and Restuccia and Rogerson (2008).

Finally, the paper contributes to micro-estimates of labor supply elasticities. Staiger et al. (2010), Falch (2010) and Berger et al. (2019) use quasi-experimental variation on the wages to estimate the firm labor supply elasticities that go from 0.1 (Staiger et al., 2010) to 5.4 (Berger et al., 2019). Both our within and across local labor market labor supply elasticities lie in that range.

The rest of the paper is organized as follows. Section 2 introduces the data. Section 3 shows the stylized facts and our empirical strategy. Section 4 introduces the model. Section 5 discusses details about parameter estimation. Section 6 discusses the results from counterfactual exercises. Section 7 presents extensions of the model and Section 8 concludes.

## 2 Data

We use two main data sources. Our first and primary source of data are firm-level fiscal records consisting of balance sheet information including wage bill, capital stock, number of employees and value added. This dataset is known as FICUS and it includes all French firms except for the smallest firms declaring at the micro-BIC regime and some agricultural firms. We also use DADS Postes, an employer-employee dataset with the universe of salaried employees. It provides firm and establishment identifiers (SIREN and SIRET respectively). We recover the location, occupation classification, wages and employment. This source is necessary to know how employment and wages are distributed across different establishment-occupations of a given firm. The sample covers private manufacturing firms in France from 1994 to 2007. A break in the industry classification series prevents us from extending the time span of the sample. ${ }^{8}$ Additionally we use data relating the city codes to commuting zones and Consumer Price Index data to deflate nominal variables. ${ }^{9}$ We define four broad categories of occupations: top management, supervisor, clerical and operational. ${ }^{10}$ We define a local labor market as the intersection between commuting zone, 3-digit industry and occupation. On average throughout the sample there are 57.900 local labor markets per year.

Our sample consists of approximately 4 million establishment-occupation-year observations that belong to around 1.25 million firms. Details about sample selection are in Appendix E.3.

### 2.1 Summary Statistics

Table 1 presents the final sample establishment-occupation level summary statistics. The median occupation at a given establishment has 2 employees and pays 27,439 euros per worker. Certain firms have occupations in different locations, which we denote as multilocation occupations. The micro evidence in the next Section focuses on multilocation firm-occupations. ${ }^{11}$ Panels (a) and (b) of Table 1 have the summary statistics of occupations belonging to monolocation and multilocation firms. Occupations of firms with plants or establishments at multiple locations have larger average (median) size of 27 employees than the 7 employees ( 4 versus 2) of monolocation occupations. Firms with multilocation occupations pay wages per capita that are $15 \%$ higher than the monolocation ones.

Manufacturing firms belong to 97 3-digit industries or sub-industries that are present in 364 different commuting zones. We denote the 3-digit industries as $h$ and the commuting zones as $n$. Summary statistics of sub-industries at 2007, the baseline year for the counterfactuals, are in Table 2. Average 3-digit industry labor share is $52 \%$ and the share of capital is $26 \%$. Taking those averages, the profit share would be around $22 \%$. We see that variation across sub-industries in size and labor productivity is important but more limited in average wage per establishment $\bar{w}_{h}$. Number of establishments $N_{h}$ and total employment $L_{h}$ are about 5 times higher passing from the first to the third quartile (from percentile 25 to 75 ), average wage increases by $27 \%$.

[^5]Table 1: Establishment-Occupation Summary Statistics

| Statistic | Obs. | Mean | $\operatorname{Pct1}(25)$ | Median | $\operatorname{Pct1}(75)$ | St. Dev. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $L_{i o t}$ | $4,151,892$ | 11.077 | 1.058 | 2.261 | 6.216 | 59.456 |
| $w_{\text {iot }} L_{\text {iot }}$ | $4,151,892$ | 367.155 | 31.566 | 71.813 | 196.554 | $2,379.449$ |
| $w_{i o t}$ | $4,151,892$ | 34.029 | 20.857 | 27.439 | 39.517 | 117.055 |
| $s_{i o \mid m}$ | $4,151,892$ | 0.203 | 0.011 | 0.051 | 0.238 | 0.306 |

(a) Monolocation

|  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $L_{i o t}$ | $3,359,236$ | 7.411 | 1.032 | 2.083 | 5.140 | 29.688 |
| $w_{i o t} L_{i o t}$ | $3,359,236$ | 216.710 | 29.636 | 64.480 | 159.624 | 925.159 |
| $w_{i o t}$ | $3,359,236$ | 32.843 | 20.299 | 26.641 | 38.478 | 35.478 |
| $s_{i o \mid m}$ | $3,359,236$ | 0.182 | 0.009 | 0.042 | 0.193 | 0.292 |

(b) Multilocation

|  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $L_{i o t}$ | 792,656 | 26.612 | 1.294 | 4.101 | 15.061 | 120.345 |
| $w_{\text {iot }} L_{\text {iot }}$ | 792,656 | $1,004.734$ | 45.711 | 139.315 | 532.979 | $5,052.361$ |
| $w_{\text {iot }}$ | 792,656 | 39.052 | 23.601 | 30.692 | 43.750 | 257.690 |
| $s_{i o \mid m}$ | 792,656 | 0.290 | 0.023 | 0.113 | 0.480 | 0.347 |

Notes: The top panel shows summary statistics for the whole sample. Panels (a) and (b) present respectively summary statistics of monolocation and multilocation firm-occupations. $L_{i o t}$ is full time equivalent employment at the establishment-occupation $i o, w_{i o t} L_{i o t}$ is the wage bill, $w_{i o t}$ is establishment-occupation wage or wage per FTE, $s_{i o \mid m}$ is the employment share out of the local labor market. All the nominal variables are in thousands of constant 2015 euros.

Table 2: Sub-industry Summary Statistics.

|  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Variable | Obs. | Mean | $\operatorname{Pctl}(25)$ | Median | $\operatorname{Pct1}(75)$ | St. Dev. |
| $N_{h}$ | 97 | $2,840.000$ | 493 | 1,261 | 2,639 | $4,530.496$ |
| $L_{h}$ | 97 | $30,466.030$ | 7,559 | 15,070 | 50,036 | $33,899.330$ |
| $\bar{w}_{h}$ | 97 | 34.607 | 29.562 | 32.990 | 37.531 | 6.902 |
| $L S_{h}$ | 97 | 0.520 | 0.482 | 0.527 | 0.581 | 0.098 |
| $K S_{h}$ | 97 | 0.261 | 0.165 | 0.233 | 0.316 | 0.133 |

[^6]Table 3 presents summary statistics for local markets in 2007. The local labor market, denoted by $m$, is a combination of commuting zone $n$, 3 -digit industry $h$ and occupations $o$. The median local market is small and has only 2 establishments and 10 employees. This is a consequence of the handful of manufacturing firms that are present in the countryside demanding certain occupations. One example of a local labor market are the blue collar workers working in the food industry in Lourdes, close to the Pyrenees. The median local labor market is concentrated with a Herfindahl-Hirschman Index (HHI henceforth) of $0.68 .{ }^{12}$ The HHI is very similar (0.69) if we consider wage bill shares $s_{i o \mid m}^{w}$ instead of employment shares $s_{i o \mid m}$. High median local labor market concentrations do not imply that most of the workers are in highly concentrated environments but rather that there are few local labor markets with low concentration levels and high employment. Further summary statistics on establishment and firm level are in Appendix E.1.

Table 3: Local Labor Market Summary Statistics. Baseline Year

| Variable | Obs. | Mean | $\operatorname{Pct1}(25)$ | Median | Pctl(75) | St. Dev. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $N_{m}$ | 57,940 | 4.755 | 1 | 2 | 4 | 14.400 |
| $L_{m}$ | 57,940 | 51.005 | 2.786 | 9.421 | 34.912 | 196.201 |
| $\bar{w}_{m}$ | 57,940 | 36.619 | 24.264 | 30.224 | 42.492 | 36.078 |
| $\widehat{w}_{m}$ | 57,940 | 36.189 | 24.081 | 30.028 | 42.179 | 25.556 |
| $\operatorname{HHI}\left(s_{i o \mid m}\right)$ | 57,940 | 0.671 | 0.384 | 0.683 | 1.000 | 0.320 |
| $\operatorname{HHI}\left(s_{i o \mid m}^{w}\right)$ | 57,940 | 0.676 | 0.392 | 0.698 | 1.000 | 0.318 |

Note: $N_{m}$ is the number of competitors in the local labor market $m, L_{m}$ is total employment in $m, \bar{w}_{m}$ is the mean $w_{i o t}$ of the establishment-occupations in $m, \widehat{w}_{m}$ is the weighted average wage at $m$ with weights equal to employment shares, $\mathrm{HHI}\left(s_{i o \mid m}\right)$ and $\mathrm{HHI}\left(s_{i o \mid m}^{w}\right)$ are respectively the Herfindahls with employment and wage shares. All the nominal variables are in thousands of constant 2015 euros.

## 3 Empirical Evidence

This section provides suggestive evidence of employer labor market power in France and presents the French institutional setting. We start by documenting some stylized facts on labor market concentration and the labor share at the industry level. Those are complemented with establishment level estimates that explore a causal link between wages and concentration. Finally, we present evidence on the institutional framework of French labor market and the importance of wage bargaining.

### 3.1 Concentration and the Labor Share

A standard measure of concentration is the Herfindahl Hirschman Index (HHI). From our definition of local labor market $m$, the HHI of market $m, H H I_{m t}$, is the sum of the squared employment shares of the plants present in $m$. Labor share at the 3-digit industry level, $L S_{h}$, is the ratio of the wage bill over value added. Due to data restrictions of observing value added only at the firm level, we cannot compute labor shares at

[^7]the local labor market level. We build a sub-industry concentration index $\overline{H H I}_{h t}$ by taking the employment weighted mean of $\mathrm{HHI}_{m t}$ across different local labor markets. ${ }^{13}$

We use the following specification:

$$
\begin{equation*}
\log \left(L S_{h, t}\right)=\delta_{b, t}+\beta \log \left(\overline{H H I}_{h, t}\right)+\varepsilon_{h, t} . \tag{1}
\end{equation*}
$$

Table 4 presents the results. Column (3) shows that the negative correlation between employment concentration and the labor share is robust to controlling for industry and industry-year fixed effects. Industry fixed effects capture differences across industries in the usage of capital. The focus of the paper being the cross sectional allocation of resources we also take industry-year fixed effects to only use cross sectional variation.

This regression gives a sense of the importance of the labor wedge heterogeneity to generate output and labor share losses. At face value, the estimate with industry fixed effects (Column (2)) imply a reduction of 1 percentage point of the labor share when passing from the first to the third quartile of concentration (quartiles of $\mathrm{HHI}\left(s_{i o \mid m}\right)$ in Table 3). Estimates in Column (3) with industry-year fixed effects are very similar.

## Table 4: Concentration and Labor Share

|  | $\log \left(L S_{h, t}\right)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) |
| $\log \left(\overline{H H I}_{h, t}\right)$ | $\begin{gathered} -0.064^{* * *} \\ (0.013) \end{gathered}$ | $\begin{gathered} -0.054^{* * *} \\ (0.013) \end{gathered}$ | $\begin{gathered} -0.056^{* * *} \\ (0.014) \end{gathered}$ |
| Industry FE | N | Y | N |
| Industry-year FE | N | N | Y |
| Observations | 1357 | 1357 | 1357 |
| $\mathrm{R}^{2}$ | 0.017 | 0.290 | 0.343 |
| Adjusted $\mathrm{R}^{2}$ | 0.017 | 0.280 | 0.170 |

Notes: This table presents estimates of equation (1). Column (1) presents the estimate without any fixed effect. Column (2) shows the exercise with industry fixed effects and Column (3) has industry-year fixed effects. The dependent variable is the logarithm of 3-digit industry $h$ labor share $\log \left(L S_{h, t}\right)$ at time $t \cdot \log \left(\overline{H H I}_{h, t}\right)$ is the logarithm of the employment weighted average of the local labor market Herfindahl Index. ${ }^{*} \mathrm{p}<0.1$; ${ }^{* *}$ p $<0.05 ;{ }^{* * *}$ p $<0.01$

The small estimated coefficient is most likely a result of two effects: the averaging across different local labor markets and level effects. The regression does not take into account the effect of concentration on the

[^8]average level of the labor share as this is absorbed by the fixed effects. Below we use this empirical exercise to validate our model.

### 3.2 Concentration and Wages

This section explores a causal relationship between employer labor market power and wages. The challenge is finding a source of exogenous variation in our proxy of local labor market power, the employment share $s_{i o \mid m}$, that will allow to estimate the effect of employer market power on wages or labor shares. Given our restriction of not observing value added at the plant level, we focus on wages. We briefly discuss the type of shocks we account for in the main specification and later on present our instrumental variable (IV henceforth) estimates with two different instruments. We focus on multi-location occupation for both exercises and the effects are estimated using residual variation across local labor markets within a firm-occupation-year.

The baseline specification is:

$$
\begin{equation*}
\log \left(w_{i o, t}\right)=\beta s_{i o \mid m, t}+\psi_{\mathbf{J}(i), o, t}+\delta_{\mathbf{N}(i), t}+\varepsilon_{i o, t}, \tag{2}
\end{equation*}
$$

where $\log \left(w_{i o, t}\right)$ is the $\log$ average wage at plant $i$ of firm $j$ and occupation $o$ at sub-market $m$ in year $t, s_{i o \mid m, t}$ is the employment share of the plant out of the market $m, \psi_{\mathbf{J}(i), o, t}$ is a firm-occupation-year fixed effect, $\delta_{\mathbf{N}(i), t}$ is a commuting zone-year fixed effect and $\varepsilon_{i o, t}$ is an error term. Our parameter of interest is $\beta$.

The specification controls for industry labor demand shocks with firm-occupation-year fixed effects $\psi_{\mathbf{J}(i), o, t}$. These include for example trade shocks either to manufacturing as a whole or for a particular industry. Shocks to occupation labor demand at the aggregate or firm level are captured by the fixed effects $\psi_{\mathbf{J}(i), 0, t}$. Lastly, the commuting zone times year fixed effects $\delta_{\mathbf{N}(i), t}$ control for permanent differences across locations and also for potential geographical spillovers of mass layoff shocks as stressed by Gathmann et al. (2017).

Establishment $i$ and occupation $o$ employment share, $s_{i o \mid m, t}$, is very likely to be endogenous to the wages themselves. On the one hand, everything else equal, higher wages attract more workers and therefore increase the employment share. On the other hand, if there is labor market power on the employer side, we expect two establishments with the same fundamentals to pay differently depending on their local labor market power. That is, everything else equal, we expect the plant with higher employment share to pay relatively less than the one at a more competitive local labor market. Given these endogeneity issues, we propose two different instruments for the employment share. First, we instrument for the employment share by using lagged measures of concentration and second, we use a quasi experimental variation of the employment shares coming from mass layoff shocks to competitors.

## Lagged Concentration Measures

We start by instrumenting the employment share by lagged concentration measures. More specifically, we instrument the employment share $s_{i o \mid m, t}$ by the lagged inverse of the number of competitors at the local labor market $1 / N_{m, t-1}$. Lagged concentration measures exclude potential endogeneity of the market structure to current period shocks. The correlation between employment shares and lagged concentration measures is 0.77 .

Table 5 shows the results. The first two columns recover estimates of the specification (2) with commuting zone (CZ) fixed effects and the last two columns with commuting zone-year fixed effects. Columns (1) and

Table 5: Wage Regression. Multi-location firms

|  | Dependent variable: |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\log \left(w_{i o, t}\right)$ |  |  |  |
|  | OLS | IV | OLS | IV |
| $s_{i o \mid m, t}$ | $\begin{gathered} 0.010^{* * *} \\ (0.001) \end{gathered}$ | $\begin{gathered} -0.030^{* * *} \\ (0.002) \end{gathered}$ | $\begin{gathered} 0.007^{* * *} \\ (0.001) \end{gathered}$ | $\begin{gathered} -0.030^{* * *} \\ (0.002) \end{gathered}$ |
| Firm-Occ-Year FE | Y | Y | Y | Y |
| CZ FE | Y | Y | N | N |
| CZ-Year FE | N | N | Y | Y |
| Observations | 792,656 | 733,576 | 792,656 | 733,576 |
| $\mathrm{R}^{2}$ | 0.833 | 0.861 | 0.853 | 0.862 |
| Adjusted $\mathrm{R}^{2}$ | 0.763 | 0.802 | 0.790 | 0.802 |

Notes: Columns (1) and (2) present estimates with commuting zone (CZ) fixed effects for the ordinary least squares (OLS) and instrumental variable (IV) exercises. The instruments in this table are lagged concentration measures $\frac{1}{N_{m, t-1}}$. Columns (3) and (4) present the analogous with commuting zone-year fixed effects. The dependent variable $\log \left(w_{i o, t}\right)$ is the logarithm of establishment-occupation wage at time $t . s_{i o \mid m, t}$ is the establishment-occupation employment share at time $t .{ }^{*} \mathrm{p}<0.1$; $^{* *} \mathrm{p}<0.05 ;{ }^{* * *} \mathrm{p}<0.01$
(3) present the Ordinary Least Squares (OLS) estimates. This econometric model reflects both labor demand and supply therefore a direct OLS estimation of (2) is theoretically problematic and expected to be biased towards zero. We indeed find that both OLS estimates are very close to zero and positive. Columns (2) and (4) present the results once we instrument for the employment share. Both specifications (with CZ and CZ-year fixed effects) give the same point estimates. Those imply that an increase of one percentage point (p.p. henceforth) of the local labor market share is associated with a decrease of $0.03 \%$ of the plant wage. This implies that the same establishment passing from the first to the third quartile of the employment share distribution reduce $0.68 \%$ the wages. This elasticity translates into a reduction of roughly 190 euros of the median yearly establishment-occupation wage.

## Labor Shock to Competitors

We propose a second reduced form estimation to provide further evidence on the causal link between labor market concentration and wages. We now instrument the endogenous employment shares by using quasiexperimental variation coming from mass layoffs to competitors. The instrument is built by the presence of a firm having a national mass layoff in the same local labor market as non affected establishments. We expect that a national level shock is exogenous to the residual within firm-occupation variation across local labor markets that identifies the effect. Here we provide some detail of the construction of the instruments that is complemented in Appendix F.

We first need to identify the firms suffering from a mass layoff. We classify a firm-occupation as having a mass layoff if the establishment-occupation employment at $t$ is less than a threshold $\kappa \%$ of the employment last year for all the firm establishments. Ideally we would like to identify firms that went bankrupt ( $\kappa=$ $0)$. Unfortunately, we cannot externally identify if a firm disappears because it went bankrupt or changes identifiers keeping the number of competitors at the local market constant. Our instrument is a proxy to capture the impact of a firm's bankruptcy into the competitors. ${ }^{14}$ We restrict the sample to non affected firm-occupations with establishments in local labor markets with and without a competitor suffering a mass layoff. In particular, we use the subsample of firms that have establishments at local labor markets hit by a mass layoff shock to a competitor and without mass layoff shocks.

There is a trade-off when choosing $\kappa$. A lower threshold leads to considering stronger negative shocks and the generated instrument will be cleaner, but it reduces the number of events considered. This creates a bias-variance trade-off in the selection of the threshold. Lacking a clear candidate for $\kappa$, we try different cut-off values. ${ }^{15}$

Results with commuting zone fixed effects are in Figure 1. OLS estimates of $\beta$ from (2) are in blue slightly above zero and IV estimates are in red. ${ }^{16}$ Both are plotted with $95 \%$ confidence intervals. ${ }^{17}$

[^9]Figure 1: Impact of Employment Share on Wages


Note: This figure presents the point estimates and $95 \%$ confidence bands of the OLS and IV exercises on the y-axis. The x-axis presents different thresholds $\kappa$ that define a mass layoff shock. The instrument is the presence of a mass layoff shock firm in the local labor market. We focus on non-affected competitors (not suffering a mass layoff shock). The specification is as (2) with commuting zone fixed effects. Results with commuting zone-year fixed effects are in Section 3.3.

The employment share being endogenous, the estimated effect with OLS is biased up and closer to zero. OLS estimates are in line with the column (3) of Table 5. The Figure shows clearly the trade-off in the selection of the cutoff $\kappa$. The lower the threshold, the stronger the impact but higher the variance of the estimated effect. With $\kappa=20 \%$ we estimate an elasticity of 0.17 . A one p.p. increase in the employment share causes a $0.17 \%$ decrease of the establishment wage. This translates into a wage loss of roughly 1000 euros when passing from the first to the third quartile of employment shares. ${ }^{18}$ For the more standard threshold of $\kappa=70 \%$ (reduction of $30 \%$ employment) the elasticity is almost divided by 4 to 0.06 which implies a twice as big reduction as with the first instrument. This is twice the estimated loss with lagged concentration measures. As we increase the threshold the estimated coefficient converges to the OLS estimate.

### 3.3 Robustness Checks

We perform several robustness checks by changing the instrument, the fixed effects and the definition of local labor market. Results are qualitatively unchanged.

Instrument. Panel (a) of Figure 9 in Appendix F. 2 shows a robustness check where the new instrument is not binary any more and takes into account the original employment share of the mass layoff establishments. Panel (b) of the same Figure shows the results from the specification with commuting zone times year fixed effects. Results are qualitatively unchanged from the baseline in both cases.

Local Labor Market. Figure 10 in Appendix F. 2 does the same exercise as in the main empirical strategy but changing the definition of local labor market. Local labor markets are here defined with 2-digit industries. ${ }^{19}$

[^10]The empirical evidence up to now focused on establishing the presence of employer labor market power of French manufacturing firms. We found that more concentrated industries have lower labor shares and firms pay lower wages in local labor markets where they have relatively higher labor market power. The last part of the empirical evidence aims to motivate the importance of unions in France.

### 3.4 Unions

The institutional framework of the French labor market is characterized by legal requirements that give unions an important role even in medium sized firms.

French labor market is known to be one where unions are relevant players, despite the fact that trade union affiliation in France is among the lowest of all the OECD countries. ${ }^{20}$ According to administrative data, the unionization rate in France was $9 \%$ in $2014 .{ }^{21}$ This unionization rate is slightly below to the one in the U.S. (10.7\%) and well below the ones in Germany (17.7\%) or Norway (49.7\%).

Low affiliation rates do not translate into low collective bargaining coverage for the French case. Collective bargaining agreements extend almost automatically to all the workers, unionized or not. That is, if an agreement is reached in a particular sector, all the workers within the sector are covered. Table 6 presents the unionization and collective bargaining coverage rates for several countries. This institutional framework implies that coverage of collective agreements was in 2014 as high as $98.5 \%$ in France despite the low union affiliation rates. ${ }^{22}$ This is in stark contrast to the U.S. collective bargaining agreements that only apply to union members and therefore coverage is very similar to the unionization rate.

Collective bargaining can happen at different levels. Firms and unions can negotiate at some aggregate level (e.g. industry, occupation, region) and also at economic units such as the group, firm or plant. ${ }^{23}$ When wage bargaining happens at the firm level it affects all the workers. Most firms that explicitly bargaining over the wages do so at the firm level (rather than at the plant or occupation level). $92 \%$ of mono-establishment firms with a specific collective bargaining agreement in 2010, negotiated it at the firm level. Only 9\% of the multi-establishment firms with specific agreements negotiated exclusively at the establishment level. ${ }^{24}$

Legal requirements regarding union representation depend on firm or plant size. First requirements start when the establishment reaches 10 employees and there is an important tightening of duties when reaching the threshold of 50 employees. ${ }^{25}$ As a consequence, firm level wage bargaining is common even at relatively small establishments. $52 \%$ ( $51 \%$ ) of establishments with at least 20 employees bargained over the wages in 2010 (in 2004). ${ }^{26}$

The prevalence of wage bargaining in the French labor market suggests it is an important element to incorporate into the structural model. Having established the existence of employer labor market power and the importance of unions, next section lays out a model in line with the stylized facts and the French labor market institutions.

[^11]Table 6: Union Density and Collective Bargaining Coverage

| Country | Union Density | Coverage |
| :--- | :---: | :---: |
| Australia | 15.10 | 59.91 |
| Austria | 27.70 | 98.00 |
| Canada | 29.30 | 30.40 |
| Chile | 15.30 | 19.33 |
| Finland | 67.60 | 89.30 |
| France | 9.00 | 98.46 |
| Germany | 17.70 | 57.80 |
| Ireland | 26.30 | 33.52 |
| Italy | 36.40 | 80.00 |
| Japan | 17.50 | 16.90 |
| Korea | 10.00 | 11.90 |
| Netherlands | 18.10 | 85.93 |
| Norway | 49.70 | 67.00 |
| Spain | 16.80 | 80.16 |
| Switzerland | 16.10 | 49.23 |
| Turkey | 6.90 | 6.63 |
| United Kingdom | 25.00 | 27.50 |
| United States | 10.70 | 12.30 |

Notes: Year 2014. All the variables are in percents. Union Density is the unionization rate which is unionized workers relative to total employment. Coverage is the collective agreement coverage; the ratio of employees covered by collective agreements divided by all wage earners with the right to bargain. The sources are administrative data except for Australia, Ireland and United States which are based on survey data.

## 4 Model

The economy consists of discrete sets of establishments $\mathcal{I}=\{1, \ldots, I\}$, locations $\mathcal{N}=\{1, \ldots, N\}$ and industries $\mathcal{B}=\{1, \ldots, B\}$. Each establishment can have several occupations $o \in \mathcal{O}=\{1, \ldots, O\}$. Each establishment $i$ is located in a specific location $n$ and belongs to sub-industry $h$ in a particular industry $b$. We define a local labor market $m$ as the combination between location $n$, sub-industry $h$ and occupation $o$, i.e. $m=n \times h \times o$.

We denote the set of establishments that are in local labor market as $\mathcal{I}_{m}$ with cardinality $N_{m}$. We define the set of all local labor markets $m$ as $\mathcal{M}$ and the set of all sub-markets in industry $b$ (in sub-industry $h$ ) as $\mathcal{M}_{b}\left(\mathcal{M}_{h}\right)$. The distribution of establishments across local labor markets is determined exogenously. Every establishment can only belong to one location and one sub-sector but can have several occupations and therefore belong to different local labor markets. We define the set of sub-markets that have at least one establishment of sector $b$ as $\mathcal{N}_{b}$.

The economy is populated by an exogenous measure $L$ of workers who are homogeneous in ability but
heterogeneous in tastes for different workplaces. They decide their workplace (establishment-occupation) in two steps without any restriction on mobility. First, workers choose in which local labor market $m$ they would like to be employed, and second, they choose in which establishment $i$ of that sub-market they will work. Workers do not save so they do not own any capital.

Capital and output markets are competitive. Industry specific rental rates of capital $R_{b t}$ are exogenous. Establishments are owned by entrepreneurs who rent the capital and collect the profits. ${ }^{27}$ Those are not explicitly modeled and therefore are excluded from the welfare analysis.

We propose a 'right-to-manage' model where firms and workers bargain over the wages at the establishmentoccupation io level. The equilibrium bargained wage is the solution to a reduced form Nash bargaining problem. Once they are hired, workers force a negotiation process over the wages. They internalize that if bargaining were to fail, employers compete in an oligopsponistic fashion. We therefore assume that workers' outside options are oligopsonistic competition outcome wages. This means that if bargaining were to fail, workers would earn wages with a markdown over their marginal revenue product. On the contrary, the threat point of employers when entering the negotiation is having zero profits. If they were not able to agree on the wage setting process and cannot hire anyone, their production and profits would be null.

If bargaining were to fail, establishments post wages per occupation in order to attract workers taking into account the labor supply they face. Having a discrete set of establishments per local labor market means they internalize the effect of their wages on the labor supply of their most immediate competitors. This reflects the idea that competition for labor is mostly local. Geography in our model is only important to define local labor markets.

Below we first set up the production side of the economy and workers' labor supply decisions. Second we present equilibrium wages in the absence of bargaining (wages in the oligopsonistic competition case) and finally we incorporate bargaining to the model.

## Production

The final good $c$ is produced by a representative firm with an aggregate Cobb-Douglas production function using as inputs a composite good $Y_{b}$ for each industry $b$ :

$$
\begin{equation*}
Y=\prod_{b \in \mathcal{B}} Y_{b}^{\theta_{b}}, \tag{3}
\end{equation*}
$$

where $\theta_{b}$ is the elasticity of the intermediate good produced by firms in sector $b$ and $\sum_{b} \theta_{b}=1$. Profit maximization implies that the representative firm spends a fixed proportion $\theta_{b}$ on the industry composite $Y_{b}$ :

$$
\begin{equation*}
P_{b} Y_{b}=\theta_{b} P Y \tag{4}
\end{equation*}
$$

The final good price, which we choose as the numeraire, is equal to:

$$
P=1=\prod_{b \in \mathcal{B}}\left(\frac{P_{b}}{\theta_{b}}\right)^{\theta_{b}} .
$$

Firms produce in a perfectly competitive goods market. $P_{b}$ is the price of the homogeneous good produced by every firm in sector $b, Y_{b}$ is their production and $P$ is the price of the final good which we take as a

[^12]numeraire. $Y_{b}$ is the aggregate of output of all the firms in that sector:
\[

$$
\begin{equation*}
Y_{b}=\sum_{i \in \mathcal{I}_{b}} y_{i} \tag{5}
\end{equation*}
$$

\]

where $\mathcal{I}_{b}$ is the set of establishments that belong to industry $b$. The establishment production function $y_{i}$ is an aggregate of occupation productions. Establishment $i$ produces using occupation $o$ specific inputs, labor $L_{i o}$ and capital $K_{i o}$, with a decreasing returns to scale technology. Output elasticity with respect to labor $\beta_{b}$ and capital $\alpha_{b}$ are industry specific and establishment-occupations are heterogeneous in their total factor productivity. We assume that occupations are perfect substitutes and their output is aggregated linearly. That is, total establishment output $y_{i}$ is the sum of occupation specific outputs $y_{i o}$. Decreasing returns to scale in the occupation output $y_{i o}$ generate an incentive to produce using several occupations.

Establishment $i^{\prime}$ s output, $y_{i}$, is defined as:

$$
\begin{equation*}
y_{i}=\sum_{o=1}^{O} y_{i o}=\sum_{o=1}^{O} \widetilde{A}_{i o} K_{i o}^{\alpha_{b}} L_{i o}^{\beta_{b}} . \tag{6}
\end{equation*}
$$

The choice of this particular production function is motivated by theoretical and empirical reasons. The linearity of the aggregation within establishments allows for the separability of different local labor markets. ${ }^{28}$ The second reason is data motivated. The absence of a particular occupation in an establishment can be rationalized by having null productivity in that particular occupation. An alternative specification where labor is a Cobb-Douglas composite of occupations is at odds with the pervasive prevalence of missing at least one occupation category. The median establishments lacks at least one occupation. Lacking a particular occupation, those establishments would not be able to produce if labor is a Cobb-Douglas composite of occupations. Appendix H lays out the model and proofs with this alternative production function.

The separability of local labor markets comes from restricting the inverse elasticity of labor demand to be equal across different industries. We assume that output elasticities with respect to capital $\alpha_{b}$ and labor $\beta_{b}$ are such that: $\frac{\beta_{b}}{1-\alpha_{b}}=1-\delta$, where $\delta \in[0,1]$ is a constant across sectors. This specification nests constant returns to scale when $\delta=0$. As long as $0<\delta<1$ the establishment faces decreasing returns to scale within occupations. This assumption together with the linearity of the production function give us separability of the local labor markets. This is further discussed in Section 4.4.

Substituting optimal demand for capital, the establishment-occupation production is:

$$
\begin{equation*}
y_{i o}=F_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)} A_{i o} L_{i o}^{1-\delta}, \quad A_{i o} \equiv \widetilde{A}_{i o}^{\frac{1}{11-\alpha_{b}}}\left(\frac{\alpha_{b}}{R_{b}}\right)^{\frac{\alpha_{b}}{1-\alpha_{b}}} \tag{7}
\end{equation*}
$$

$A_{i o}$ is a transformed productivity of $i o$ that incorporates elements coming from the optimal demand of capital and $F_{b}$ is a transformed industry $b$ price. ${ }^{29}$ Details of these derivations are in Appendix A. From now on we work with the production function with optimal demand for capital.

## Labor Supply

We now present worker preferences that give rise to upward sloping establishment-occupation specific labor supplies. A worker $k$ receives utility by consuming a single final good $c$ and by the product of two idiosyncratic utility shocks: one establishment-occupation specific preference shifter $z_{k i o}$ and another one common

[^13]for all establishments in local labor market $m, u_{k m}$. The utility of a worker $k$ working for establishment $i$ at occupation $o$ in local labor market $m$ is:
\[

$$
\begin{equation*}
\mathcal{U}_{k i o}=c_{k} z_{k i o} u_{k m} . \tag{8}
\end{equation*}
$$

\]

Following Eaton and Kortum (2002) in the trade literature and Redding (2016) and Ahlfeldt et al. (2015) in urban economics literature we assume that the idiosyncratic utility shocks are drawn from a Fréchet distribution:

$$
\begin{array}{r}
P(z)=e^{-T_{i 0} z^{-\varepsilon_{b}}}, \quad T_{i o}>0, \varepsilon_{b}>1 \\
P(u)=e^{-u^{-\eta}}, \quad \eta>1 \tag{10}
\end{array}
$$

where the parameter $T_{i o}$ determines the average utility derived from working in establishment $i$ and occupation $o$. In contrast, we normalize these parameter to 1 for the sub-market specific shock $u$. The shape parameters $\varepsilon_{b}$ and $\eta$ control the dispersion of the idiosyncratic utility. They are inversely related to the variance of the preference shifters. We name the parameters $\varepsilon_{b}$ and $\eta$ as the within and across labor market elasticities. If both have high values workers have similar tastes for different local labor markets and establishment-occupations. This in turn implies that their labor supply is more elastic and will react more to changes in wages.

The labor supply elasticities in this framework are different from the ones studied by public economists. Our baseline model features a constant level of aggregate employment and workers do not decide the amount of hours to work but rather the workplace to which they want to supply their labor. The Frisch elasticity of labor supply is zero in our baseline environment but yet workers do not supply their labor inelastically to any establishment.

We assume that establishments cannot discriminate workers based on their taste shocks. This implies that establishment $i$ for occupation $o$ pays the same wage $w_{i o}$ to all its employees, leaving the marginal worker indifferent between working in io or moving. Small wage reductions induce the movement of the marginal worker but infra-marginal workers stay. One can view these taste shocks as mobility costs in a static model.

The only source of worker income are wages, therefore the indirect utility of worker $k$ is:

$$
\begin{equation*}
\mathcal{U}_{k i o}=w_{i o} z_{k i o} u_{k m}, \tag{11}
\end{equation*}
$$

where the last two elements are the taste shocks. A worker chooses where to work in two steps: first, they choose their local labor market after observing local labor market shocks $u_{k m}$. After picking a local labor market, the worker then observes the establishment idiosyncratic shocks and chooses the establishment that maximizes expected utility. Following the usual derivations as in Eaton and Kortum (2002), the probability of a worker choosing establishment $i$ and occupation $o$ is a product of two terms: the employment share of the establishment-occupation within the local labor market $s_{i o \mid m}$ and the employment share of the local labor market itself $s_{m}$. We develop the derivations in Appendix A. The probability $\Pi_{i o}=s_{i o \mid m} \times s_{m}$ writes as:

$$
\begin{equation*}
\Pi_{i o}=\frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\sum_{j \in I_{m}} T_{j o} w_{j o}^{\varepsilon_{b}}} \times \frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\sum_{m^{\prime} \in \mathcal{M}} \Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}, \tag{12}
\end{equation*}
$$

where $\Phi_{m}=\sum_{j \in I_{m}} T_{j} w_{j o}^{\varepsilon_{b}}$ is a local labor market aggregate, the functional $\Gamma_{b}$ is independent of the endogenous variables and the economy wide constant $\Phi$ is $\Phi=\sum_{m \in \mathcal{M}} \Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}$. In equilibrium, the first fraction is equal to $s_{i o \mid m}$ and the second term in (12) is $s_{m}$.

Integrating over the continuous measure of workers $L$, the labor supply $L_{i o}$ for establishment and occupation $o$ is:

$$
\begin{equation*}
L_{i o}\left(w_{i o}\right)=\frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\Phi_{m}} \frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi} L=\Pi_{i o} L \tag{13}
\end{equation*}
$$

The inverse of this labor supply is upward sloping as long as the within and across local labor market elasticities are bounded. In the limit where both tend to infinity, workers are indifferent across workplaces and the inverse labor supply becomes flat.

### 4.1 Absence of Bargaining

In this section we characterize equilibrium wages in the absence of bargaining. Given the labor supply curves with bounded elasticities, establishments post wages taking into account the labor supply curves (13) they face. This monopsony power translates into a markdown between the wages and the marginal revenue products of labor. When the establishments solve their wage posting problem, they look at probability $\Pi_{i o}$ and take into account the effect of wages on the establishment-occupation term $T_{i o} w_{i o}^{\varepsilon_{b}}$ and also on the local labor market aggregate $\Phi_{m}$. However, they take as given economy wide aggregates ( $\Phi$ and L). ${ }^{30}$ The finite set of establishments per local labor market generates strategic interaction among the competitors. The strategic interaction within a local labor market induces oligopsonistic competition that features a heterogeneous markdown.

The first order condition for the establishment-occupation wage io under oligopsonistic competition is:

$$
\begin{equation*}
w_{i o}^{M P}=\frac{e_{i o}}{e_{i o}+1} \beta_{b} A_{i o} L_{i o}^{-\delta} P_{b}^{\frac{1}{1-\alpha_{b}}} \tag{14}
\end{equation*}
$$

where $e_{i o}=\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}$ is the perceived labor supply elasticity. This expression is similar to Card et al. (2018) with the difference that we have variable perceived elasticities that arise from the strategic interaction between establishments. We denote with a subscript $M P$ the equilibrium wage when there is only employer labor market power. The fraction $\frac{e_{i o}}{e_{i 0}+1}$ in equation (14) is the markdown and it is defined as:

$$
\begin{equation*}
\mu\left(s_{i o \mid m}\right)=\frac{\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}}{\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}+1} . \tag{15}
\end{equation*}
$$

In the absence of bargaining, the wedge between the marginal revenue product of labor and the wages boils down to a markdown (15). ${ }^{31}$ We denote this object in short notation as $\mu_{i o}$.

As long as workers are less elastic across local labor markets than across establishments within a given local labor market (i.e. as long as $\eta<\varepsilon_{b}$ ), the markdown (15) is a decreasing function of the share of employment $s_{i o \mid m}$. Once an establishment is big with respect to the nearby competitors, it internalizes that it is facing a more inelastic labor supply and applies a more important markdown. In the limit where $\varepsilon_{b}$ and $\eta$ tend to infinity, establishments face an infinitely elastic labor supply and a perfectly competitive labor market rises with $\mu\left(s_{i o \mid m}\right)=1$.

Heterogeneous markdowns distort relative wages across establishment-occupations and therefore the labor supplies. This implies that the labor allocation to a particular establishment-occupations is different to

[^14]the one if the markdowns were absent. Distorting the labor allocation across the production units, the heterogeneous markdown generates misallocation of resources and potentially reduces aggregate output even at the case where total employment is fixed. We formalize the source of misallocation in Section 4.4. ${ }^{32}$

When the markdown is constant and total labor supply fixed, labor market power does not have efficiency consequences as it only affects the division of output into the labor share and the profit share. This is not any more true if we were to allow an endogenous leisure or labor force participation decisions. Counterfactually increasing wages would increase total labor supply $L$ and therefore total output. ${ }^{33}$

### 4.2 Bargaining

We now introduce the bargaining between employers and unions. We assume that bargaining happens at the establishment-occupation level and involves only wages rather than indirect utilities because workers do not know each others' taste shocks. Given the perfect substitutability of occupations in the production function, bargaining at the occupation level is equivalent to a situation where bargaining happens at the establishment level but there are different wage agreements per occupation.

When they are hired, workers force the negotiation over the wages in order to earn above the statusquo. Workers understand the nature of employer labor market and take the wages under oligopsonistic competition as their threat points. Their reservation wage is therefore: $w_{i o}^{r}=\mu_{i o} \times M R P L$. We assume that firms on the contrary act naively and take as threat points a situation without production or profits.

The bargained equilibrium wage is the solution to a reduced form Nash bargaining where union's bargaining power is $\varphi_{b}$ and the one of the establishment is $1-\varphi_{b}$. Appendix A. 4 gives more detail on the bargaining set up and discusses other situations that lead to the same negotiated equilibrium wages.

The equilibrium bargained wage is:

$$
\begin{equation*}
w_{i o}=\underbrace{\left[\left(1-\varphi_{b}\right) \mu_{i o}+\varphi_{b} \frac{1}{1-\delta}\right]}_{\text {Wedge } \lambda\left(\mu_{i o}, \varphi_{b}\right)} \times \underbrace{\beta_{b} A_{i o} L_{i o}^{-\delta} P_{b}^{\frac{1}{1-\alpha_{b}}}}_{\text {MRPL }} \tag{16}
\end{equation*}
$$

The wedge between equilibrium wages and the marginal revenue product of labor, $\lambda\left(\mu_{i o}, \varphi_{b}\right) \equiv\left(1-\varphi_{b}\right) \mu_{i o}+$ $\varphi_{b} \frac{1}{1-\delta}$, is a combination of two parts. First, the markdown $\mu_{i o}$ coming from the oligopsonistic competition in the absence of bargaining, and second, the markup $\frac{1}{1-\delta}$ coming from the bargaining process. The markup is a consequence of the ability of the union to extract quasi-rents coming from the decreasing returns to scale $1-\delta<1 .{ }^{34}$ Bargained wages will be above or below the marginal revenue product depending on the union's bargaining power $\varphi_{b}$ and the relative strength of markdowns and markups. This comes from the fact that the term inside brackets is a convex combination between $\mu_{i o}<1$ and $\frac{1}{1-\delta}>1$.

In our calibrated model, labor supply elasticity $e_{i o}$ is decreasing in the local labor market employment share. Hence, even with bargaining $\left(0<\varphi_{b}<1\right)$, one would observe a negative relationship between employment shares $s_{i o \mid m}$ and wages $w_{i o}$. A desirable feature of the model is that it nests the oligopsonistic competition only and bargaining only as special cases. The former is equivalent to a situation where union's

[^15]bargaining power is zero $\varphi_{b}=0$. Equilibrium wages would be equal to a markdown times the marginal revenue product of labor $w^{M P}=\mu_{i o} \times M R P L$. A bargaining model without employer labor market power is encompassed when worker's outside option is the competitive wage. The wedge in that case is equal to: $1-\varphi_{b}+\varphi_{b} \frac{1}{1-\delta}=1+\varphi_{b} \frac{\delta}{1-\delta}$. The bargained wages incorporate a markup over the marginal product and become $w^{B}=\left(1+\varphi_{b} \frac{\delta}{1-\delta}\right) \times M R P L$. Workers are not only paid their marginal product but are also able to extract rents that come from the decreasing returns to scale. Rent extraction from the workers is governed by their bargaining power $\varphi_{b}$.

### 4.3 Equilibrium

For given industry rental rates of capital $\left\{R_{b}\right\}_{b=1}^{B}$, the general equilibrium of this economy is a set of wages $\left\{w_{i o}\right\}_{i o=1}^{I O}$, output prices $\left\{P_{b}\right\}_{b=1}^{B}$, a measure of labor supplies to every establishment and occupation $\left\{L_{i o}\right\}_{i o=1}^{I O}$, capital $\left\{K_{i o}\right\}_{i o=1}^{I O}$ and output $\left\{y_{i o}\right\}_{i o=1}^{I O}$, industry $\left\{Y_{b}\right\}_{b=1}^{B}$ and economy wide outputs $Y$, such that equations (3)-(13) and (16) are satisfied $\forall$ io $\in \mathcal{I}_{m}, m \in \mathcal{M}$ and $b \in \mathcal{B}$.

### 4.4 Characterization of the Equilibrium

Solving the model amounts to finding establishment wages, industry prices and allocations. In order to simplify the solution, we restrict the labor demand elasticity to be the same across industries. That is, we assume $\frac{\beta_{b}}{1-\alpha_{b}}=1-\delta$, where $\delta \in[0,1]$. This restriction implies the separability of the different local labor markets which allows us to split the solution in two. First, we take a partial equilibrium approach and solve for establishment-occupation components normalizing aggregates above the local labor market and show existence and uniqueness of the system of normalized wages. Second, we show that the model can be rewritten at the 2-digit industry level with the solution to these normalized wages and deep parameters. This last aggregate model is in turn enough to solve for industry prices.

Substituting the labor supply into (16) and simplifying we obtain:

$$
\begin{equation*}
w_{i o}=\left(\beta_{b} \lambda\left(\mu_{i o}, \varphi_{b}\right) \frac{A_{i o}}{\left(T_{i o} \Gamma_{b}^{\eta}\right)^{\delta}}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} \Phi_{m}^{\left(1-\eta / \varepsilon_{b}\right) v_{b}}\left(\frac{\Phi}{L}\right)^{v_{b}} F_{b}, \quad v_{b} \equiv \frac{\delta}{1+\varepsilon_{b} \delta} \tag{17}
\end{equation*}
$$

where $v_{b}=\frac{\delta}{1+\varepsilon_{b} \delta}$ is just an auxiliary parameter to ease notation.
To gain intuition on the allocation distortions from the heterogeneous wedges we focus on two establishments in the same local labor market. From (17), their relative wages are:

$$
\begin{equation*}
\frac{w_{i o}}{w_{j o}}=\left(\frac{\lambda\left(\mu_{i o}, \varphi_{b}\right)}{\lambda\left(\mu_{j o}, \varphi_{b}\right)}\right)^{\frac{1}{1+\varepsilon_{b} \delta}}\left(\frac{A_{i o}}{A_{j o}} \frac{T_{j o}^{\delta}}{T_{i o}^{\delta}}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} \tag{18}
\end{equation*}
$$

The ratio of heterogeneous labor wedges $\frac{\lambda\left(\mu_{i o}, \varphi_{b}\right)}{\lambda\left(\mu_{j o}, \varphi_{b}\right)}$ distorts the relative wages of the establishments at the same local labor market and consequently the labor supply (13). It is important to note that even in the absence of the labor wedge, in equilibrium, establishments pay different wages. This is a consequence of the workers' idiosyncratic taste shocks. In the limit where workers are infinitely elastic across establishments within the local labor market $\varepsilon_{b} \rightarrow \infty$, wages would be equalized. The same logic applies for differences across local labor markets and the respective elasticity $\eta$.

The first order condition (17) separates the establishment wage into terms constant for every establishment in sub-market $m\left(\Phi_{m}^{\left(1-\eta / \varepsilon_{b}\right) v_{b}}\left(\frac{\Phi}{L}\right)^{v_{b}} F_{b}\right)$ and establishment-occupation specific components of wages. We denote the latter as $\widetilde{w}_{i o}$ and are defined as:

$$
\begin{equation*}
\widetilde{w}_{i o}=\left(\beta_{b} \lambda\left(\mu_{i o}, \varphi_{b}\right) \frac{A_{i o}}{\left(T_{i o} \Gamma_{b}^{\eta}\right)^{\delta}}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} \tag{19}
\end{equation*}
$$

The real wage $w_{i o}$ is therefore $w_{i o}=\widetilde{w}_{i o} \Phi_{m}^{\left(1-\eta / \varepsilon_{b}\right) v_{b}}\left(\frac{\Phi}{L}\right)^{v_{b}} F_{b}$.
We can now establish existence and uniqueness of the system of equations (17) in partial equilibrium:
Proposition 1. For given parameters $\left\{\alpha_{b}, \beta_{b}, \varphi_{b}\right.$ s.t. $\left.0 \leq \alpha_{b}, \beta_{b}, \varphi_{b}<1, \forall b \in \mathcal{B}\right\}$ and $1<\eta<\varepsilon_{b} \forall b \in \mathcal{B}$, $0 \leq \delta \leq 1$, transformed price $F_{b}$, constants $\left\{\Phi_{m}\right\}, \Phi$, total labor supply $L$ and non-negative vectors of productivities $\left\{A_{i o}\right\}_{i o \in m}$ and amenities $\left\{T_{i o}\right\}_{i o \in m}$, there exists a unique vector of wages $\left\{w_{i o}\right\}_{i o \in I_{m}}$ for every local labor market $m$ that solves the system formed by (17).

Proof. See Appendix.
Proposition 1 tells us that if we take these aggregate terms as constants, then the solution for this system exists and is unique. Employment shares $s_{i o \mid m}$ are not affected if all local labor market wages are scaled up or down. This is a result of the wedges $\lambda\left(\mu_{i o}, \varphi_{b}\right)$ being homogeneous of degree zero with respect to local labor market constants. System (17) has a unique solution as we can use Proposition 1 with $\Phi_{m}=\Phi=L=F_{b}=1$.

We now turn to the second step of the model solution. Given the solutions to the establishment-occupation components we build industry level productivity measures and write the model at the industry $b$ level.

Starting from the lowest production unit (7) we aggregate up to industry output:

$$
\begin{equation*}
Y_{b}=F_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)} A_{b} L_{b}^{1-\delta}, \quad A_{b}=\sum_{i o \in \mathcal{I}_{b}} A_{i o} s_{i o \mid m}^{1-\delta} s_{m \mid b}^{1-\delta} \tag{20}
\end{equation*}
$$

where $A_{b}$ is an employment weighted productivity and $F_{b}$ is the transformed industry price. Solving the model now amounts to solving the system of intermediate good demand (4) to find industry prices. Using the final good production function (3) and the intermediate input demand (4),

$$
\begin{equation*}
F_{b}^{1+\varepsilon_{b} \delta} A_{b} L_{b}(\mathbf{F})^{1-\delta}=\theta_{b} \prod_{b^{\prime} \in \mathcal{B}}\left(F_{b^{\prime}}^{\alpha_{b^{\prime}}\left(1+\varepsilon_{b^{\prime}} \delta\right)} A_{b^{\prime}} L_{b^{\prime}}(\mathbf{F})^{1-\delta}\right)^{\theta_{b^{\prime}}} \tag{21}
\end{equation*}
$$

Steps to get to this expression are in Appendix A.5. Having the solution for normalized wages we can leave the industry labor supply $L_{b}$ and total output $Y$ as a function of the transformed prices $\mathbf{F}=\left\{F_{b}\right\}_{b \in \mathcal{B}}$.

Collecting all these expressions for the different industries forms a system of $B$ equations with $B$ unknowns. ${ }^{35}$ Solving for the vector of transformed prices $\mathbf{F}$ we can back out the rest of the variables in the model. Note that the system of equations is unchanged irrespective of the aggregate level of employment $L$ because the final good production function being constant returns to scale and industry employment $L_{b}$ is linear on aggregate labor supply.

Given the solution for normalized wages, we can think of industry productivity $A_{b}$ and industry level normalized wages $\widetilde{\Phi}_{b}$ as additional parameters at the industry level. The following proposition characterizes the solution for this system as a function of these parameters.

[^16]Proposition 2. For any set of parameters $\left\{\beta_{b}, \theta_{b} \quad\right.$ s.t. $\left.0 \leq \beta_{b}, \theta_{b}<1, \forall b \in \mathcal{B}\right\}, 0 \leq \delta \leq 1, \quad\left\{\psi_{b} \equiv \frac{1+\varepsilon_{b} \delta}{1+\eta \delta}\right\}_{b \in \mathcal{B}}$, non-negative vectors $\left\{A_{b}\right\}_{b \in \mathcal{B}}$ and $\left\{\widetilde{\Phi}_{b}\right\}_{b \in \mathcal{B}}$, there exists a unique vector of transformed prices $\mathbf{F}$ such that solves the system formed by (21) and it's characterized by:

$$
\begin{align*}
& F_{b}=X_{b} C^{\frac{1}{\psi_{b}(1+\eta)}},  \tag{22}\\
& X_{b}=\left(\frac{\theta_{b}}{A_{b}\left(\widetilde{\Phi}_{b} \Gamma_{b}^{\eta}\right)^{(1-\delta)}}\right)^{\frac{1}{\psi_{b}(1+\eta)}}, \quad C=\left(\prod_{b^{\prime} \in \mathcal{B}}\left(\theta_{b^{\prime}} X_{b^{\prime}}^{-\chi_{b^{\prime}}}\right)^{\theta_{b^{\prime}}}\right)^{\frac{1+\eta}{\Sigma_{b^{\prime} \in \mathcal{B}^{\theta_{b^{\prime}}\left(1-\alpha_{b^{\prime}}\right)(1+\eta \delta)}}}}
\end{align*}
$$

for all $b \in \mathcal{B}$.
Proof. See Appendix.
Proposition (2) provides an analytical solution for the (transformed) industry prices. Given the aggregations of the establishment-occupation components up to the industry level, the solution of the prices is unique and is characterized in closed form.

Proposition 1 showed the existence and uniqueness of the establishment-occupation components. A useful characteristic of those components is that they are homogeneous of degree zero with respect to local labor market aggregates. We therefore have that the normalized wages (or establishment-occupation components) are independent of industry prices. By taking together Propositions 1 and 2 we therefore can then conclude that there exists a unique solution to the model for any set of valid parameters and vectors of productivities and amenities.

## 5 Estimation

In this section, we describe the estimation procedure and present the results. The parameters to estimate are the within and across local labor market elasticities $\left(\left\{\varepsilon_{b}\right\}_{b=1}^{B}\right.$ and $\eta$ respectively), the inverse elasticity of the labor demand $(\delta)$, the industry output elasticities $\left(\left\{\alpha_{b}\right\}_{b=1}^{B},\left\{\beta_{b}\right\}_{b=1}^{B}\right)$ and the workers' bargaining powers $\left(\left\{\varphi_{b}\right\}_{b=1}^{B}\right)$. Given our restriction $\delta$, we only need to calibrate either the capital elasticities $\left\{\alpha_{b}\right\}_{b=1}^{B}$ or the labor ones $\left\{\beta_{b}\right\}_{b=1}^{B}$.

We estimate the model in three steps. First, by exploiting differences in the variance-covariance matrix of structural shocks across occupations we identify the across local labor market labor supply elasticity $\eta$ and the inverse elasticity of labor demand $\delta$. Then, we calibrate the output elasticities of capital to match industry capital shares. Second, we estimate the within local labor market labor supply elasticities $\left\{\varepsilon_{b}\right\}_{b=1}^{B}$ by estimating the labor supply equation while instrumenting for the wages. Finally, we calibrate the union's bargaining powers $\left\{\varphi_{b}\right\}_{b=1}^{B}$ to match the industry labor shares.

We take advantage of the presence of establishment-occupations with $s_{i o \mid m}=1$ in the data. We name those establishment-occupations that are alone in a particular local labor market as full monopsonists. We restrict the sample to full monopsonists for the first estimation step. Being alone in their local labor markets, the only firm specific labor supply elasticity in play is the across local labor market one $\eta$. Identification of the within local labor market elasticities $\varepsilon_{b}$ requires to focus on the establishment-occupations competing with others in their local labor markets.

We start the estimation by restricting to full monopsonists to perform the first step of the estimation procedure. Being the only players in the local labor market, the labor wedge they apply is constant and equal
to $\mu(s=1)=\frac{\eta}{\eta+1}$. Their labor demand is:

$$
\begin{equation*}
w_{i o}=\left[\left(1-\varphi_{b}\right) \frac{\eta}{\eta+1}+\varphi_{b} \frac{1}{1-\delta}\right] \beta_{b} P_{b}^{\frac{1}{1-\alpha_{b}}} A_{i o} L_{i o}^{-\delta} \tag{23}
\end{equation*}
$$

and the labor supply they face is:

$$
\begin{equation*}
L_{i o}=\frac{T_{i o}^{\eta / \varepsilon_{b}} w_{i 0}^{\eta} \Gamma_{b}^{\eta}}{\Phi} L \tag{24}
\end{equation*}
$$

Similar labor supply and demand systems can be formed for each occupation. This system suffers from standard identification issues when we have simultaneous equations. Independent identification of each of the equations requires different instruments shifting only one of them.

Lacking such instruments, we follow the identification through heteroskedasticity approach of Rigobon (2003) to identify the across local labor market labor supply elasticity $\eta$ and the inverse elasticity of labor demand $\delta$. Our identification strategy is based on restrictions on the variance-covariance matrix of structural shocks. In our preferred specification, we group the occupations into two categories and assume that the covariance between the demand and supply shifters (productivity and amenity respectively) are constant within the occupation category. This assumption is in line with the idea that amenities such as working hours, repetitiveness of the tasks or more general working environments are similarly related to productivity. In our main specification we group occupations into white collar workers (top management and clerical) and blue collar (supervisor and operational). The assumption states that occupations within those two categories share the same relationship between productivity and amenities.

Taking logarithms and demeaning by substracting the industry $b$ average per year, the system for occupation $o$ is:

$$
\binom{\ln \left(L_{i o}\right)}{\ln \left(w_{i o}\right)}=\frac{1}{1+\eta \delta}\left(\begin{array}{cc}
1 & -\eta \\
\delta & 1
\end{array}\right)\binom{\frac{\eta}{\varepsilon_{b}} \ln \left(T_{i o}\right)}{\ln \left(A_{i o}\right)}
$$

We estimate the variance covariance matrix of employment and wages per occupation from the data. The restriction we impose on the variance-covariance matrix of the structural shocks is that the covariance between the labor demand shifter (the productivity) and the labor supply shifter (the amenity) is constant across occupations within the same category. Equalizing the covariances we obtain a system of equations that do not depend on the within local labor market labor supply elasticity $\varepsilon_{b}$ anymore. More details about the estimation are in Appendix D.

The second step is devoted to the calibration of the output and the within local labor market labor supply elasticities. We start by calibrating the capital elasticities. We follow Barkai (2016) to construct the industry interest rates or required rates $\left\{R_{b t}\right\}_{b=1}^{B}$ per year and target the average industry capital shares. ${ }^{36}$ From the first order condition for capital, the industry $b$ capital share of output is: ${ }^{.37}$

$$
\frac{R_{b t} K_{b t}}{P_{b t} Y_{b t}}=\alpha_{b} .
$$

We calibrate $\alpha_{b}$ such that $\mathbb{E}_{t}\left[\left.\frac{R_{b t} K_{b t}}{P_{b t} Y_{b t}} \right\rvert\, b\right]=\alpha_{b}$. Given our restriction of constant inverse labor demand elasticity $\delta$, we back out the output elasticities with respect to labor by using $\frac{\beta_{b}}{1-\alpha_{b}}=1-\delta$.

[^17]The within market labor supply elasticities $\varepsilon_{b}$ are estimated exploiting the labor supply equation of non full monopsonists. The labor supply they face (13) in logs is:

$$
\ln \left(L_{i o}\right)=\varepsilon_{b} \ln \left(w_{i o}\right)+f_{m}+\ln \left(T_{i o}\right)
$$

where $f_{m}$ is a local labor market constant. At this point of the estimation the amenities $T_{i o}$ are unobserved. The usual exclusion restrictions when running this regression requires that the conditional expectation of the error term (here, the amenity) is equal to zero. Everything else equal, higher amenity establishments pay lower wages. We instrument for the wages using a proxy $\widehat{A}$ of firm productivity.

$$
\widehat{A}=\frac{P_{b} Y_{J}}{\sum L_{i o}^{1-\delta}}
$$

The first estimation step did not require independence of the structural shocks. In order to minimize the potential of endogeneity bias of our instrument, we use the lag instrument instead of the contemporaneous one.

Finally, the union bargaining powers are pinned down by industry labor shares. In the model, labor share of any establishment $i$ and occupation $o$ at period $t$ is:

$$
\begin{equation*}
L S_{i o}=\frac{w_{i o} L_{i o}}{P_{b} y_{i o}}=\beta_{b} \lambda\left(\mu_{i o}, \varphi_{b}\right) \tag{25}
\end{equation*}
$$

where the only parameter left is $\varphi_{b}$ in the wedge function $\lambda\left(\mu_{i o}, \varphi_{b}\right)=\left(1-\varphi_{b}\right) \frac{\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}}{\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}+1}+\varphi_{b} \frac{1}{1-\delta}$. Writing the analogous at the industry level, the union bargaining power $\varphi_{b}$ is pinned down by the average industry labor share. When constructing the theoretical labor share, we assume that given the estimated parameters, we later perfectly match the observed wages of establishments and labor allocations. We do not target the unobserved establishment-occupation value added and therefore neither the industry value added measures. ${ }^{38}$ For now, we assume that we match the wages and labor allocations in equilibrium. Details of how we back out amenities $T_{i o}$ to ensure that are in Appendix E.5.

We additionally need to calibrate the elasticities of the final good production function in order to be able to compute counterfactuals. Table 15 in Appendix D. 3 has the calibrated elasticities and interest rates for 2007, our baseline year for the counterfactuals. The next Section presents the estimation results and the goodness of the fit.

### 5.1 Estimation Results

Table 7 recovers the estimation results of the main parameters. The most important parameters of the estimation are arguably the firm specific labor supply elasticities and the union bargaining powers.

The estimated across local labor market elasticity is $\hat{\eta}=0.42$ and the industry specific local labor market labor supply elasticities $\widehat{\varepsilon}_{b}$ range from 1.22 to $4.05 .{ }^{39} \eta$ and $\varepsilon_{b}$ are inversely related to the variances of the taste shocks. The across local labor market elasticity being lower than the within ones ( $\left.\widehat{\varepsilon}_{b}>\widehat{\eta} \quad \forall b\right)$, workers are more likely to change workplaces within than across local labor markets. This implies that the markdown $\mu_{i o}$ is more relevant (further away from 1) for establishments having higher employment shares out of the local labor market. Consequently, the structural labor wedge $\lambda\left(\mu_{i o}, \varphi_{b}\right)$ of our calibrated model is decreasing in employment shares $s_{i o \mid m}$. This feature is in line with the empirical evidence from Section 3.

[^18]Table 7: Main Estimates

| Param. | Name | Estimate | Identification |
| :---: | :--- | :---: | :--- |
| $\eta$ | Across labor market elast. | 0.42 | Heteroskedasticity |
| $\delta$ | 1 - Returns to scale | 0.04 | Heteroskedasticity |
| $\left\{\varepsilon_{b}\right\}$ | Within labor market elast. | $1.2-4$ | Labor supply |
| $\left\{\beta_{b}\right\}$ | Output elast. labor | $0.57-0.85$ | Capital share and $\delta$ |
| $\left\{\varphi_{b}\right\}$ | Union bargaining | $0.06-0.7$ | Industry LS |

Comparing our labor supply elasticities to the recent estimates for the U.S. from Berger et al. (2019) for the US, they are qualitatively similar. Their analogous estimate of the across local labor market elasticity $\eta$ is 0.66 (compared to our estimate of 0.42 ) and their estimated within local labor market elasticity is 5.38 . The across local labor market estimates are very similar. On the contrary, all of our industry specific within local labor market elasticities lie below their estimate. This might be a consequence of the low mobility that characterizes the French labor market. ${ }^{40}$

The estimates of union bargaining power range from 0.06 for Chemical to 0.73 for Telecommunications. According to our estimates, there is an important heterogeneity of bargaining power across industries. Lacking direct estimates of bargaining power within manufacturing we validate our estimates by two comparisons. First, French labor law imposes more restrictive legal duties regarding union representation for larger establishments. We compute the correlation between the bargaining power estimates $\widehat{\varphi}_{b}$ and average plant or firm size (in terms of employment) per industry. We find a positive correlation of 0.33 between average establishment employment per industry and union's bargaining power $\varphi_{b} .^{41}$ Second, Cahuc et al. (2006) provide manufacturing bargaining power estimates for France in a framework of search and matching with on the job search. Our estimated bargaining power for manufacturing as a whole is $0.37 .{ }^{42}$ This is close to the estimate of Cahuc et al. (2006) for top management workers of 0.35.

The estimate of the inverse labor demand elasticity, $\delta$, is $\widehat{\delta}=0.04$. This parameter is also related to the average returns to scale of the production function which are about 0.97 . The combination of $\delta$ and the estimated capital elasticities per industry $\left\{\alpha_{b}\right\}$ allow us to recover the values for the output elasticity with respect to labor. We have that $\left\{\beta_{b}\right\}$ is equal to $\beta_{b}=\left(1-\alpha_{b}\right)(1-\delta)$. Labor elasticities go from 0.56 for Transport to the 0.85 for Shoe and leather production.

### 5.2 Estimation Fit

Using the point estimates we check the fit of the model for non-targeted moments. Figure 2 depicts the fit of the model and the non-targeted data. In panel (a) we have industry labor shares per year. On the horizontal axis we have the model generated moments while on the vertical axis we observed the corresponding moment in the data. If the fit was perfect, each dot would be on the 45 degree line. Each color represents an industry.

[^19]We see that most of the dots are aligned around the 45 degree line. Next to it, in panel (b), we show the fit to aggregate value added.

We can check the model does against other non-targeted moments. Panel (a) of Figure 2 shows the model matches value added per industry. This in fact might not be surprising as there is a very strong relationship between establishment's production and wage bill in the model and in the data. Since the model exactly matches the establishment's wages and labor allocations, it also has a good fit of the value added. The second non-targeted moment is the evolution of the aggregate value added, shown in panel (b) of the same figure. The model also does a very good job following the actual data.

Figure 2: Model Fit Non Targeted Moments

(a) Sub-industry Labor Share

(b) Aggregate Value Added. Model in dashed blue, data in red.

Table 8: Concentration and Labor Share: Data vs. Model

|  | Data: $\log \left(L S_{h, t}^{D}\right)$ |  | Oligopsony: $\log \left(L S_{h, t}^{M, M P}\right)$ |  | Model: $\log \left(L S_{h, t}^{M}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (1) | (2) | (3) | (4) | (5) | (6) |
| $\log \left(\overline{H H I}_{h, t}\right)$ | $\begin{gathered} -0.054^{* * *} \\ (0.013) \end{gathered}$ | $\begin{gathered} -0.056^{* * *} \\ (0.013) \end{gathered}$ | $\begin{gathered} -0.388^{* * *} \\ (0.009) \end{gathered}$ | $\begin{gathered} -0.416^{* * *} \\ (0.003) \end{gathered}$ | $\begin{gathered} -0.175^{* * *} \\ (0.007) \end{gathered}$ | $\begin{gathered} -0.161^{* * *} \\ (0.005) \end{gathered}$ |
| Ind FE | Y | N | Y | N | Y | N |
| Ind-Year FE | N | Y | N | Y | N | Y |
| Obs. | 1357 | 1357 | 1357 | 1357 | 1357 | 1357 |
| $\mathrm{R}^{2}$ | 0.29 | 0.343 | 0.901 | 0.903 | 0.946 | 0.909 |
| Adj. $\mathrm{R}^{2}$ | 0.280 | 0.172 | 0.899 | 0.878 | 0.945 | 0.936 |

Notes: The dependent variable of the first two Columns are the logarithm of 3-digit industry labor share at year $t, \log \left(L S_{h, t}^{D}\right)$. These present the results from Table 4 with fixed effects. Next two Columns present the model generated log labor shares $\log \left(L S_{h, t}^{M, M P}\right)$ when the model does not incorporate wage bargaining. This is a framework where the labor wedge $\lambda$ boils down to $\lambda\left(\mu_{i o}, 0\right)=\mu_{i o}$. Last two Columns present the analogous regressions with our framework where bargaining is incorporated $\log \left(L S_{h, t}^{M}\right)$. Throughout the different frameworks Column (1) presents estimates with industry fixed effects and Column (2) results with industry-year fixed effects. ${ }^{*} \mathrm{p}<0.1$; ${ }^{* *} \mathrm{p}<0.05 ;{ }^{* * *} \mathrm{p}<0.01$

To further investigate the model fit to non-targeted moments we repeat the aggregate empirical evidence of Section 3. Table 8 presents the empirical evidence of Table 4 with fixed effects (Columns (2) and (3)) in the first 2 Columns and the rest of the rest are devoted to compare two alternative models. Model results present the same regressions as the ones for the data for the model with oligopsonistic competition only $L S_{h, t}^{M, M P}$ (Columns (3) and (4)) and for our model with collective wage bargaining $L S_{h, t}^{M}$ (Columns (5) and (6)). The negative relationship between labor share and concentration in the model with oligopsonistic competition is about 8 times higher than in the data. Comparing now the last two Columns that correspond to our model, the negative relationship is still too strong but it is half of the model without bargaining. Models with bargaining only and with employer labor market power without strategic interactions would not match the data as the effect of concentration on the labor shares would be null.

## 6 Counterfactuals

In this section we evaluate efficiency and welfare effects of the labor wedges. We compute the main counterfactuals for the last year of our sample, 2007. We start by showing that counterfactuals can be computed observing establishment Revenue Total Factor Productivities (TFPRs) instead of the underlying productivities. Second, we perform our main counterfactual where we completely eliminate the structural labor wedges and compute output and welfare gains under free mobility of workers. We also consider other counterfactual situations where labor wedges remain and are equal to the bargaining only or oligopsonistic competition
only cases.
Our baseline counterfactuals assume free mobility of labor. We perform three additional counterfactuals relaxing the free mobility assumption to evaluate if output gains can be attained when mobility is restricted. First, in the most restrictive case, we allow movements only within local labor markets. This is equivalent to assuming infinite mobility costs across locations, industry and occupations. Second, we fix employment at the 2-digit and occupation level and let labor move across locations and 3-digit industries. Third, we fix employment at the 2-digit level. Compared to the previous case, labor is mobile across occupations.

We finally use the model to study the incidence of labor market power on the pass-through of productivity to wages, the urban-rural wage gap and de-industrialization process over time.

### 6.1 Fundamentals

This section shows that is possible to compute the counterfactuals in general equilibrium by just backing out the Revenue Total Factor Productivities (TFPRs), which are a function of prices determined in general equilibrium, rather than the underlying physical productivities. A priori, the issue is that counterfactually changing the labor wedge changes equilibrium prices and therefore the 'fundamental' TFPRs.

The literature has used the TFPRs, together with a modeling assumption on the industry price, to compute the normalized within industry productivity distribution. This has prevented to compute full blown general equilibrium counterfactuals that also take into account productivity differences across industries. ${ }^{43}$ We show that we can perform counterfactuals in general equilibrium by writing the model in relative differences from a baseline scenario and also compute the movement of production factors across industries.

We observe employment and wages at the establishment-occupation level from the data. The method is based on recovering establishment-occupation TFPRs using the wages' first order conditions. Equation (16) in nominal terms is:

$$
\begin{equation*}
P w_{i o}=\beta_{b} \lambda\left(\mu_{i o}, \varphi_{b}\right) P F_{b}^{1+\varepsilon_{b} \delta} A_{i o} L_{i o}^{-\delta} \tag{26}
\end{equation*}
$$

where $P w_{i o}$ and $L_{i o}$ are observed and $\beta_{b} \lambda\left(\mu_{i 0}, \varphi_{b}\right)$ depends on the estimated parameters and observed employment shares. Equation (26) makes clear that given the observed nominal wages and employment, one can only back out the transformed TFPRs $Z_{i o}=P F_{b}^{1+\varepsilon_{b} \delta} A_{i o}$ that are a function of the establishment-occupation physical productivity $A_{i o}$ and prices $P F_{b}^{1+\varepsilon_{b} \delta} .44$

Our approach is to write counterfactual industry prices relative to the baseline and fix the transformed revenue productivities. ${ }^{45}$ Using the definition of the transformed revenue productivities, the above equation

[^20](26) is:
$$
P w_{i o}=\beta_{b} \lambda\left(\mu_{i o}, \varphi_{b}\right) Z_{i o} L_{i o}^{-\delta} .
$$

We denote with a prime the variables in the counterfactual (e.g. $F_{b}^{\prime}$ ) and with hat the relative variables (e.g. $\widehat{F}_{b}=\frac{F_{b}^{\prime}}{F_{b}}$. We have that $Z_{i o}^{\prime}=P^{\prime}\left(F_{b}^{\prime}\right)^{1+\varepsilon_{b} \delta} A_{i o}=\widehat{P} \widehat{F}_{b}^{1+\varepsilon_{b} \delta} Z_{i o}$. Fixing the transformed TFPR's observed in the data, we can compute $Z_{i o}$. Denoting by $\lambda_{i o}^{\prime}$ the counterfactual wedge, the counterfactual real wages are:

$$
\begin{align*}
w_{i o}^{\prime} & =\beta_{b} \lambda_{i o}^{\prime} Z_{i o}^{\prime} L_{i o}^{\prime-\delta} \frac{1}{P^{\prime}} \\
& =\beta_{b} \lambda_{i o}^{\prime} Z_{i o} \frac{\widehat{F}_{b}^{1+\varepsilon_{b} \delta}}{P} L_{i o}^{\prime-\delta}, \tag{27}
\end{align*}
$$

where in the last step we used the definition of the transformed TFPRs. In the counterfactuals $Z_{i o}$ is fixed and we have to solve for industry prices relative to the baseline $w h F_{b}$.

Substituting the labor supply and solving for the wages the system becomes:

$$
\begin{equation*}
w_{i o}^{\prime}=\left(\beta_{b} \lambda_{i o}^{\prime} \frac{Z_{i o}}{\left(T_{i o} \Gamma_{b}^{\eta}\right)^{\delta}}\right)^{\frac{1}{1+\varepsilon_{b} b^{\delta}}} \frac{\widehat{F}_{b}}{P^{\frac{1}{1+\varepsilon_{b} \delta}}} \Phi_{m}^{\prime\left(1-\eta / \varepsilon_{b}\right) v_{b}}\left(\frac{\Phi^{\prime}}{L^{\prime}}\right)^{v_{b}} \tag{28}
\end{equation*}
$$

The establishment-occupation component in the counterfactual $\omega_{i o}$ is: $\omega_{i o}=\left(\beta_{b} \lambda_{i o}^{\prime} \frac{Z_{i o}}{\left(T_{i o} \Gamma_{b}^{\prime}\right)^{\delta}}\right)^{\frac{1}{1+\varepsilon_{b}{ }^{\delta}}}$.
Finally, the counterfactual conditional employment shares up to the industry level, $s_{i o \mid m o}^{\prime} s_{m \mid b}^{\prime}$ and industry employment $L_{b}^{\prime}$ can be computed. Following the same steps as in the baseline, the industry level system of equations is analogous to (21) but with relative variables. ${ }^{46}$ Propositions 1 and 2 apply and therefore the solution for the relative counterfactuals exists and is unique.

### 6.2 Main Counterfactuals

We consider four different situations. First, the main counterfactual presents a situation where labor wedges disappear and establishments and workers acts as price takers. Second, the limit case of our framework where there is only bargaining. Third, the limit case where employer labor market power is the only one present, and finally, a situation where unions collect all the profits.

Table 9 shows results of different counterfactuals under the free mobility assumption. The first Column present labor shares in the baseline and the counterfactuals and the rest of the Columns recover the percentage gains of the counterfactuals with respect to the baseline. Output gains are in Column 2 of Table 9. Eliminating labor wedges coming from employer and union labor market power increases aggregate output by $1.6 \%$.

The counterfactual without employer labor market power but keeping the one of unions almost attains the output gains from eliminating both distortions. This counterfactual is a situation where establishments would not internalize movements along the labor supply and the labor wedges become $\lambda\left(1, \varphi_{b}\right)=1+\varphi_{b} \frac{\delta}{1-\delta}$. It is important to note that this is due to the assumed institutional framework for the unions. The bargaining only case features a reduced heterogeneity of labor wedges (only different across industries) that is behind the result of almost attaining output gains of the main counterfactual.

Comparing now to the counterfactual with employer labor market power, we see that output is reduced by $0.21 \%$ with respect to the baseline. This result is despite the fact that total employment is fixed. The

[^21]mechanism behind this result is that labor wedges would be slightly more heterogeneous than in the baseline. Finally, output gains when there is full bargaining and workers extract all the profit rents are the same as in the main counterfactual as wedges would be constant.

Table 9: Counterfactuals: Efficiency and Distribution

|  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  |  |  | Gains (\%) |  |
|  | LS (\%) | $\Delta Y$ | $\Delta$ Wage | $\Delta$ Welfare (L) |
| Baseline | 50.62 | - | - |  |
| Counterfactuals |  |  |  |  |
| No wedges $\lambda\left(\mu, \varphi_{b}\right)=1$ |  |  |  |  |
| Not internalize $\lambda\left(1, \varphi_{b}\right)=1+\varphi_{b} \frac{\delta}{1-\delta}$ | 73.38 | 1.60 | 47.27 | 44.34 |
| Oliposonistic $\lambda(\mu, 0)=\mu_{i o}$ | 40.94 | -0.21 | -19.29 | -20.53 |
| Full bargain $\lambda(\mu, 1)=1+\frac{\delta}{1-\delta}$ | 75.47 | 1.62 | 51.51 | 48.38 |

> Notes: First Column presents the aggregate labor share (in percent) for the baseline and the different counterfactuals. The last three Columns changes with respect to the baseline in percentages. $\Delta Y$ is the change of aggregate output, $\Delta$ Wage is the change in aggregate wage. Aggregate wage is an employment weighted average of establishment-occupation wages. $\Delta$ Welfare $(L)$ is the change of the median expected welfare of the workers. The main counterfactual is the one without wedges $\lambda=1$. The second counterfactual Not internalize is the counterfactual where the workers' outside options are the competitive wages. Oligopsonistic is the counterfactual where the wedge is equal to the equilibrium markdown under oligopsonistic competition and Full bargain is the counterfactual where $\varphi_{b}=1$ workers earn all the profits. Counterfactuals are performed in 2007 .

Getting now to the split of output into the labor and profit shares, the aggregate labor share in the model can be constructed from industry level labor wedges $\Lambda_{b}$. Those are sufficient statistics to compute the aggregate labor share which is simply a value added weighted sum of industry labor shares. Aggregate labor share is: ${ }^{47}$

$$
L S=\sum_{b \in \mathcal{B}} \beta_{b} \Lambda_{b} \theta_{b} .
$$

Aggregate labor share is equal in all the variations of the main counterfactual without labor wedges as $\Lambda_{b}=1$, for all industries $b$.

Column (1) of Table 9 presents the aggregate labor shares of the different counterfactuals. We find that completely removing structural labor wedges increases the labor share by 21 percentage points, passing from $50.62 \%$ in the baseline to $72.26 \%$ in the counterfactual. Aggregate labor share increases slightly more in the counterfactuals where employer labor market power disappears (up to $75 \%$ where there is full bargain) and is reduced by 9 p.p. in the counterfactual with oligopsonistic competition.

Labor share changes imply changes in aggregate wages and worker welfare. Column 3 presents the relative change of wages with respect to the baseline. Wages go up by $45 \%$ in the price taking case and are

[^22]reduced by $19 \%$ when the wedge becomes $\lambda(\mu, 0)=\mu_{i o}$. Increases in the aggregate wage do not imply that wage inequality is reduced. Figure 13 in Appendix G shows that the demeaned wage distributions on the baseline and the price taking counterfactuals (in Panel (a) and (b) respectively) are very similar. This Figure highlights that even in the absence of labor wedges, wages across establishments are not equalized. This result is due to differences in productivities and amenities across establishments.

We can also analyze how the median expected welfare changes for workers. This median expected utility is: ${ }^{48}$

$$
\operatorname{Median}\left(\mathcal{U}_{i o k}\right) \propto \Phi^{\frac{1}{\eta}}
$$

Column (4) of Table 9 present counterfactual gains of the median worker utility. The median expected worker utility is $42 \%$ greater in the scenario without labor wedges compared to the baseline. Unsurprisingly, welfare gains are greater than output gains as the workers not only benefit from the productivity boost but also from the redistribution of pure rents that the owners were taking. Unsurprisingly, gains in wages are higher than gains in median welfare. Given the taste shocks, welfare gains go hand in hand with wage gains. Nevertheless, wages need to increase slightly more than welfare to induce labor reallocation.

We perform three additional counterfactuals to locate the output gains in a more realistic environment with mobility costs. They differ in restrictions imposed on mobility. First, we limit mobility to be only within industry, industry-occupation and local labor market. Table 10 compares the free mobility case with restricted mobility cases. Comparing Column (1) across the different scenarios, we find that the key margin of adjustment is geographical mobility. Fixing employment at the industry-occupation level accounts for $82 \%$ of the gains of the free mobility case. Restricting workers to stay in their particular local labor market output gains are $0.49 \%$ which constitute only $30 \%$ of the gains under free mobility.

These results underscore the importance of free mobility of labor across locations as the main driver for output gains. Figure 3 shows the percentage change of manufacturing employment in the free mobility case. Each block is a commuting zone and we aggregate all local labor markets. ${ }^{49}$ The main conclusion from the counterfactual analysis is that, in the absence of labor wedges, manufacturing employment in big cities as Paris, Lyon, Marseille or Toulouse would be reduced. The counterfactual reveals that there are a handful rural productive establishments in concentrated local labor markets. In the baseline these have lower wage markdowns and lower employment. Moving to the counterfactual, those are the ones with the biggest wage and employment gains. ${ }^{50}$

Turning now to the source of the output gains, we can use the aggregate production function and the relative industry output from Appendix A (equation (41)), and decompose the logarithm of the relative final output into three terms:

$$
\begin{equation*}
\ln \widehat{Y}=\underbrace{\sum_{b \in \mathcal{B}} \theta_{b} \ln \widehat{F}_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)}}_{\Delta \mathrm{GE}}+\underbrace{\sum_{b \in \mathcal{B}} \theta_{b} \ln \widehat{Z}_{b}}_{\Delta \text { Productivity }}+\underbrace{\sum_{b \in \mathcal{B}} \theta_{b} \ln \widehat{L}_{b}^{1-\delta}}_{\Delta \text { Labor }} \tag{29}
\end{equation*}
$$

[^23]Table 10: Counterfactuals: Limited Mobility

|  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Contribution (\%) |  |  |
| Free mobility | 1.62 | 1.33 | 9 | 83 | 8 |
| Mobility within |  |  |  |  |  |
| Industry | 1.32 | 1.33 | -1 | 101 | 0 |
| Industry-occ | 1.33 | 1.35 | -2 | 102 | 0 |
| Local market | 0.49 | 0.49 | -2 | 102 | 0 |

Notes: All the table presents results in percentages. First Column presents the $\Delta Y$ is the change of aggregate output with respect to the baseline, $\Delta$ Prod is the change in aggregate productivity from decomposition (29). Last three Columns present the contribution of each of the elements of the decomposition (29) to output gains. Free Mobility presents the main counterfactual without wedges and under free mobility of labor. Industry is the counterfactual where mobility is restricted to be only within industry, Industry-occ fixes employment at the industry-occupation and allows for mobility across locations, and Local market allows for mobility only across establishments within local labor markets. Counterfactuals are performed in 2007.

Figure 3: Employment Change (\%) with Counterfactual


Notes: The map presents employment changes with respect to the baseline economy in percentages. Each block constitutes a commuting zone. Local labor markets are aggregated up to the commuting zone. Counterfactuals are performed in 2007.

Figure 4: Productivity Change (\%) with Counterfactual


Notes: The map presents productivity changes with respect to the baseline economy in percentages. Each block constitutes a commuting zone. Local labor markets are aggregated up to the commuting zone. Commuting zone productivity is an employment weighted average of individual productivities. Following the discussion in Section 6.1, keeping fixed the baseline revenue productivities, any change in the counterfactual comes from changes in productivities.
Counterfactuals are performed in 2007.

The first term on the right hand side corresponds to the capital effects or general equilibrium effects of capital flowing to different sectors as a response to changes in relative prices. The second term, arguably the most important, represents total productivity gains. This term suffers the most from labor market concentration as big productive firms are shrinking their relative participation, therefore reducing overall productivity. The third term corresponds to how labor is allocated across sectors.

Columns (3) to (5) of Table 10 show the relative changes of output with respect to these three terms. ${ }^{51}$ The main source of output gains come from productivity. Industry productivity is an employment weighted sum of establishment-occupation productivities (that are unchanged). The original source of productivity and output gains is the reallocation of workers towards productive firms.

Column (2) shows the productivity gains in the different mobility cases. Those are similar as long as labor is mobile at the industry level. General equilibrium effects determine the reallocation of employment across industries and total output gains. Mobility restrictions below the industry level prevent the reallocation towards productive establishments and reduce the productivity gains.

Figure 4 shows geographical differences of productivity gains in the free mobility case. The Figure is similar to Figure 3 in the sense that most significant gains of the counterfactual productivity happen outside urban areas. The largest gains in terms of productivity, wages and employment are in commuting zones without big cities.

[^24]
### 6.3 Pass Through

The structural wage equation (28) relates our recovered measure of productivity $Z_{i o}$ to equilibrium wages. Taking logs, equilibrium wage in the baseline economy is:

$$
\begin{equation*}
\log w_{i o}=\frac{1}{1+\varepsilon_{b} \delta}\left(\log Z_{i o}-\delta \log T_{i o}+\log \lambda\left(\mu_{i o}, \varphi_{b}\right)\right)+f_{m} \tag{30}
\end{equation*}
$$

where $f_{m}$ is a fixed effect at the local labor market level. We use this equation to study the incidence of labor market power on the pass through of the transformed revenue productivity $Z$. The elasticity of wages with respect to $Z$ is:

$$
\epsilon_{Z}^{W}=\frac{\partial \log w_{i o}}{\partial \log Z_{i o}}=\underbrace{\frac{1}{1+\varepsilon_{b} \delta}}_{\text {Pass Through No Wedge }}+\frac{1}{1+\varepsilon_{b} \delta} \underbrace{\epsilon_{s}^{\lambda}}_{<0} \underbrace{\epsilon_{Z}^{s}}_{>0},
$$

where $\epsilon_{s}^{\lambda}$ and $\epsilon_{Z}^{s}$ denote respectively the elasticity of the wedge $\lambda_{i o}$ with respect to the employment share $s$ and the elasticity of the employment share $s$ with respect to our measure of productivity Z . The equation above emphasizes the origin of potential distortions coming from labor market power. When the wedge is constant, the last term becomes zero because $\epsilon_{s}^{\lambda}=0$. In that case, the pass through of productivity to wages is the same as in the price taking case and the labor allocations are not distorted.

We estimate the following:

$$
\log w_{i o t}=f_{m o t}+\beta_{b}^{Z} \log Z_{i o t}+\beta_{b}^{T} \log T_{i o t}+u_{i o t}
$$

Table 18 in Appendix I presents the estimates of the productivity pass through in the baseline $\beta_{b}^{Z}$ and the one in the absence of labor wedges. The average dampening due to labor market power is equal to 0.05 . This means that when Z increases by $1 \%, 0.05 \%$ of that increase is not translated to wages due to labor market frictions.

### 6.4 Mobility and Wage Gap

Figure 3 suggests an important movement from cities to rural areas in the counterfactual. This section explores the impact of employer and union labor market power on the de-industrialization process and the urban-rural wage gap.

## Mobility over time

Movements in Figure 3 suggest employment reallocation from cities to rural areas in the manufacturing sector. Here we compare the de-industrialization process observed in the data and the one from the counterfactuals.

In the data, de-industrialization or the reduction of manufacturing employment occurred primarily in cities. Figure 5 compares the de-industrialization process observed in the data to the one we would have in the counterfactuals.

First, we compute the commuting zone employment share out of total manufacturing for the initial and final years (1994 and 2007 respectively) and for the different scenarios. Then, we compute the differences in the data ( $\Delta^{D}=S_{07}^{D}-S_{94}^{D}$ ) and in the counterfactual $\left(\Delta^{M}=S_{07}^{P T}-S_{94}^{P T}\right)$. Figure 5 presents this comparison. The $x$ axis shows $\Delta^{D}$ and the $y$ axis shows $\Delta^{M}$. The size of the dots are the initial population. The counterfactual de-industrialization process is very similar to the process observed in the data. Over time, de-industrialization is mostly guided by exogenous productivity and firm location decisions and not by labor market distortions.

Figure 5: De-industrialization differences


Notes: The x -axis shows the percentage differences of employment shares over time in the data ( $\Delta^{D}=S_{07}^{D}-S_{94}^{D}$ ). The y -axis presents the analogous for the counterfactual without wedges $\left(\Delta^{M}=S_{07}^{P T}-S_{94}^{P T}\right)$. The initial period is 1994 and the final year is 2007.

The line generated by the largest population commuting zones is slightly flatter than the 45 degree line. The de-industrialization would have been a bit slower in the counterfactual. This is mostly explained by the closure of manufacturing firms in the largest cities that became more concentrated over time.

## Wage Gap

Table 11 presents urban and rural wages besides the urban/rural wage gap. ${ }^{52}$ Both experience important wage gains in the counterfactual. Gains are bigger outside cities, which reduces the wage gap from $36 \%$ to $23 \%$. This reveals that labor market distortions account for more than a third of the urban/rural wage gap.

Table 11: Wage Gap

|  |  |  |  |
| :--- | :---: | :---: | :---: |
|  | Rural Wage | Urban Wage | Gap (\%) |
| Baseline | 33.321 | 45.210 | 36 |
| Counterfactual | 49.486 | 60.675 | 23 |

Note: Wages in thousands of constant 2015 euros. We classify as Urban the 10 biggest commuting zones: Paris, Marseille, Lyon, Toulouse, Nantes, and the Paris surrounding, Boulogne-Billancourt, Creteil, Montreuil, Saint-Denis and Argenteuil. The rest are considered as Rural. Wages are employment weighted averages per category for the baseline and counterfactual for the year 2007.

[^25]
## 7 Extensions

Total labor supply was fixed in the baseline counterfactual, workers were perfectly mobile and there were no agglomeration externalities. In this section, we propose two extensions. First, we allow for an endogenous labor participation. Second, we introduce agglomeration forces in the local labor markets.

### 7.1 Endogenous Participation

We briefly present an extension where we allow for endogenous labor force participation decisions. We assume workers can decide between working and staying at home. In the latter case, they earn some wages related to home production. In the model, staying at home is an endogenous choice that happens when the indirect utility of being out of the labor force is higher than the one being employed.

We lack detailed data on the geographical distribution of out of the labor force status. Labor force surveys provide only information at the region level. Basing our counterfactuals in those surveys would require the extreme assumption of constant rates of labor participation for entire regions. Instead, while acknowledging is not a perfect assumption, we use commuting zone level unemployment rates as out-of-the labor-force rates.

Defining out-of-the-labor-force, from now on OTLF, as a new sub-industry at every location, 2-digit industry and occupation combination, we have that the probability of being OTLF in a particular commuting zone $n$ and 2-digit industry $b$ is:

$$
L_{u o}=\frac{\left(T_{u o} w_{u o}^{\varepsilon_{b}}\right)^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi} L, \quad \Phi=\Phi_{e}+\Phi_{u}
$$

where $\Phi_{e}=\sum_{m \in \mathcal{I}_{m}} \Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}$ is the part of $\Phi$ that comes from the employed and $\Phi_{u}=\sum_{u o \in \mathcal{U}_{m}}\left(T_{u o} w_{u o}^{\varepsilon_{b}}\right)^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}$ is the part from the unemployed ( $\mathcal{U}_{m}$ is the set of all OTLF local labor markets). $L$ is the total labor supply of the both employed and OTLF workers. The proportion of OTLF workers in each local market identifies the home production wage $T_{u o} w_{u 0}^{\varepsilon_{b}}{ }^{53}$ This wage is fixed in the counterfactuals while the real wages of firms change depending on the counterfactual wedges.

Table 12 shows the results of the counterfactuals with endogenous labor force participation. The counterfactual output gain is $1.98 \%$. Introducing the endogenous labor participation margin induces higher output gains than in the baseline (Fixed L). In contrast with the results shown in Table 10, around $30 \%$ of the gains come from the increased total employment. Labor force increases $1 \%$ in the main counterfactual without wedges. This extensive margin adjustment in the total labor supply amplifies original differences in output gains across counterfactuals. In particular, output losses from oligopsonistic competition are as high as 1.29\% because total labor force participation is reduced ( $-0.75 \%$ ).

### 7.2 Agglomeration

In this section we present an extension of the model that includes agglomeration forces at the local labor market level. To keep the model tractable, we assume that the productivity is: $\widehat{A}_{i o}=\widetilde{A}_{i o} L_{m}^{\gamma\left(1-\alpha_{b}\right)}$. The agglomeration effect is a local labor market externality with elasticity $\gamma\left(1-\alpha_{b}\right)$. The wage first order condition is:

$$
\begin{equation*}
P w_{i o}=\beta_{b} \lambda\left(\mu_{i o}, \varphi_{b}\right) Z_{i o} L_{i o}^{-\delta} L_{m}^{\gamma} \tag{31}
\end{equation*}
$$

[^26]Table 12: Counterfactual: Endogenous Participation

|  | $\Delta Y(\%)$ | $\Delta \operatorname{Prod}(\%)$ | $\Delta \mathrm{L}(\%)$ | Contribution (\%) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Sh. GE | Sh. Prod | Sh. Labor |
| Fixed L | 1.62 | 1.33 | 0.00 | 9 | 83 | 8 |
| Endogenous Part. |  |  |  |  |  |  |
| No wedges $\lambda\left(\mu, \varphi_{b}\right)=1$ | 1.98 | 1.18 | 1.00 | 11 | 60 | 29 |
| Not internalize $\lambda\left(1, \varphi_{b}\right)=1+\varphi_{b} \frac{\delta}{1-\delta}$ | 2.04 | 1.18 | 1.04 | 10 | 58 | 32 |
| Oligopsonistic $\lambda(\mu, 0)=\mu(s)$ | -1.29 | -0.59 | -0.75 | 2 | 46 | 53 |
| Full bargain $\lambda(\mu, 1)=1+\frac{\delta}{1-\delta}$ | 2.09 | 1.18 | 1.12 | 10 | 57 | 33 |

Notes: All the table presents results in percentages. First Column $\Delta Y$ is the change of aggregate output with respect to the baseline, $\Delta$ Prod is the change in aggregate productivity from decomposition (29) and $\Delta L$ is the counterfactual change in total employment. Last three Columns present the contribution of each of the elements of the decomposition (29) to output gains. Fixed $L$ is the main counterfactual without wedges, under free mobility of labor and fixed total labor supply. The main counterfactual is the one without wedges $\lambda=1$. All the other counterfactuals in this table allow for endogenous labor force participation. No wedges is the analogous to the main counterfactual without wedges. Not internalize is the counterfactual where the workers' outside options are the competitive wages. Oligopsonistic is the counterfactual where the wedge is equal to the equilibrium markdown under oligopsonistic competition and Full bargain is the counterfactual where $\varphi_{b}=1$ workers earn all the profits.

Similarly to the baseline counterfactual, we back out the fundamental $Z_{i o}$ to perfectly match observed establishment-occupation wages $w_{i 0}$. In the case where employment for a given local labor market is high, the productivity of the establishments in that market $m$ is lower than for the main counterfactual. ${ }^{54}$

[^27]Table 13: Counterfactuals: Agglomeration

|  |  |  | Contribution (\%) |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | $\Delta Y(\%)$ | $\Delta$ Prod (\%) | Sh. GE | Sh. Prod | Sh. Labor |
| No Agglomeration | 1.62 | 1.33 | 9 | 83 | 8 |
| Agglomeration |  |  |  |  |  |
| $\gamma=0.05$ | 1.73 | 1.40 | 8 | 82 | 10 |
| $\gamma=0.1$ | 1.84 | 1.48 | 7 | 81 | 12 |
| $\gamma=0.15$ | 1.96 | 1.57 | 6 | 81 | 13 |
| $\gamma=0.2$ | 2.08 | 1.66 | 5 | 80 | 15 |
| $\gamma=0.25$ | 2.22 | 1.75 | 3 | 80 | 17 |

Notes: All the table presents results in percentages. First Column $\Delta Y$ is the change of aggregate output with respect to the baseline, $\Delta$ Prod is the change in aggregate productivity from decomposition (29). Last three Columns present the contribution of each of the elements of the decomposition (29) to output gains. No Agglomeration is the main counterfactual without wedges, under free mobility of labor, fixed total labor supply and no agglomeration forces. All the other counterfactuals in this table allow for agglomeration within the local labor market. Similarly to the main counterfactual, workers are freely mobile and total employment is fixed. We present different counterfactuals depending on the agglomeration elasticity $\gamma$.

Table 13 summarizes the counterfactual results for different values of $\gamma$. All the counterfactuals in Table 13 also assume price taking and free mobility but introduce agglomeration forces in local labor markets. As $\gamma$ becomes higher, the more important are the agglomeration forces and the higher are the efficiency gains. The reason behind this result is that increasing $\gamma$ the local labor market employment $L_{m}$ becomes more important in (31)- Consequently, productivity differences across local labor markets with different employment are amplified. The movements towards small local labor markets are therefore bigger than in the main counterfactual. Output gains are monotonic in the importance of agglomeration externalities.

## 8 Conclusion

This paper measures efficiency and welfare losses generated by employer and union labor market power for French manufacturing establishments. We present stylized facts at the aggregate level that show higher employment concentration relates to lower labor shares for French manufacturing firms. We further document the relevance of heterogeneous labor market power at the establishment level. Our empirical strategy identifies a negative relationship between local labor market employment share and wages. This reduced form evidence suggests employer labor market power is relevant and heterogeneous across markets and firms.

We lay out a quantitative general equilibrium model that links structural labor wedges to employment shares and union's bargaining power. Our framework nests the cases with bargaining only and oligopsonistic competition only as special cases. We show existence and uniqueness of the equilibrium and provide its analytical characterization. We estimate parameters by exploiting the structural equations and the micro-
data.
Finally, we evaluate the efficiency and welfare costs of employer and union labor market power. We find that removing structural labor wedges would increase output by $1.6 \%$. Gains are slightly bigger, up to $1.98 \%$ when we allow for an endogenous labor force participation margin. The main mechanism behind the output gains is the reallocation of resources towards more productive firms.

Removing labor market distortions lead to significant labor share and wage gains. Those results imply that the markdown is more important on the labor wedge and in turn highlight the importance of employer labor market power in France. The potential insights for policy are clear. The framework suggests that the allocation without labor market distortions can be implemented by hiring subsidies that would eliminate the effect of the labor wedge. Those subsidies could be financed either by taxes on profits or on wage earnings.

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## A Derivations

In this section we provide the derivations of the model that are not presented in the main text. First, we show how to obtain the establishments labor supplies by solving the workers establishment choice problem. Later, we show how we obtain the markdown function from the establishments optimality conditions. We then show how to get a close form solution for the prices given the solution for the normalized wages.

## A. 1 Establishment-Occupation Labor Supply

To simplify the notation, we get rid of the occupation subscript $o$ in this subsection. The indirect utility of a worker $k$ that is employed in establishment $i$ in sub-market $m$ is:

$$
u_{k i m}=w_{i} z_{i \mid m}^{1} z_{m}^{2}
$$

where $z_{i \mid m}^{1}$ and $z_{m}^{2}$ are independent utility shocks. They are both distributed Frèchet with shape and scale parameters $\varepsilon_{b}$ and $T_{i}$ for $z_{i \mid m^{\prime}}^{1}$ and $\eta$ and 1 for $z_{m}^{2}$.

Workers first see the realizations of the shocks $z_{m}^{2}$ for all local labor markets. After choosing to which labor market to go, the workers then observe the establishment specific shocks. Therefore, there is a two stage decision: first, the worker choose the local labor market that maximizes her expected utility, and later will choose the establishment that maximizes her utility conditional on the chosen sub-market.

The goal is to compute the unconditional probability of a worker going to establishment $i$ in sub-market $m$. This probability is equal to:

$$
\Pi_{i}=P\left(w_{i} z_{i \mid m}^{1} \geq \max _{i^{\prime} \neq i} w_{i^{\prime}} z_{i^{\prime} \mid m}^{1}\right) P\left(\mathbb{E}_{m}\left(\max _{i} w_{i} z_{i \mid m}^{1}\right) z_{m}^{2} \geq \max _{m^{\prime} \neq m} \mathbb{E}_{m^{\prime}}\left(\max _{i} w_{i} z_{i \mid m^{\prime}}^{1} z_{m^{\prime}}^{2}\right)\right.
$$

We first solve for the left term. Let's define the following distribution function:

$$
G_{i}(v)=P\left(w_{i} z_{i \mid m}^{1}<v\right)=P\left(z_{i \mid m}^{1}<v / w_{i}\right)=e^{-T_{i} w_{i}^{\varepsilon_{b}} v^{-\varepsilon_{b}}} .
$$

To ease notation, define conditional utility $v_{i}=w_{i} z_{i \mid m}^{1}$ for all $i, i^{\prime}$. We need to solve for $P\left(v_{i} \geq \max _{i^{\prime} \neq i} v_{i^{\prime}}\right)$. Fix $v_{i}=v$. Then we have:

$$
P\left(v \geq \max _{i^{\prime} \neq i} v_{i^{\prime}}\right)=\bigcap_{i^{\prime} \neq i} P\left(v_{j}<v\right)=\prod_{i^{\prime} \neq i} G_{i^{\prime}}(v)=e^{-\Phi_{m}^{-i} v^{-\varepsilon_{b}}}=G_{m}^{-i}(v)
$$

where $\Phi_{m}^{-i}=\sum_{i^{\prime} \neq i} T_{i^{\prime}} w_{i^{\prime}}^{\varepsilon_{b}}$. Similarly, the probability of having at most conditional utility $v$ is equal to

$$
G_{m}(v)=P\left(v \geq \max _{i^{\prime}} v_{i^{\prime}}\right)=e^{-\Phi_{m} v^{-\varepsilon_{b}}}
$$

where $\Phi_{m}=\sum_{i^{\prime}} T_{i^{\prime}} w_{i^{\prime}}^{\varepsilon_{b}}$. Integrating $G_{m}^{-i}(v)$ over all possible values of $v$ we then get:

$$
\begin{aligned}
P\left(v_{i} \geq \max _{i^{\prime} \neq i} v_{i^{\prime}}\right) & =\int_{0}^{\infty} e^{-\Phi_{m}^{-i} v^{-\varepsilon_{b}}} d G_{i}(v) \\
& =\int_{0}^{\infty} \varepsilon_{b} T_{i} w_{i}^{\varepsilon_{b}} v^{\varepsilon_{b}-1} e^{-\Phi_{m} v^{-\varepsilon_{b}}} d v \\
& =\frac{T_{i} w_{i}^{\varepsilon_{b}}}{\Phi_{m}} \int_{0}^{\infty} \varepsilon_{b} \Phi_{m} v^{\varepsilon_{b}-1} e^{-\Phi_{m} v^{-\varepsilon_{b}}} d v \\
& =\frac{T_{i} w_{i}^{\varepsilon_{b}}}{\Phi_{m}} \int_{0}^{\infty} d G_{m}(v)=\frac{T_{i} w_{i}^{\varepsilon_{b}}}{\Phi_{m}}
\end{aligned}
$$

Now we need to find $P\left(\mathbb{E}_{m}\left(\max _{i} w_{i} z_{i \mid m}^{1}\right) z_{m}^{2} \geq \max _{m^{\prime} \neq m} \mathbb{E}_{m^{\prime}}\left(\max _{i} w_{i} z_{i \mid m^{\prime}}^{1}\right) z_{m^{\prime}}^{2}\right)$. So first, the expected utility of working in sub-market $m$ is:

$$
\mathbb{E}_{m}\left(\max _{i} w_{i} z_{i \mid m}^{1}\right)=\int_{0}^{\infty} v_{i} d G_{m}(v)=\int_{0}^{\infty} \varepsilon_{b} \Phi_{m} v^{-\varepsilon_{b}} e^{-\Phi_{m} v^{-\varepsilon_{b}}} d v
$$

We define this new variable:

$$
x=\Phi_{m} v^{-\varepsilon_{b}} \quad d x=-\varepsilon_{b} \Phi_{m} v^{-\left(\varepsilon_{b}+1\right)} d v
$$

Now we can change variable in the previous integral and obtain:

$$
\int_{0}^{\infty} x^{-1 / \varepsilon_{b}} \Phi_{m}^{1 / \varepsilon_{b}} e^{-x} d x=\Gamma\left(\frac{\varepsilon_{b}-1}{\varepsilon_{b}}\right) \Phi_{m}^{1 / \varepsilon_{b}}
$$

where $\Gamma\left(\dot{)}\right.$ is just the Gamma function. Defining $\Gamma_{b} \equiv \Gamma\left(\frac{\varepsilon_{b}-1}{\varepsilon_{b}}\right)$, we can then rewrite:

$$
P\left(\mathbb{E}_{m}\left(\max _{i} w_{i} z_{i \mid m}^{1}\right) z_{m}^{2} \geq \max _{m^{\prime} \neq m} \mathbb{E}_{m^{\prime}}\left(\max _{i} w_{i} z_{i \mid m^{\prime}}^{1}\right) z_{m^{\prime}}^{2}\right)=P\left(\Phi_{m}^{1 / \varepsilon_{b}} \Gamma_{b} z_{m}^{2} \geq \max _{m^{\prime} \neq m} \Phi_{m^{\prime}}^{1 / \varepsilon_{b^{\prime}}} \Gamma_{b^{\prime}} z_{m^{\prime}}^{2}\right)
$$

Following the similar arguments as above, this probability is equal to:

$$
P\left(\Phi_{m}^{1 / \varepsilon_{b}} \Gamma_{b} z_{m}^{2} \geq \max _{m^{\prime} \neq m} \Phi_{m^{\prime}}^{1 / \varepsilon_{b}} \Gamma_{b^{\prime}} z_{m^{\prime}}^{2}\right)=\frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi}
$$

where $\Phi=\sum_{b^{\prime} \in \mathcal{B}} \sum_{m^{\prime} \in \mathcal{M}_{b^{\prime}}} \Phi_{m^{\prime}}^{\eta / \varepsilon_{b^{\prime}}} \Gamma_{b^{\prime}}^{\eta}$.
Finally, combining the two probabilities we obtain the same expression in the main text:

$$
\Pi_{i}=\frac{T_{i} w_{i}^{\varepsilon_{b}}}{\Phi_{m}} \frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi}
$$

By integrating $\Pi_{i}$ over the whole measure of workers $L$, we can obtain the labor supply for each establishment:

$$
L_{i}=\frac{T_{i} w_{i}^{\varepsilon_{b}}}{\Phi_{m}} \frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi} L
$$

Workers' welfare. An obvious way to measure workers welfare would be to compute the average utility for workers. However this is not possible as the shape parameter $\eta$ is smaller than 1 . This implies that the mean for the Frechét distributed utilities is not defined. Instead, we compute the median utility agents expect to receive in each local labor market. This is equal to:

$$
\text { Median }\left[\max _{m} \mathbb{E}_{m}\left(\max _{i} w_{i} z_{i \mid m}^{1}\right) z_{m}^{2}\right] \propto \Phi^{\frac{1}{\eta}}
$$

## A. 2 Establishment Decision

In the absence of bargaining, the profit maximization problem of establishment $i$ is:

$$
\max _{w_{i o t}, K_{i o t}} P_{b t} \sum_{o=1}^{O} \widetilde{A}_{i o t} K_{i o t}^{\alpha_{b}} L_{i o t}^{\beta_{b}}-\sum_{o=1}^{O} w_{i o t} L_{i o t}\left(w_{i o t}\right)-R_{b t} \sum_{o=1}^{O} K_{i o t},
$$

where $L_{i o t}\left(w_{i o t}\right)$ is the labor supply (13) where they take $\Phi$ and $L$ as given but internalize their effect on $\Phi_{i o}$ and $\Phi_{m} . P_{b t}$ and $R_{b t}$ are respectively the industry price and required rate. ${ }^{55}$ Getting rid of the time index $t$, the first order conditions of this problem are:

$$
\begin{align*}
w_{i o} & =\beta_{b} \frac{e_{i o}}{e_{i o}+1} P_{b} \widetilde{A}_{i o} K_{i o}^{\alpha_{b}} L_{i o}^{\beta_{b}-1} \\
R_{b} & =\alpha_{b} P_{b} \widetilde{A}_{i o} K_{i o}^{\alpha_{b}-1} L_{i o}^{\beta_{b}} \tag{32}
\end{align*}
$$

[^28]$e_{i o}=\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}$ is the perceived elasticity of supply for establishment $i$ in occupation $o$.
We can use the first order conditions of capital to substitute it into the establishment's production function and obtain an expression that depends only in labor:
\[

$$
\begin{equation*}
y_{i o}=\left(\frac{\alpha_{b}}{R_{b}}\right)^{\frac{\alpha_{b}}{1-\alpha_{b}}} \widetilde{A}_{i o}^{\frac{1}{1-\alpha_{b}}} L_{i o}^{\frac{\beta_{b}}{1-\alpha_{b}}} P_{b}^{\frac{\alpha_{b}}{1-\alpha_{b}}} \tag{33}
\end{equation*}
$$

\]

In order to gain tractability in the solution of the model we restrict the output elasticity with respect to capital such that $1-\frac{\beta_{b}}{1-\alpha_{b}}=\delta$, where $\delta \in[0,1]$ is a constant across sectors. This specification would nest a constant returns to scale technology when $\delta=0$. As long as $0<\delta<1$ the establishment faces decreasing returns to scale within occupations. Define a transformed productivity $A_{i o} \equiv \widetilde{A}_{i o}^{\frac{1}{1-\alpha_{b}}}\left(\frac{\alpha_{b}}{R_{b}}\right)^{\frac{\alpha_{b}}{1-\alpha_{b}}}$. The establishment-occupation production is:

$$
\begin{equation*}
y_{i o}=P_{b}^{\frac{\alpha_{b}}{1-\alpha_{b}}} A_{i o} L_{i o}^{1-\delta} \tag{34}
\end{equation*}
$$

## A. 3 Markdown function

We derive the markdown function from the establishments optimality condition with respect to wages. The establishment post a wage and choose capital quantity in order to maximize profits subject to their individual labor supply. Establishments only take into account the effect on their local labor market. As explained in the main text, this can happen because of a myopic behavior from the establishments or if there is a continuum of local labor markets. The establishment problem is:

$$
\max _{w_{i o}, K_{i o}} P_{b} \sum_{o=1}^{O} \widetilde{A}_{i o} K_{i o}^{\alpha_{b}} L_{i o}^{\beta_{b}}-\sum_{o=1}^{O} w_{i o} L_{i o}\left(w_{i o}\right)-R_{b} \sum_{o=1}^{O} K_{i o}
$$

The first order condition with respect to labor is:

$$
P_{b} \frac{\partial F}{\partial L_{i o}} \frac{\partial L_{i o}}{\partial w_{i o}}=L_{i o}\left(w_{i o}\right)+w_{i o} \frac{\partial L_{i o}}{\partial w_{i o}}
$$

where the derivative of the labor supply $L_{i o}$ with respect to the establishment-occupation wage $w_{i o}$ is:

$$
\begin{aligned}
\frac{\partial L_{i o}}{\partial w_{i o}} & =\frac{L \Gamma_{b}^{\eta}}{\Phi}\left(\left[\frac{\varepsilon_{b} T_{i o} w_{i o}^{\varepsilon_{b}-1} \Phi_{m}-T_{i o} w_{i o}^{\varepsilon_{b}} \varepsilon_{b} T_{i o} w_{i o}^{\varepsilon_{b}-1}}{\Phi_{m}^{2}}\right] \Phi_{m}^{\eta / \varepsilon_{b}}+\eta \frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\Phi_{m}} \Phi_{m}^{\eta / \varepsilon_{b}-1} T_{i o} w_{i o}^{\varepsilon_{b}-1}\right) \\
& =\frac{\varepsilon_{b} T_{i o} w_{i o}^{\varepsilon_{b}-1}}{\Phi_{m}} \frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi} L-\frac{\varepsilon_{b} T_{i o} w_{i o}^{\varepsilon_{b}-1} \Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi_{m} \Phi} L \frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\Phi_{m}}+\eta \frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\Phi_{m}} \frac{T_{i o} w_{i o}^{\varepsilon_{b}-1}}{\Phi_{m}} \frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi} L \\
& =\varepsilon_{b} \frac{L_{i o}}{w_{i o}}-\varepsilon_{b} \frac{L_{i o}}{w_{i o}} \frac{L_{i o}}{L_{m}}+\eta \frac{L_{i o}}{w_{i o}} \frac{L_{i o}}{L_{m}} \\
& =\frac{L_{i o}}{w_{i o}}\left(\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}\right) .
\end{aligned}
$$

Substituting this last derivative into the first order condition we get:

$$
\begin{aligned}
& L_{i o}+L_{i o}\left(\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}\right)=P_{b} \frac{\partial F}{\partial L_{i o}} \frac{L_{i o}}{w_{i o}}\left(\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}\right) \\
& \Rightarrow \quad w_{i o}=\frac{\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}}{\varepsilon_{b}\left(1-s_{i o \mid m}\right)+\eta s_{i o \mid m}+1} P_{b} \frac{\partial F}{\partial L_{i o}} \\
& \quad w_{i o}=\mu\left(s_{i o \mid m}\right) P_{b} \frac{\partial F}{\partial L_{i o}} .
\end{aligned}
$$

## A. 4 Bargaining Details

Workers of each occupation bargain with the establishment that retains the right-to-manage. Each establishment has different occupation profit functions $\left(1-\alpha_{b}\right) p F\left(L_{i o}\right)-w_{i o}^{u} L_{i o}$, where the optimal capital decision has been taken. In what follows we abstract from the occupation index $o$ for clarity. The threat point for workers is the wage they would obtain under oligopsonistic competition, $w_{i o}^{M P}$, that we take as an status-quo scenario, where the threat point of firms is zero profits. The bargaining solution chooses wages to maximize:

$$
\max _{w_{i o}^{u}}\left(w_{i o}^{u} L_{i o}-w_{i o}^{M P} L_{i o}\right)^{\varphi_{b}}\left(\left(1-\alpha_{b}\right) p F\left(L_{i o}\right)-w_{i o}^{u} L_{i o}\right)^{1-\varphi_{b}}
$$

with $\varphi_{b}$ being the union's bargaining power, $w_{i 0}^{u}$ the wage bargained with the unions at establishmentoccupation $i o, L_{i o}$ the number of workers employed at establishment-occupation io in equilibrium, $w_{i o}^{M P}$ is the threat wage of workers, $\left(1-\alpha_{b}\right) F\left(L_{i o}\right)$ is the output of the establishment-occupation after substituting for the optimal decision of capital. To ease exposition, in what follows we get rid of the establishment-occupation subscript $i o$. The first order conditions of the above maximization problem are:

$$
\varphi_{b}\left(\left(1-\alpha_{b}\right) p F(L)-w^{u} L\right)=\left(1-\varphi_{b}\right)\left(w^{M P} L-w^{u} L\right)
$$

Rearranging the first order condition:

$$
w^{u}=w^{M P}+\frac{\varphi_{b}}{1-\varphi_{b}} \frac{\left(\left(1-\alpha_{b}\right) p F(L)-w^{u} L\right)}{L} .
$$

This is the standard expression on bargaining models, where workers earn a fraction $\frac{\varphi_{b}}{1-\varphi_{b}}$ of the quasirents of the establishment on excess of their reservation wage. Solving for $w^{u}$ and substituting $w^{M P}=$ $\mu(s) \times M R P L=\frac{e}{e+1} \times M R P L$ yields:

$$
w^{u}=\left(1-\varphi_{b}\right) \frac{e}{e+1}\left(1-\alpha_{b}\right) p \frac{\partial F(L)}{\partial L}+\varphi_{b} \frac{\left(1-\alpha_{b}\right) p F(L)}{L} .
$$

In the case of a Cobb-Douglas production function, the marginal revenue product of labor is proportional to the labor productivity, i.e. $\left(1-\alpha_{b}\right) p \frac{\partial F(L)}{\partial L}=\beta_{b} \frac{p F(L)}{L}$, where $\beta_{b}$ is the elasticity of output with respect to labor. By the definition of $\delta, \beta_{b} /\left(1-\alpha_{b}\right)=(1-\delta)$, the bargained wage becomes:

$$
w^{u}=\underbrace{\left(1-\alpha_{b}\right) p \frac{\partial F(L)}{\partial L}}_{M R P L}\left[\left(1-\varphi_{b}\right) \frac{e}{e+1}+\varphi_{b} \frac{1}{1-\delta}\right]
$$

where we recovered the expression from the main text.

## A. 5 Aggregate Model

Given the equilibrium definition, the model contains a very large number of variables that could make it unfeasible to be solved numerically. This is because each firm in every location and industry sets its own wage. So if in every sector location pair there would be $H$ sub-industries, and each sub-industry would have $I$ firms, there would be $N \times B \times H \times I$ wages to be solved in the model plus $B+1$ equations for the prices and final output. In comparison, quantitative spatial economic models that assume implicitly that all firms in the same location have the same amenity would only need to solve for $N$ different wages. In this section we show how the fact that firms only take into account the effect of their wage decision on the local labor market helps to tackle this problem by separating it in two main parts. First, we show that we can solve
for each sub-market wages by normalizing the sectoral prices and an economy wide constant. Later, we use this normalized wages to construct aggregate expressions that are just functions of sectoral prices and some economy wide constants. Finally, we provide a closed form solution of these prices and the final output conditional on having the solution for the normalized wages.

Following this path allows us to solve the model in a feasible way. Instead of solving a system of ( $N \times$ $B \times H \times I)+(B+1)$ equations, we can solve $N \times B \times H$ smaller and simpler systems of $I$ equations each and later a system of $B+1$ equations.

Starting from the expression of wages (17),

$$
w_{i o}=\widetilde{w}_{i o} \Phi_{m}^{\left(1-\eta / \varepsilon_{b}\right) v_{b}}\left(\frac{\Phi}{L}\right)^{v_{b}} F_{b}
$$

we can use the definition of $\Phi_{m}=\sum_{i o \in I_{m}} T_{i o} w_{i o}^{\varepsilon_{b}}$ to find,

$$
\begin{equation*}
\Phi_{m}=\widetilde{\Phi}_{m}^{\psi_{b}} F_{b}^{\varepsilon_{b} \psi_{b}}\left(\frac{\Phi}{L}\right)^{\psi_{b} v_{b} \varepsilon_{b}}, \quad \widetilde{\Phi}_{m}=\sum_{i \in I_{m} 0} T_{i o} \widetilde{w}_{i o}^{\varepsilon_{b}}, \quad \psi_{b} \equiv \frac{1+\varepsilon_{b} \delta}{1+\eta \delta} \geq 1 \tag{35}
\end{equation*}
$$

Plugging the expression of $\Phi_{m}$ into the one above, and noticing that $\psi_{b} v_{b}=\delta /(1+\eta \delta)$ we can rewrite the equilibrium wage as,

$$
\begin{equation*}
w_{i o}=\widetilde{w}_{i o} \widetilde{\Phi}_{m}^{\frac{\psi_{b}-1}{\varepsilon_{b}}} F_{b}^{\psi_{b}}\left(\frac{\Phi}{L}\right)^{\frac{\delta}{1+\eta \delta}} . \tag{36}
\end{equation*}
$$

The establishment-occupation labor supply $L_{i o}$ can be written as $L_{i o}=s_{i o \mid m} s_{m \mid b} L_{b}$. Given the solution of normalized wages per sub-market $\widetilde{w}_{i o}$, we can actually compute the employment share out of the local labor market $s_{i o \mid m}$ :

$$
s_{i o \mid m}=\frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\Phi_{m}}=\frac{T_{i o} \widetilde{w}_{i o}^{\varepsilon_{b}}}{\widetilde{\Phi}_{m}}, \quad \widetilde{\Phi}_{m}=\sum_{i \in \mathcal{I}_{m}} T_{i o} \widetilde{w}_{i o}^{\varepsilon_{b}}
$$

We can also compute the employment share of the local labor market out of the industry $s_{m \mid b}$. Using the definition of $\Phi_{b}=\sum_{m \in \mathcal{M}_{b}} \Phi_{m}^{\eta / \varepsilon_{b}}$ and (35),

$$
s_{m \mid b}=\frac{\Phi_{m}^{\eta / \varepsilon_{b}}}{\Phi_{b}}=\frac{\widetilde{\Phi}_{m}^{\psi_{b} \eta / \varepsilon_{b}}}{\widetilde{\Phi}_{b}}, \quad \widetilde{\Phi}_{b}=\sum_{m \in \mathcal{M}_{b}} \widetilde{\Phi}_{m}^{\psi_{b} \eta / \varepsilon_{b}}
$$

where $\mathcal{M}_{b}$ is the set of all local labor markets that belong to industry $b$. This just formalizes the notion that, as long as we know the relative wages within an industry, we can compute the measure of workers that go to each establishment conditioning on industry employment.

Turning now to output, we can compute output at the industry level by aggregating establishmentoccupation ones according to (5):

$$
\begin{equation*}
Y_{b}=F_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)} A_{b} L_{b}^{1-\delta}, \quad A_{b}=\sum_{m \in \mathcal{M}_{b}} \sum_{i o \in \mathcal{I}} A_{i o} s_{i o \mid m}^{1-\delta} s_{m \mid b}^{1-\delta}, \tag{37}
\end{equation*}
$$

where we obtained an expression that represents the productivity at the industry level $A_{b}$. As it is evident from the definition, $A_{b}$ is an employment weighted industry productivity. The covariance between those two is key in order to determine industry productivity. As long as market power distorts the employment distribution making more productive firms to constraint their size, the covariance between productivity and employment is lower than in the case with competitive labor markets. This decreases total industry productivity $A_{b}$.

Using (35), industry labor supply can be written as function of normalized (tilde) variables and transformed prices:

$$
\begin{equation*}
L_{b}=\frac{\Phi_{b} \Gamma_{b}^{\eta}}{\sum_{b^{\prime} \in \mathcal{B}} \Phi_{b^{\prime}} \Gamma_{b^{\prime}}^{\eta}} L=\frac{F_{b}^{\psi_{b} \eta} \widetilde{\Phi}_{b} \Gamma_{b}^{\eta}}{\widetilde{\Phi}} L, \quad \widetilde{\Phi}=\sum_{b^{\prime} \in \mathcal{B}} F_{b^{\prime}}^{\psi_{b} \eta} \widetilde{\Phi}_{b^{\prime}} \Gamma_{b^{\prime}}^{\eta} . \tag{38}
\end{equation*}
$$

This is where the simplifying assumption on the labor demand elasticity $\delta \equiv 1-\frac{\beta_{b}}{1-\alpha_{b}}$ being constant across industries buys us tractability. We can factor out the economy wide constant from (35) and leave everything on terms of normalized wages and transformed prices.

In order to find equilibrium allocations, we need to solve for the transformed prices $\mathbf{F}=\left\{F_{b}\right\}_{b=1}^{\mathcal{B}}$. Using the intermediate input demand from the final good producer (4) and the above expression for industry labor supply $L_{b}$ we get:

$$
F_{b}^{\psi_{b}(1+\eta)} A_{b}\left(\widetilde{\Phi}_{b} \Gamma_{b}^{\eta}\right)^{1-\delta}=\theta_{b} \prod_{b^{\prime} \in \mathcal{B}}\left(A_{b^{\prime}}\left(\widetilde{\Phi}_{b^{\prime}} \Gamma_{b^{\prime}}^{\eta}\right)^{1-\delta}\right)^{\theta_{b^{\prime}}} \prod_{b^{\prime} \in \mathcal{B}}\left(F_{b^{\prime}}^{\alpha_{b^{\prime}}\left(1+\varepsilon_{b} \delta\right)+\psi_{b} \eta(1-\delta)}\right)^{\theta_{b^{\prime}}}
$$

where we used $1+\varepsilon_{b} \delta+\psi_{b} \eta(1-\delta)=\psi_{b}(1+\eta)$. Solving for $F_{b}$ we get (22) from the main text.

## Aggregate Labor Share

Here we present the steps to compute aggregate labor share, capital to labor expenditures and profit to labor expenditure shares.

Aggregating (16) to the industry level,

$$
\begin{equation*}
w_{b} L_{b}=\beta_{b} \Lambda_{b} P_{b} Y_{b} \tag{39}
\end{equation*}
$$

where, $w_{b}=\sum_{i o \in \mathcal{I}_{b}} w_{i o} s_{i o \mid m} s_{m \mid b}$ is the labor weighted average of individual and $\mathcal{I}_{b}$ is the set of establishmentoccupations that belong to industry $b$. The industry wedge $\Lambda_{b}=\sum_{i o \in \mathcal{I}_{b}} \lambda_{i o} \frac{P_{b} Y_{i o}}{P_{b} Y_{b}}$ is just the value added weighted average of individual wedges. Using (33) and (20), the industry markdown $\Lambda_{b}$ yields the following expression:

$$
\Lambda_{b}=\frac{\sum_{i o \in \mathcal{I}_{b}} \lambda_{i o} A_{i o} s_{i o \mid m}^{1-\delta} s_{m \mid b}^{1-\delta}}{A_{b}}
$$

Industry and aggregate labor shares are:

$$
\begin{equation*}
L S_{b}=\beta_{b} \Lambda_{b}, \quad L S=\frac{\sum_{b \in \mathcal{B}} w_{b} L_{b}}{\sum_{b \in \mathcal{B}} P_{b} Y_{b}} \tag{40}
\end{equation*}
$$

Substituting (39) and realizing that industry $b$ expenditure share is equal to $\theta_{b}$,

$$
L S=\sum_{b \in \mathcal{B}} \beta_{b} \Lambda_{b} \theta_{b} .
$$

For given parameters, knowing the industry wedge $\Lambda_{b}$ is enough to compute the aggregate labor share.

## A. 6 Hat Algebra

From the main text, we get that the counterfactual wage $w_{i o}^{\prime}$ from (28) can be written as: $w_{i o}^{\prime}=\omega_{i o} \frac{\widehat{F}_{b}}{\frac{1}{p^{1+\varepsilon_{b} \delta}}} \Phi_{m}^{\prime}\left(1-\eta / \varepsilon_{b}\right) v_{b}\left(\frac{\Phi^{\prime}}{L^{\prime}}\right)^{v_{b}}$ where we denote by $\omega_{i 0}$ the establishment-occupation component of the counterfactual wage. This variable $\omega_{i o}$ contains the counterfactual equilibrium wedge $\lambda_{i 0}^{\prime}$.

Summing $T_{i o}\left(w_{i o}^{\prime}\right)^{\varepsilon_{b}}$ and factoring out the industry or economy wide constants we find the following relation,

$$
\Phi_{m}^{\prime}=\widetilde{\Phi}_{m}^{\prime}{ }_{m}^{\psi_{b}} \frac{\widehat{F}_{b}^{\psi_{b} \varepsilon_{b}}}{P^{\frac{\psi_{b} \varepsilon_{b}}{1+\varepsilon_{b} \delta}}}\left(\frac{\Phi^{\prime}}{L^{\prime}}\right)^{\psi_{b} v_{b} \varepsilon_{b}}, \quad \widetilde{\Phi}_{m}^{\prime}=\sum_{i o \in I_{m}} T_{i o} \omega_{i o}^{\varepsilon_{b}}
$$

Using the definition of $\Phi_{b}^{\prime}=\sum_{m \in \mathcal{M}_{b}} \Phi_{m}^{\prime}{ }^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}$, we have that $\Phi_{b}^{\prime}$ and $\Phi^{\prime}$ are:

$$
\begin{aligned}
& \Phi_{b}^{\prime}=\widetilde{\Phi}_{b}^{\prime} \frac{\widehat{F}_{b}^{\psi_{b} \eta}}{P^{\frac{\psi_{b} \eta}{1+\varepsilon_{b} \delta}}}\left(\frac{\Phi^{\prime}}{L^{\prime}}\right)^{\psi_{b} v_{b} \eta}, \quad \widetilde{\Phi}_{b}^{\prime}=\sum_{m \in \mathcal{M}_{b}}\left(\widetilde{\Phi}_{m}^{\prime}\right)^{\psi_{b} \eta / \varepsilon_{b}} \\
& \Phi^{\prime}=\left(\widetilde{\Phi}^{\prime}\right)^{1+\eta \delta} P^{-\eta} L^{\prime-\eta \delta}, \quad \widetilde{\Phi}^{\prime}=\sum_{b^{\prime} \in \mathcal{B}} \widetilde{\Phi}_{b}^{\prime} \widehat{F}_{b^{\prime}}^{\psi_{b^{\prime}} \eta} \Gamma_{b^{\prime}}^{\eta} .
\end{aligned}
$$

Industry employment in the counterfactual is equal to:

$$
L_{b}^{\prime}=\frac{\widehat{F}_{b}^{\psi_{b} \eta} \widetilde{\Phi}_{b}^{\prime} \Gamma_{b}^{\eta}}{\sum_{b^{\prime} \in \mathcal{B}} \widehat{F}_{b^{\prime}}^{\psi_{b} \eta} \widetilde{\Phi}_{b^{\prime}}^{\prime} \Gamma_{b^{\prime}}^{\eta}} L^{\prime}
$$

Establishment-occupation output in the counterfactual is:

$$
\begin{aligned}
y_{i o}^{\prime} & =\left(F_{b}^{\prime}\right)^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)} A_{i o}\left(L_{i o}^{\prime}\right)^{1-\delta} \\
& =P P_{b}^{\frac{1}{1-\alpha_{b}}} A_{i o} \frac{\left(F_{b}^{\prime}\right)^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)}}{P P_{b}^{\frac{1}{1-\alpha_{b}}}}\left(L_{i o}^{\prime}\right)^{1-\delta} \\
& =\frac{\widehat{F}_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)}}{P P_{b}} Z_{i o}\left(L_{i o}^{\prime}\right)^{1-\delta} .
\end{aligned}
$$

The analogue expression for the baseline is: $y_{i o}=\frac{1}{P P_{b}} Z_{i o} L_{i o}^{1-\delta}$. Aggregating up to industry $b$ level, the counterfactual industry output $Y_{b}^{\prime}$ is,

$$
Y_{b}^{\prime}=\frac{\widehat{F}_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)}}{P P_{b}} Z_{b}\left(s^{\prime}\right)\left(L_{b}^{\prime}\right)^{1-\delta}, \quad Z_{b}\left(s^{\prime}\right) \equiv \sum_{i o \in \mathcal{I}_{b}} Z_{i o}\left(s_{i o \mid m}^{\prime}\right)^{1-\delta}\left(s_{m o \mid b}^{\prime}\right)^{1-\delta}
$$

The analogue expression for the baseline is: $Y_{b}=\frac{1}{P P_{b}} Z_{b}(s) L_{b}^{1-\delta}$ with $Z_{b}(s)$ analogue to the one defined for the counterfactual but with baseline employment shares, $Z_{b}(s) \equiv \sum_{i o \in \mathcal{I}_{b}} Z_{i o} s_{i o \mid m}^{1-\delta} s_{m \mid b}^{1-\delta}$. Taking the ratio, counterfactual industry output relative to the baseline, $\widehat{Y}_{b}$ is:

$$
\begin{equation*}
\widehat{Y}_{b}=\widehat{F}_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)} \widehat{Z}_{b} \widehat{L}_{b}^{1-\delta} \tag{41}
\end{equation*}
$$

where $\widehat{Z}_{b}=\frac{Z_{b}\left(s^{\prime}\right)}{Z_{b}(s)}$. Using $L_{b}^{\prime}$ and equation (4) we get,

$$
\begin{equation*}
\widehat{F}_{b}^{\psi_{b}(1+\eta)} \widehat{Z}_{b}\left(\frac{\widetilde{\Phi}_{b}^{\prime} \Gamma_{b}^{\eta}}{L_{b}}\right)^{1-\delta}=\prod_{b^{\prime} \in \mathcal{B}}\left(\widehat{F}_{b^{\prime}}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)+(1-\delta) \psi_{b} \eta}\right)^{\theta_{b^{\prime}}} \prod_{b^{\prime} \in \mathcal{B}} \widehat{Z}_{b^{\prime}}^{\theta_{b^{\prime}}} \prod_{b^{\prime} \in \mathcal{B}}\left(\frac{\widetilde{\Phi}_{b^{\prime}}^{\prime} \Gamma_{b^{\prime}}^{\eta}}{L_{b^{\prime}}}\right)^{(1-\delta) \theta_{b^{\prime}}} \tag{42}
\end{equation*}
$$

By taking the ratio, the elasticities $\theta_{b}$ and the economy wide constants cancel out on both side. Rewriting, we get an expression very similar to (22) in Proposition 2 with hat variables:

$$
\begin{gather*}
\widehat{F}_{b}=\widehat{X}_{b} \widehat{C}^{\frac{1}{\psi_{b}(1+\eta)}}  \tag{43}\\
\widehat{X}_{b}=\left(\frac{L_{b}^{1-\delta}}{\widehat{Z}_{b}\left(\widetilde{\Phi^{\prime}}{ }_{b} \Gamma_{b}^{\eta}\right)^{1-\delta}}\right)^{\frac{1}{\psi_{b}(1+\eta)}}, \widehat{C}=\left(\prod_{b^{\prime} \in \mathcal{B}}\left(\widehat{X}_{b^{\prime}}^{-\chi_{b^{\prime}}}\right)^{\theta_{b^{\prime}}}\right)^{\frac{1+\eta}{\bar{L}_{b^{\prime} \in \mathcal{B}^{\theta} b_{b^{\prime}}\left(1-\alpha_{\left.b^{\prime}\right)}(1+\eta \delta)\right.}}} .
\end{gather*}
$$

## Fixed Labor

In the case where employment is fixed at the industry level $b$, the counterfactual wage (28) becomes:

$$
w_{i o}^{\prime}=\left(\beta_{b} \lambda_{i o} \frac{Z_{i o}}{T_{i o}^{\delta}}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} \frac{\widehat{F}_{b}}{P^{\frac{1}{1+\varepsilon_{b} \delta}}}\left(\Phi_{m}^{\prime}\right)^{\left(1-\eta / \varepsilon_{b}\right) v_{b}}\left(\frac{\Phi_{b}^{\prime}}{L_{b}^{\prime}}\right)^{v_{b}} .
$$

Fixing lower levels than $b$ would only change the last element. Keeping total employment at the local labor market fixed, the last term would become: $\left(\frac{\Phi_{m}^{\prime}}{L_{m}^{\prime}}\right)^{v_{b}}$. The constant $\Gamma_{b}$ does not appear in this case as workers can't move across industries and the functional $\Gamma_{b}$ is the same for all the local labor markets within an industry. Also, fixing lower levels than $b$ clearly implies that $L_{b}^{\prime}$ is known and equal to the baseline labor in the industry $L_{b}$.

The counterfactuals where employment at $b$ or lower level employment is fixed will give rise to a condition similar to (42). Given that $L_{b}^{\prime}$ is known, we have that:

$$
\widehat{F}_{b}^{1+\varepsilon_{b} \delta} \widehat{Z}_{b}=\prod_{b^{\prime} \in \mathcal{B}}\left(\widehat{F}_{b^{\prime}}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)} \widehat{Z}_{b^{\prime}}\right)^{\theta_{b^{\prime}}} .
$$

Propositions 1 and 2 therefore also apply in the relative counterfactuals with fixed labor at the industry level $b$ (or at a lower level).

## B Extensions

## B. 1 Endogenous Participation

We showed in the proof of Proposition 2 that the solution of transformed prices $\mathbf{F}$ is homogeneous of degree zero with respect to total employment level which we denote here as $L_{e}$. We have that,

$$
L_{i o}\left(w_{i o}\right)=\frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\Phi_{m}} \frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi} L=\frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\Phi_{m}} \frac{\Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}}{\Phi_{e}} L_{e}
$$

We have that $L_{e}=\frac{\Phi_{e}}{\Phi} L$ with $\Phi_{e}=\sum_{m \in \mathcal{I}_{m}} \Phi_{m}^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}$ is the part of $\Phi$ that comes from the employed and $\Phi_{u}=\sum_{u o \in \mathcal{U}_{m}}\left(T_{u o} w_{R o}^{\varepsilon_{b}}\right)^{\eta / \varepsilon_{b}} \Gamma_{b}^{\eta}$ is the part from the out of the labor force as in the main text.

The model aggregation steps are the same as in A with the exception that $L_{b}$ now is $L_{b, e}$.
Note that the markdown is the same as the TFP of the out-of-the-labor-force workers and is set to 0 . From (35),

$$
\begin{align*}
& \Phi_{b, e}=\left(\frac{\Phi}{L}\right)^{\psi_{b} v_{b} \eta} \sum_{m \in \mathcal{M}_{b}} \widetilde{\Phi}_{m}^{\psi_{b} \eta / \varepsilon_{b}} F_{b}^{\psi_{b} \eta} \Gamma_{b}^{\eta}=\left(\frac{\Phi}{L}\right)^{\psi_{b} v_{b} \eta} \widetilde{\Phi}_{b, e} F_{b}^{\psi_{b} \eta}  \tag{44}\\
& \widetilde{\Phi}_{b, e}=\sum_{m \in \mathcal{M}_{b}} \widetilde{\Phi}_{m}^{\psi_{b} \eta / \varepsilon_{b}}
\end{align*}
$$

and,

$$
\begin{align*}
& \Phi_{e}=\left(\frac{\Phi}{L}\right)^{\psi_{b} v_{b} \eta} \sum_{b \in \mathcal{B}} \widetilde{\Phi}_{b, e} F_{b}^{\psi_{b} \eta} \Gamma_{b}^{\eta}=\left(\frac{\Phi}{L}\right)^{\psi_{b} v_{b} \eta} \widetilde{\Phi}_{e}  \tag{45}\\
& \widetilde{\Phi}_{e}=\sum_{b \in \mathcal{B}} \widetilde{\Phi}_{b, e} F_{b}^{\psi_{b} \eta} \Gamma_{b}^{\eta}
\end{align*}
$$

Therefore,

$$
L_{b, e}=\frac{\Phi_{b, e}}{\Phi_{e}} L=\frac{\widetilde{\Phi}_{b, e}}{\widetilde{\Phi}_{e}} L
$$

where $L$ is total labor supply (employed and out-of-the-labor-force) and we can solve for the prices without knowing total employment level $L_{e}$. In order to get that, we need to solve for $\Phi_{e}$ in equation (45),

$$
\Phi_{e}^{\frac{1+\eta \delta}{\eta \delta}} L=\left(\Phi_{e}+\Phi_{u}\right) \widetilde{\Phi}_{e}^{\frac{1+\eta \delta}{\eta \delta}} .
$$

The solution is obviously unique as the left hand side is convex and the right hand side linear. With the solution for $\Phi_{e}$ one can construct all the aggregates back.

## B. 2 Agglomeration

Plugging the labor supply into (31), the wage in the baseline economy is,

$$
w_{i o}=\left(\beta_{b} \lambda\left(\mu_{i o}, \varphi_{b}\right) \frac{Z_{i o}}{\left(T_{i o} \Gamma_{b}^{\eta}\right)^{\delta}}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} \Phi_{m}^{v_{b}-\frac{\eta}{\varepsilon_{b}} \widetilde{v_{b}}} P^{-\frac{1}{1+\varepsilon_{b} \delta}}\left(\frac{\Phi}{L}\right)^{\widetilde{v_{b}}}, \quad v_{b}=\frac{\delta}{1+\varepsilon_{b} \delta^{\prime}}, \quad \widetilde{v_{b}}=\frac{\delta-\gamma}{1+\varepsilon_{b} \delta} .
$$

The baseline wage can be written as: $w_{i o}=\widetilde{w}_{i o} \Phi_{m}^{v_{b}-\frac{\eta}{\varepsilon_{b}} \widetilde{v}_{b}} P^{-\frac{1}{1+\varepsilon_{b} \delta}}\left(\frac{\Phi}{L}\right)^{\widetilde{v_{b}}}$. Analogously, the counterfactual wage is: $w_{i o}=\omega_{i o} \widehat{F}_{b} \Phi_{m}^{v_{b}-\frac{\eta}{\varepsilon_{b}} \widetilde{v_{b}}} P^{-\frac{1}{1+\varepsilon_{b} \delta}}\left(\frac{\Phi}{L}\right)^{\widetilde{v_{b}}}$. Aggregating to generate $\Phi_{m}$,

$$
\begin{equation*}
\Phi_{m}=\widetilde{\Phi}_{m}^{\widetilde{\psi_{b}}} P^{-\frac{\widetilde{\psi_{b}} \varepsilon_{b}}{1+\varepsilon_{b} \delta}}\left(\frac{\Phi}{L}\right)^{\widetilde{\psi_{b}} \widetilde{v}_{b} \varepsilon_{b}}, \quad \widetilde{\psi_{b}} \equiv \frac{1+\varepsilon_{b} \delta}{1+\eta(\delta-\gamma)} . \tag{46}
\end{equation*}
$$

The counterfactual $\Phi_{m}^{\prime}$ is analogously $\Phi_{m}^{\prime}=\left(\widetilde{\Phi^{\prime}}{ }_{m}{\widetilde{\psi_{b}}}^{-\frac{\widetilde{\psi_{b}} \varepsilon_{b}}{1+\varepsilon_{b} \delta}} \widehat{F}_{b}^{\widetilde{\psi}_{b} \varepsilon_{b}}\left(\frac{\Phi^{\prime}}{L}\right)^{\widetilde{\psi_{b}} \widetilde{v}_{b} \varepsilon_{b}}\right.$.
In order to be able to find a solution to the model, we need that $\widetilde{\psi_{b}}<\infty$. This is equivalent to requiring $\gamma \neq \frac{1}{\eta}+\delta$. The parameter $\gamma$ governs the strength of agglomeration forces within a local labor market, and $\delta$ and $\frac{1}{\eta}$ are related with dispersion forces. Those come from the decreasing returns to scale ( $\delta$ ) and from the variance of taste shocks $\left(\frac{1}{\eta}\right)$. When the latter is high, the mass of workers having extreme taste shocks is higher. This implies that agglomeration forces will impact less as workers would be more inelastic to changes in wages. The standard condition for uniqueness of the equilibrium with agglomeration would be that is sufficiently weak ( $\gamma \leq \frac{1}{\eta}+\delta$ ). In our context we do not find such inequality condition.

The counterfactual industry labor supply is:

$$
L_{b}^{\prime}=\frac{\widehat{F}_{b}^{\psi_{b} \eta} \widetilde{\Phi}_{b}^{\prime} \Gamma_{b}^{\eta}}{\sum_{b \in \mathcal{B}} \widehat{F}_{b^{\prime}}^{\widetilde{\psi}_{b}} \eta \widetilde{\Phi}_{b^{\prime}}^{\prime} \Gamma_{b^{\prime}}^{\eta}}
$$

Turning to production, the establishment-occupation output $y_{i o}^{\prime}$ and local labor market output $Y_{m}$ in the counterfactual and the baseline are respectively:

$$
\begin{aligned}
& y_{i o}^{\prime}=\frac{Z_{i o} \widehat{F}_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)}}{P_{b} P} L_{i o}^{\prime 1-\delta} L_{m}^{\prime}{ }^{\gamma} \\
& Y_{m}^{\prime}=\frac{Z_{m}\left(s^{\prime}\right) \widehat{F}_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)}}{P_{b} P} L_{m}^{\prime 1-\delta+\gamma}, \quad Z_{m}\left(s^{\prime}\right)=\sum_{i \in \mathcal{I}_{m}} Z_{i o} s_{i o \mid m}^{\prime}{ }^{1-\delta} .
\end{aligned}
$$

The expressions for the baseline are analogous but setting $\widehat{F}_{b}=1$. The counterfactual output of industry $b$, $Y_{b}^{\prime}$, when there are agglomeration forces is:

$$
Y_{b}^{\prime}=\frac{Z_{b}\left(s^{\prime}\right) \widehat{F}_{b}^{\alpha_{b}\left(1+\varepsilon_{b} \delta\right)}}{P_{b} P} L_{b}^{\prime 1-\delta+\gamma}, \quad Z_{b}\left(s^{\prime}\right)=\sum_{m \in \mathcal{M}_{b}} Z_{m} s_{m o \mid b}^{\prime}{ }^{1-\delta+\gamma},
$$

where $\gamma$ changed the returns to scale of the industry production function and the aggregation of productivities $Z_{b}\left(s^{\prime}\right)$. The intermediate good demand in the counterfactual relative to the baseline is:

$$
\begin{aligned}
\widehat{F}_{b}^{1+\varepsilon_{b} \delta} \widehat{Z}_{b}\left(\frac{L_{b}^{\prime}(\widehat{\mathbf{F}})}{L_{b}}\right)^{1-\delta+\gamma} & =\prod_{b^{\prime} \in \mathcal{B}} \widehat{F}_{b^{\prime}}^{\alpha_{b^{\prime}}\left(1+\varepsilon_{b} \delta\right)} \widehat{Z}_{b^{\prime}}\left(\frac{L_{b^{\prime}}^{\prime}(\widehat{\mathbf{F}})}{L_{b^{\prime}}}\right)^{1-\delta+\gamma} \\
\Leftrightarrow & \widehat{F}_{b} \widehat{\psi}_{b}(1+\eta) \widehat{Z}_{b}\left(\frac{\widetilde{\Phi}_{b}^{\prime} \Gamma_{b}^{\eta}}{L_{b}}\right)^{1-\delta+\gamma}=\prod_{b^{\prime} \in \mathcal{B}} \widehat{F}_{b^{\prime}}^{\alpha_{b^{\prime}}\left(1+\varepsilon_{b} \delta\right)+\widetilde{\psi}_{b} \eta(1-\delta+\gamma)} \widehat{Z}_{b^{\prime}}\left(\frac{\widetilde{\Phi}_{b^{\prime}}^{\prime} \Gamma_{b^{\prime}}^{\eta}}{L_{b^{\prime}}}\right)^{1-\delta+\gamma} .
\end{aligned}
$$

Uniqueness of the solution to this system of equations is guaranteed by $\sum_{b \in \mathcal{B}} \alpha_{b} \theta_{b}<1$. This condition being the same as for Proposition 2, uniqueness of the equilibrium with agglomeration forces only needs the additional requirement of $\gamma \neq \frac{1}{\eta}+\delta$.

## C Proofs

## Proof of Proposition 1.

Existence. We follow closely the proof by Kucheryavyy (2012). Define the right hand side of (17) as:

$$
f_{i o}(\mathbf{w})=\left[\lambda\left(\mu_{i o}(\mathbf{w}), \varphi_{b}\right)\right]^{\frac{1}{1+\varepsilon_{b}}} c_{i o}, f_{i o}(\mathbf{w})=[\lambda(\mu(s(\mathbf{w})))]^{\frac{1}{1+\varepsilon_{b} \delta}} c_{i 0}
$$

where $\mathbf{w}$ denotes the vector formed by $\left\{w_{i o}\right\}$, we simplified the notation of the wedge $\lambda\left(\mu_{i 0}, \varphi_{b}\right)$ from the main text getting rid of the second argument and $c_{i o}=\left(\beta_{b} \frac{A_{i o}}{\left(T_{i 0} \Gamma_{b}^{\prime}\right)^{\delta}}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} \Phi_{m}^{\left(1-\eta / \varepsilon_{b}\right) v_{b}}\left(\frac{\Phi}{L}\right)^{v_{b}} F_{b}$ is an establishmentoccupation specific parameter. This means we take $\Phi_{m}$ and $\Phi$ as constants and not as functions of $w_{i o}$.

Under the assumption $0<\eta<\varepsilon_{b}$, the function $\mu(s)=\frac{\varepsilon_{b}(1-s)+\eta s}{\varepsilon_{b}(1-s)+\eta s+1}$ is decreasing in $s$, the employment share out of the local labor market. We therefore also have that the wedge $\lambda(\mu(s))=\left(1-\varphi_{b}\right) \mu(s)+\varphi_{b} \frac{1}{1-\delta}$ is also decreasing in $s$. The employment share has bounds $0 \leq s \leq 1$, which implies $\left(1-\varphi_{b}\right) \frac{\eta}{\eta+1}+\varphi_{b} \frac{1}{1-\delta} \leq$ $\lambda(\mu(s)) \leq\left(1-\varphi_{b}\right) \frac{\varepsilon_{b}}{\varepsilon_{b}+1}+\varphi_{b} \frac{1}{1-\delta}$. Also, $1+\varepsilon_{b} \delta>0$. Therefore we have that $f_{i o}(\mathbf{w})$ is bounded:

$$
\left(\left(1-\varphi_{b}\right) \frac{\eta}{\eta+1}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} c_{i o} \leq f_{i}(\mathbf{w}) \leq\left(\left(1-\varphi_{b}\right) \frac{\varepsilon_{b}}{\varepsilon_{b}+1}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} c_{i o}
$$

If the number of participants in sub-market $m$ is $N_{m}$, we can define the compact set $S$ where $f_{i o}(\mathbf{w})$ maps into itself as:

$$
\begin{aligned}
S & =\left[\left(\left(1-\varphi_{b}\right) \frac{\eta}{\eta+1}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} c_{1},\left(\left(1-\varphi_{b}\right) \frac{\varepsilon_{b}}{\varepsilon_{b}+1}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} c_{1}\right] \times \ldots \\
& \times\left[\left(\left(1-\varphi_{b}\right) \frac{\eta}{\eta+1}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} c_{N_{m}}\left(\left(1-\varphi_{b}\right) \frac{\varepsilon_{b}}{\varepsilon_{b}+1}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\varepsilon_{b} \delta}} c_{N_{m}}\right] .
\end{aligned}
$$

The function $f_{i o}(\mathbf{w})$ is continuous in wages on $S$. We can therefore apply Brouwer's fixed point theorem and claim that at least one solution exists for the system of equations formed by (19).

Uniqueness. First we introduce the following Theorem and Corollary that we will use later to establish uniqueness in our proofs. These are just transcribed from Allen et al. (2016):

Theorem 1. Consider $g: \mathbb{R}_{++}^{n} \times \mathbb{R}_{++}^{m}$ for some $n \in\{1, \ldots, N\}$ and $m \in\{1, \ldots, M\}$ such that:

1. homogeneity of any degree: $g(t x, t y)=t^{k} g(x, y), t \in \mathbb{R}_{++} 0$ and $k \in \mathbb{R}$,
2. gross-substitution property: $\frac{\partial g_{i}}{\partial x_{j}}>0$ for all $i \neq j$,
3. monotonicity with respect to the joint variable: $\frac{\partial g_{i}}{\partial y_{k}} \geq 0$, for all $i, k$.

Then, for any given $y^{0} \in \mathbb{R}_{++}^{M}$ there exists at most one solution satisfying $g\left(x, y^{0}\right)=0$.
Proof. See the proof for Theorem 5 in Allen et al. (2016).
Corollary 1. Assume (i) $f(x)$ satisfies gross-substitution and (ii) $f(x)$ can be decomposed as $f(x)=\sum_{j=1}^{v_{f}} g^{j}(x)$ $\sum_{k=1}^{v_{g}} h^{k}(x)$ where $g^{j}(x), h^{k}(x)$ are non-negative vector functions and, respectively, homogeneous of degree $\alpha_{j}$ and $\beta_{k}$, $\bar{\alpha}=\max \alpha_{j} \leq \min \beta_{k}$.

1. Then there is at most one up-to-scale solution of $f(x)=0$.
2. In particular, if for some $j, k \alpha_{j} \neq \beta_{k}$, then there is at most one solution.

Proof. See the proof for Corollary 1 in Allen et al. (2016).
In order to prove uniqueness we use Theorem 1 and Corollary 1 stated above.
Define the function $g: \mathbb{R}_{++}^{n} \rightarrow \mathbb{R}^{n}$ for some $n \in\{1, \ldots, N\}$ as:

$$
g_{i o}(\mathbf{w})=f_{i o}(\mathbf{w})-w_{i o}, \quad \forall i \in\{1, . ., N\}
$$

We want to prove that the solution satisfying $g(\mathbf{w})=0$ is unique. In order to do so, we first need to show that $g(\mathbf{w})$ satisfies the gross substitution property $\left(\frac{\partial g_{i o}}{\partial w_{j o}}>0\right.$ for any $\left.j \neq i\right)$.

Taking the partial derivative of $g_{i o}$ with respect to $w_{j o}$ for any $j \neq i$ :

$$
\frac{\partial g_{i o}}{\partial w_{j o}}=\frac{\partial f_{i o}(\mathbf{w})}{\partial \lambda(\mu(s(\mathbf{w}))} \times \frac{\partial \lambda\left(\mu\left(s_{i o \mid m}\right)\right)}{\partial \mu\left(s_{i o \mid m}\right)} \times \frac{\partial \mu\left(s_{i o \mid m}\right)}{\partial s_{i o \mid m}} \times \frac{\partial s_{i o \mid m}}{\partial w_{j o}}
$$

where $\frac{\partial f_{i o}(\mathbf{w})}{\partial \lambda(\mu(s(\mathbf{w}))}=\frac{1}{1+\varepsilon_{b} \delta} \frac{f_{i o}(\mathbf{w})}{\lambda(\mu(s(\mathbf{w}))}>0$. We have that $\frac{\partial \lambda\left(\mu\left(s_{i o \mid m}\right)\right)}{\partial \mu\left(s_{i o \mid m}\right)}>0$ and we previously established that, under the assumption that $0<\eta<\varepsilon_{b}, \frac{\partial \mu\left(s_{i o \mid m}\right)}{\partial s_{i o \mid m}}<0$. The share of an establishment $i$ with occupation $o$ in sub-market $m o$ is defined as:

$$
s_{i o \mid m}=\frac{T_{i o} w_{i o}^{\varepsilon_{b}}}{\sum_{j \in \mathcal{I}_{m}} T_{j o} w_{j o}^{\varepsilon_{b}}}
$$

Clearly, $\frac{\partial s_{i o \mid m}}{\partial w_{j o}}<0$ for any $i \neq j$. Therefore $\frac{\partial g_{i o}}{\partial w_{j o}}>0$ for any $i \neq j$ and $g$ satisfies the gross-substitution property.
The remaining condition to use Corollary 1 is simply that $f_{i o}(\mathbf{w})$ is homogeneous of a degree smaller than $1 .{ }^{56}$ Clearly, $f_{i o}(\mathbf{w})$ is homogeneous of degree 0 as a consequence that the markdown function itself $\mu\left(s_{i o \mid m}\right)$ is homogeneous of degree 0 . Therefore, the function $g$ satisfies the conditions of Corollary 1 and we can conclude that there exists at most one solution satisfying $g(\mathbf{w})=0$.

## Proof of Proposition 2.

Developing equation (21) we get

$$
\begin{aligned}
& F_{b}^{1+\varepsilon_{b} \delta} A_{b}\left(\frac{F_{b}^{\psi_{b} \eta} \widetilde{\Phi}_{b} \Gamma_{b}^{\eta}}{\widetilde{\Phi}} L\right)^{1-\delta}=\theta_{b} \prod_{b^{\prime} \in \mathcal{B}}\left(F_{b^{\prime}}^{\alpha_{b^{\prime}}\left(1+\varepsilon_{b} \delta\right)}\right)^{\theta_{b^{\prime}}} \prod_{b^{\prime} \in \mathcal{B}} A_{b^{\prime}}^{\theta_{b^{\prime}}} \prod_{b^{\prime} \in \mathcal{B}}\left(\frac{\left.F_{b^{\prime}}^{\psi_{b} \eta} \widetilde{\Phi}_{b^{\prime}} \Gamma_{b^{\prime}}^{\eta} L\right)^{(1-\delta) \theta_{b^{\prime}}}}{\widetilde{\Phi}}\right. \\
& \Leftrightarrow F_{b}^{\psi_{b}(1+\eta)} A_{b}\left(\widetilde{\Phi}_{b} \Gamma_{b}^{\eta}\right)^{1-\delta}=\theta_{b} \prod_{b^{\prime} \in \mathcal{B}}\left(A_{b^{\prime}}\left(\widetilde{\Phi}_{b^{\prime}} \Gamma_{b^{\prime}}^{\eta}\right)^{1-\delta}\right)^{\theta_{b^{\prime}}} \prod_{b^{\prime} \in \mathcal{B}}\left(F_{b^{\prime}}^{\alpha_{b^{\prime}}\left(1+\varepsilon_{b^{\prime}} \delta\right)+\psi_{b^{\prime}} \eta(1-\delta)}\right)^{\theta_{b^{\prime}}}
\end{aligned}
$$

[^29]Define $f_{b}=\log \left(F_{b}\right)$ and $\mathbf{f}$ as a $B \times 1$ vector whose element $b^{\prime}$ is $f_{b^{\prime}}$. Then, taking logs and rearranging the previous expression we obtain:

$$
f_{b}=C_{b}+\mathbf{d}^{\prime} \mathbf{f}
$$

where

$$
C_{b}=\frac{1}{\psi_{b}(1+\eta)}\left[\log \left(\theta_{b}\right)-\log \left(A_{b}\right)-(1-\delta) \log \left(\widetilde{\Phi}_{b} \Gamma_{b}^{\eta}\right)+\sum_{b^{\prime} \in \mathcal{B}} \theta_{b^{\prime}}\left(\log \left(A_{b^{\prime}}\right)+(1-\delta) \log \left(\widetilde{\Phi}_{b^{\prime}} \Gamma_{b^{\prime}}^{\eta}\right)\right)\right]
$$

and $\mathbf{d}$ is a $B \times 1$ vector whose $b^{\prime}$ element $\mathbf{d}_{b^{\prime}}$ is:

$$
\mathbf{d}_{b^{\prime}}=\frac{1}{\psi_{b^{\prime}}(1+\eta)}\left(\alpha_{b^{\prime}}\left(1+\varepsilon_{b^{\prime}} \delta\right)+\psi_{b^{\prime}} \eta(1-\delta)\right) \theta_{b^{\prime}}
$$

Define the vector $\mathbf{C}=\left[C_{1}, \ldots, C_{b}, \ldots, C_{B}\right]$ that contains the constant terms and the matrix $\mathbf{D}=[d, \ldots, d]$ which repeats the $\mathbf{D}$ vector $B$ times. We can stack all the terms for all $b \in \mathcal{B}$ from the previous expression and obtain the following system of equations:

$$
\begin{equation*}
\mathbf{f}=\mathbf{C}+\mathbf{D}^{\prime} \mathbf{f} \tag{47}
\end{equation*}
$$

A solution to the system (47) exists if the matrix $\mathbf{I}-\mathbf{D}^{\prime}$ is invertible. This matrix has an eigenvalue of zero if and only if the sum of the elements of the vector $\mathbf{d}$ is equal to 1 . Additionally, this sum is equal to 1 if and only if $\sum_{b} \alpha_{b} \theta_{b}=1$ as:

$$
\begin{aligned}
\sum_{b} \mathbf{d}_{b}=1 & \Leftrightarrow \sum_{b}\left(\alpha_{b}\left(1+\varepsilon_{b} \delta\right)+\psi_{b} \eta(1-\delta)\right) \theta_{b}=\psi_{b}(1+\eta) \\
& \Leftrightarrow \sum_{b} \alpha_{b} \theta_{b}\left(1+\varepsilon_{b} \delta\right)=\psi_{b}(1+\eta \delta) \Leftrightarrow \sum_{b} \alpha_{b} \theta_{b}=1 .
\end{aligned}
$$

Therefore we can conclude that whenever $\sum_{b} \alpha_{b} \theta_{b} \neq 1$ the transformed prices $\mathbf{F}$ have a unique solution. This is always the case as long as $0 \leq \beta_{b}, \theta_{b}<1 \forall b \in \mathcal{B}$ and $0 \leq \delta \leq 1$.

In order to obtain the closed form solution, rewrite (21) as:

$$
F_{b}=\left(\frac{\theta_{b}}{A_{b}\left(\widetilde{\Phi}_{b} \Gamma_{b}^{\eta}\right)^{(1-\delta)}}\right)^{\frac{1}{\psi_{b}^{(1+\eta)}}} C^{\frac{1}{\psi_{b}(1+\eta)}}=X_{b} C^{\frac{1}{\psi_{b}(1+\eta)}}
$$

where $C$ is a constant that is equal to:

$$
C=\prod_{b^{\prime} \in \mathcal{B}}\left(A_{b^{\prime}}\left(\widetilde{\Phi}_{b^{\prime}} \Gamma_{b^{\prime}}^{\eta}\right)^{1-\delta}\right)^{\theta_{b^{\prime}}} \prod_{b^{\prime} \in \mathcal{B}}\left(F_{b^{\prime}}^{\alpha_{b^{\prime}}\left(1+\varepsilon_{b^{\prime}} \delta\right)+\psi_{b^{\prime}} \eta(1-\delta)}\right)^{\theta_{b^{\prime}}} .
$$

To solve for the constant, we use the ideal price index equation substituting the relative prices $P_{b}$ for the transformed prices $F_{b}$ :

$$
1=\prod_{b \in \mathcal{B}}\left(\frac{F_{b}^{\chi_{b}}}{\theta_{b}}\right)^{\theta_{b}}
$$

Substituting $F_{b}$ into the price index and solving for $C$ we recover the expression showed in Proposition 2.

## D Identification Details

## D. 1 Identification of $\eta$ and $\delta$

In order to identify the across markets labor supply elasticity $\eta$ and the labor demand elasticity $\delta$ we exploit the fact that in local labor markets where there is only one establishment, the wedge $\lambda\left(\mu, \phi_{b}\right)$ is constant
within industries $b$. We denominate this type of establishments as full monopsonists. Additionally, the effect of wages on the labor supply of full monopsonists is only affected by the parameter $\eta$ as the within market labor supply elasticity $\varepsilon_{b}$ is irrelevant in local labor markets with only one establishment. Taking the logarithm for the labor supply full monopsonists face (13) we get:

$$
\ln \left(L_{i o, s=1}\right)=\eta \ln \left(w_{i o}\right)+\frac{\eta}{\varepsilon_{b}} \ln \left(T_{i o}\right)+\ln \left(\Gamma_{b}^{\eta} L / \Phi\right) .
$$

As mentioned before, full monopsonists apply a constant markdown equal to $\mu(s=1)=\frac{\eta}{\eta+1}$ that in turn will imply a constant wedge $\lambda\left(\mu, \phi_{b}\right)$ within industry $b$. Their (inverse) labor demand (16) in logs is:

$$
\ln \left(w_{i o, s=1}\right)=\ln \left(\beta_{b}\right)+\ln \left(\frac{\eta}{\eta+1}\right)+\ln \left(A_{i o}\right)-\delta \ln \left(L_{i o}\right)+\frac{1}{1-\alpha_{b}} \ln \left(P_{b}\right)
$$

In order to get rid of industry and economy wide constants, we demean $\ln \left(L_{i o, s=1}\right)$ and $\ln \left(w_{i o, s=1}\right)$ by removing the industry $b$ averages per year. Denoting with $\overline{\ln (X)}$ the demeaned variables, we rewrite the labor supply and (inverse) demand equations as:

$$
\begin{align*}
& \overline{\ln \left(L_{i o}\right)}=\eta \overline{\ln \left(w_{i o}\right)}+\frac{\eta}{\varepsilon_{b}} \overline{\ln \left(T_{i o}\right)}, \\
& \overline{\ln \left(w_{i o}\right)}=-\delta \overline{\ln \left(L_{i o}\right)}+\overline{\ln \left(A_{i o}\right)} . \tag{48}
\end{align*}
$$

The above system is just a traditional demand and supply setting. As it is well known, the above system is under-identified. It is the classic textbook example of when a regression model suffers from simultaneity bias. The reason for this under-identification is the following: while the variance-covariance matrix of $\left(\overline{\ln \left(L_{i o}\right)}, \overline{\ln \left(w_{i o}\right)}\right)$ gives us three objects from the data, the system above has five unknowns, which are the elasticities, $\eta$ and $\delta$, plus the three components of the variance-covariance matrix of the structural errors $\frac{\eta}{\varepsilon_{b}} \overline{\ln \left(T_{i o}\right)}$ and $\overline{\ln \left(A_{i 0}\right)}$. Therefore, in absence of valid instruments that would exogenously vary either the supply or demand equations in (48) we can not identify the elasticities. ${ }^{57}$

In order to identify the elasticities using the labor supply and demand equations in (48), we impose restrictions on the variance-covariance matrix of the structural errors while exploiting the differences in the variance-covariance matrix of the employment and wages across occupations. This way of achieving identification is known in the literature as identification through heteroskedasticity (see Rigobon (2003)). We classify our four occupations into two broader categories $S \in\{1,2\}$. Our identification assumption is that the covariance between the transformed productivity $\overline{\ln \left(A_{i o}\right)}$ and amenities $\frac{\eta}{\varepsilon_{b}} \overline{\ln \left(T_{i o}\right)}$, that we denote $\sigma_{T A}$ is constant within each category $S$. The fact that the elasticities are the same across occupational groups, in addition to the assumption of common covariance of the structural errors within broad categories, are the reason we can achieve identification. The reason is simple: while the four occupational categories give us $3 \times 4=12$ bits of information, the unknowns to be identified are $2, \delta$ and $\eta$, plus 2 , the broad category covariances, plus 8 , the variances of the transformed productivities and amenities for each of the four occupational categories. ${ }^{58}$

[^30]We can rewrite the system (48) in the following way:

$$
\begin{align*}
\frac{\eta}{\varepsilon_{b}} \overline{\ln \left(T_{i o}\right)} & =\overline{\ln \left(L_{i o}\right)}-\eta \overline{\ln \left(w_{i o}\right)} \\
\overline{\ln \left(A_{i o}\right)} & =\delta \overline{\ln \left(L_{i o}\right)}+\overline{\ln \left(w_{i o}\right)} \tag{49}
\end{align*}
$$

Denote the covariance matrix of the structural errors for occupation $o$ in category $S$ (meaning the left hand side of system (49)) by $\Psi_{o S}$. Denote the covariance matrix between employment and wages of the full monosponists by $\widehat{V}_{o S}$. The covariance of system (49) writes as:

$$
\Psi_{o S}=D \widehat{V}_{o S} D^{T}, \quad D=\left(\begin{array}{cc}
1 & -\eta \\
\delta & 1
\end{array}\right)
$$

where $T$ denotes the transpose. Formally, our identifying assumption is that $\sigma_{A T, o S}=\sigma_{A T, o^{\prime} S}$ for occupations that belong to the same category $S$. Taking differences within category,

$$
\Delta_{S} \equiv \Psi_{o S}-\Psi_{o^{\prime} S}=D\left[\widehat{V}_{o S}-\widehat{V}_{o^{\prime} S}\right] D^{T}, \quad \forall S \in\{1,2\}
$$

where the differences of covariances in the left hand (element $\Delta_{S,[1,2]}$ ) is equal to zero. This gives us a just identified system (two equations with two unknowns) to find the parameters $\eta$ and $\delta$. More details are provided in Appendix D.

The system (49) in matrix form is $\Omega_{o S}=D \widehat{V}_{o S} D^{T}$.. Defining an auxiliary parameter $\widetilde{\delta}=-\delta$, the system writes as:

$$
\left(\begin{array}{cc}
\left(\frac{\eta}{\varepsilon_{b}}\right)^{2} \sigma_{T, o S}^{2} & \frac{\eta}{\varepsilon_{b}} \sigma_{T A, S} \\
\frac{\eta}{\varepsilon_{b}} \sigma_{T A, S} & \sigma_{A, o S}^{2}
\end{array}\right)=\left(\begin{array}{cc}
1 & -\eta \\
-\widetilde{\delta} & 1
\end{array}\right)\left(\begin{array}{cc}
\sigma_{L, o S}^{2} & \sigma_{L W, o S} \\
\sigma_{L W, o S} & \sigma_{W, o S}^{2}
\end{array}\right)\left(\begin{array}{cc}
1 & -\tilde{\delta} \\
-\eta & 1
\end{array}\right)
$$

This system only allows us to identify $\eta$ and $\delta$. Denote by $\Omega_{S} \equiv \widehat{V}_{o S}-\widehat{V}_{o^{\prime} S}$ the difference between the variance covariance matrix within category $S$ and by $\Omega_{S,[1,2]}=\omega_{12, S}$ the element on first row and second column. The system of differences is:

$$
\Delta_{S}=D \Omega_{S} D^{T}, \quad \forall S \in\{1,2\}
$$

With the identification assumption of equal covariance within category, we have that:

$$
\Delta_{S,[1,2]}=0=-\eta \omega_{22, S}+(1+\eta \widetilde{\delta}) \omega_{12, S}-\widehat{\delta} \omega_{11, S}
$$

Solving for $\eta$,

$$
\eta=\frac{\omega_{12, S}-\widetilde{\delta} \omega_{11, S}}{\omega_{22, S}-\widetilde{\delta} \omega_{12, S}}, \quad \forall S \in\{1,2\}
$$

Equalizing the above across both occupation categories we get a quadratic equation in $\widehat{\delta}$ that solves:

$$
\begin{equation*}
\widetilde{\delta}^{2}\left[\omega_{11,1} \omega_{12,2}-\omega_{11,2} \omega_{12,1}\right]-\widetilde{\delta}\left[\omega_{11,1} \omega_{22,2}-\omega_{11,2} \omega_{22,1}\right]+\omega_{12,1} \omega_{22,2}-\omega_{12,2} \omega_{22,1}=0 \tag{50}
\end{equation*}
$$

This is the same system as the simple case without covariance between the fundamental shocks in Rigobon (2003). Different to him, $\Omega_{S}$ is not directly the estimated variance-covariance matrix of each of the 4 occupations but rather the matrix of differences within category or state $S$. As mentioned by Rigobon (2003) there
are two solutions to the previous equation. One can show that if $\widetilde{\delta}^{*}$ and $\eta^{*}$ are a solution then the other solution is equal to $\widetilde{\delta}=1 / \eta^{*}$ and $\eta=1 / \widetilde{\delta}^{*}$. This means that the solutions are actually the two possible ways the original structural system (48) can be written. In order to identify which of the two possible solutions we are identifying, we have that by assumption $\eta$ is positive while $\widetilde{\delta}$ is negative. Therefore as long as the two possible solutions for $\widetilde{\delta}$ have different signs, we just need to pick the negative one.

Given the identification strategy, in order to estimate the elasticities $\delta$ and $\eta$ we just need to obtain the employment and wages covariance matrices directly from the data on establishments that are full monopsonists and solve for (50).

## D. 2 Identification of $\varphi_{b}$

In order to identify the industry workers bargaining power, we need to construct the model counterparts of the industry labor share at every period $t$ :

$$
L S_{b t}^{M}\left(\varphi_{b}\right)=\frac{\beta_{b} \sum_{i o \in \mathcal{I}_{b}} w_{i o t} L_{i o t}}{\sum_{i o \in \mathcal{I}_{b}} w_{i o t} L_{i o t} / \lambda\left(\mu_{i o}, \varphi_{b}\right)},
$$

$\mathcal{I}_{b}$ being the set of all establishment-occupations that belong to 2-digit industry $b$. We target the average across time industry labor share. That is, we pick $\phi_{b}$ such that:

$$
\begin{equation*}
\mathbb{E}_{t}\left[L S_{b t}^{M}\left(\varphi_{b}\right)-L S_{b t}^{D}\right]=0 \tag{51}
\end{equation*}
$$

Given that the wedge $\lambda\left(\mu_{i o}, \varphi_{b}\right)$ is increasing in $\varphi_{b}$, then $L S_{b t}^{M}\left(\varphi_{b}\right)$ is increasing in $\varphi_{b}$ as well. Therefore, if a solution exists for (51) with $\varphi_{b} \in[0,1]$ this has to be unique. ${ }^{59}$

## D. 3 Additional Results

Table 15 has the calibrated final good production function elasticities of the intermediate the $\left\{\theta_{b}\right\}_{b=1}^{\mathcal{B}}$ and the required rate $\left\{R_{b}\right\}_{b=1}^{\mathcal{B}}$ for the year 2007.

## E Data Details

We provide additional summary statistics and details about sample selection and variable construction.

[^31]Table 14: Industry Estimates

|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Industry Code | Industry Name | $\widehat{\beta}_{b}$ | $\widehat{\varepsilon}_{b}$ | $\widehat{\varphi}_{b}$ |
| 15 | Food | 0.74 | 1.69 | 0.22 |
| 17 | Textile | 0.74 | 1.49 | 0.51 |
| 18 | Clothing | 0.84 | 1.41 | 0.31 |
| 19 | Leather | 0.85 | 2.09 | 0.26 |
| 20 | Wood | 0.77 | 1.51 | 0.42 |
| 21 | Paper | 0.61 | 3.06 | 0.55 |
| 22 | Printing | 0.84 | 1.52 | 0.18 |
| 24 | Chemical | 0.67 | 3.25 | 0.06 |
| 25 | Plastic | 0.73 | 2.51 | 0.35 |
| 26 | Other Minerals | 0.65 | 1.62 | 0.43 |
| 27 | Metallurgy | 0.61 | 3.77 | 0.59 |
| 28 | Metals | 0.81 | 1.22 | 0.38 |
| 29 | Machines and Equipments | 0.79 | 2.18 | 0.32 |
| 30 | Office Machinery | 0.81 | 3.33 | 0.20 |
| 31 | Electrical Equipment | 0.65 | 3.02 | 0.67 |
| 32 | Telecommunications | 0.62 | 3.54 | 0.73 |
| 33 | Optical Equipment | 0.75 | 1.91 | 0.45 |
| 34 | Transport | 0.57 | 4.05 | 0.69 |
| 35 | Other Transport | 0.72 | 3.49 | 0.44 |
| 36 | Furniture | 0.81 | 1.57 | 0.43 |

Notes: All the estimated parameters are 2-digit industry specific. $\widehat{\beta}_{b}$ are the estimated output elasticities with respect of labor, $\widehat{\varepsilon}_{b}$ are the within local labor market elasticities and $\widehat{\varphi}_{b}$ are union bargaining powers.

Table 15: Calibrated $\left\{\theta_{b}\right\}$ and $\left\{R_{b}\right\}$

|  |  |  |  |
| :--- | :--- | :--- | :--- |
| Industry Code | Industry Name | $\theta_{b}$ | $R_{b}$ |
| 15 | Food | 0.13 | 0.11 |
| 17 | Textile | 0.02 | 0.14 |
| 18 | Clothing | 0.01 | 0.14 |
| 19 | Leather | 0.01 | 0.14 |
| 20 | Wood | 0.02 | 0.13 |
| 21 | Paper | 0.02 | 0.13 |
| 22 | Printing | 0.06 | 0.13 |
| 24 | Chemical | 0.14 | 0.16 |
| 25 | Plastic | 0.06 | 0.15 |
| 26 | Other Minerals | 0.05 | 0.15 |
| 27 | Metallurgy | 0.03 | 0.14 |
| 28 | Metals | 0.10 | 0.14 |
| 29 | Machines and Equipments | 0.09 | 0.17 |
| 30 | Office Machinery | 0.00 | 0.17 |
| 31 | Electrical Equipment | 0.04 | 0.23 |
| 32 | Telecommunications | 0.04 | 0.23 |
| 33 | Optical Equipment | 0.04 | 0.23 |
| 34 | Transport | 0.04 | 0.19 |
| 35 | Other Transport | 0.06 | 0.19 |
| 36 | Furniture | 0.03 | 0.14 |

Notes: All the calibrated parameters are 2-digit industry specific for the year 2007. $\theta_{b}$ are the intermediate good elasticities in the final good production function and $R_{b}$ are the capital rental rates for 2007. We construct the rental rates following Barkai (2016).

## E. 1 Additional Summary Statistics

Table 17: CZ Summary Statistics. Baseline Year

| Variable | Obs. | Mean | Pctl(25) | Median | Pctl(75) | St. Dev. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $N_{n}$ | 356 | 773.798 | 266.8 | 461 | 861.2 | $1,168.407$ |
| $L_{n}$ | 356 | $8,300.567$ | $2,567.403$ | $5,244.300$ | $10,086.210$ | $11,322.000$ |
| $\bar{L}_{n}$ | 356 | 11.389 | 8.148 | 10.878 | 13.547 | 6.043 |
| $\bar{w}_{n}$ | 356 | 34.399 | 32.707 | 34.161 | 35.593 | 3.242 |

Note: $N_{n}$ is the number of establishments at the CZ, $L_{n}$ is full time equivalent employment at CZ, $\bar{L}_{n}$ is the average $L_{i o t}$ of establishment-occupations at $n, \bar{w}_{n}$ is the mean $w_{i o t}$ of the establishment-occupations at $n$ in thousands of constant 2015 euros.

Table 16: Estimated Within Elasticities for Different Lags

|  |  |  |  |
| :--- | :--- | :---: | :---: |
| Industry Code | Industry Name | 1 Lag $\widehat{\varepsilon}_{b}$ | 2 Lags $\widehat{\varepsilon}_{b}$ |
| 15 | Food | 1.69 | 1.99 |
| 17 | Textile | 1.49 | 1.83 |
| 18 | Clothing | 1.41 | 1.69 |
| 19 | Leather | 2.09 | 2.50 |
| 20 | Wood | 1.51 | 1.77 |
| 21 | Paper | 3.06 | 3.39 |
| 22 | Printing | 1.52 | 1.79 |
| 24 | Chemical | 3.25 | 3.56 |
| 25 | Plastic | 2.51 | 3.04 |
| 26 | Other Minerals | 1.62 | 1.77 |
| 27 | Metallurgy | 3.77 | 4.35 |
| 28 | Metals | 1.22 | 1.48 |
| 29 | Machines and Equipments | 2.18 | 2.63 |
| 30 | Office Machinery | 3.33 | 3.72 |
| 31 | Electrical Equipment | 3.02 | 3.61 |
| 32 | Telecommunications | 3.54 | 4.08 |
| 33 | Optical Equipment | 1.91 | 2.36 |
| 34 | Transport | 4.05 | 4.56 |
| 35 | Other Transport | 3.49 | 4.05 |
| 36 | Furniture | 1.57 | 1.90 |

Notes: All the estimated parameters are 2-digit industry specific. 1 Lag $\widehat{\varepsilon}_{b}$ are the estimated within local labor market elasticities when we instrument for the wages with one lag and 1 Lag $\widehat{\varepsilon}_{b}$ present the analogous when we instrument with two lags.

## E. 2 Sample Selection

Ficus. This data source comes from tax records therefore we observe yearly firm information. We exclude the source tables belonging to public firms. ${ }^{60}$ Before 2000 we take table sources in euros and from 2001 onward we use data from consolidated economic units. ${ }^{61}$ After excluding firms without firm identifier the raw data sample contains about 29 million firms from which about 2.8 million are manufacturing firms. ${ }^{62}$ Manufacturing sector (sector code equal to $D$ ) constitutes on average $10 \%$ of the observations, $19.2 \%$ of value added and $27.2 \%$ of employment.

[^32]Postes. DADS Postes covers all the employment spells of a salaried employee per year. If a worker has several spells in a year we would have multiple observations. The main benefit of this employer-employee data source is that we can know the establishment and employment location of the workers. We exclude workers in establishments with fictitious identifiers (SIREN starting by F) and in public firms. For every establishment identifier (SIRET) we sum the wage bill and the full time equivalent number of employees.

Merged Data. After merging both data sources we finish with data with yearly establishment observations. After the filters and merging the sample consists of 1.3 million firms and 1.6 million establishment observations. In the process of filtering and merging about half of the original firms are lost. Wages and value added are deflated using the Consumer Price Index. ${ }^{63}$

Labor and wage data coming from the balance sheets (at the firm level) and the one from employee records needs to be consolidated. In order to be consistent with balance sheet information we assign labor and employment coming from FICUS to the establishments according to their respective shares. We proceed in several steps. First, we filter out observations with no wage or employment information from Postes from firms present at different commuting zones. Second, we do some additional cleaning by getting rid of observations with no labor, capital and wage bill information coming from FICUS and also observations with non existing or missing commuting zone. Third, we aggregate employee data to the firm times commuting zone level. ${ }^{64}$ Then we compute the labor and wage shares of these entities out of the firm's aggregates. What we call establishment through out the text is the entity aggregated at the commuting zone level. Finally, we split firm data from the balance sheet according to those shares. This procedure leaves the firms in a unique commuting zone with their balance sheet data but allows to split wage bill and employment data coming from the balance sheet for multi-location firms. Establishment wage is simply the average wage. That is, wage bill over total full time equivalent employees.

We further exclude Tobacco (2-digits industry code 16), Refineries \& Nuclear industry (code 23) and Recycling (code 37). We finally get rid of the outliers reducing the sample $1.5 \%$ and finish with $4,156,754$ establishment-occupation-year observations that belong to 1.25 million firms. ${ }^{65}$

## E. 3 Variable Construction

## Ficus:

- Value added: value added net of taxes $(V A C B F)$. We restrict to firms with strictly positive value added. ${ }^{66}$
- Capital: tangible and intangible capital without counting depreciation. It is the sum of the variables IMMOCOR and IMMOINC.
- Employment: full time equivalent employment at the firm (EFFSALM).

[^33]- Wage bill: gross total wage bills. Is the sum of wages (SALTRAI) and firm taxed (CHARSOC). ${ }^{67}$
- Industry: industry classification comes from APE. The sub-industries $h$ are 3 digit industries and industries $b$ are at two digits.


## Postes:

- Occupation: original occupation categories come from the two digit occupations (CS2). We group occupations with first digits 2 and 3 into a unique occupation group. ${ }^{68}$ This regrouping is done to avoid substantial changes in occupation groups between 1994 and 2007. Observations with missing occupation information are excluded.
- Employment: full time equivalent at the establishment-occupation level (etp).
- Wage: is the gross wage (per year) of individual worker (sbrut). If the spell is less than a year is the gross wage corresponding to the spell.
- Commuting zone: depending on the year, the commuting zone classification is taken from the variable zemp or zempt. Commuting zone information is missing for the years 1994 and 1995 and is imputed using the city codes. ${ }^{69}$


## E. 4 Construction of Required Rates

In order to construct the required rates for the different sectors we follow the methodology proposed by Barkai (2016) using the Capital Input Data from the EU KLEMS database, December 2016 revision. In this dataset one can find, for a given industry, different depreciation rates and price indices for different types of capital. The types of capital that are present in the manufacturing sector are: Computing Equipment, Communications Equipment, Computer Software and Databases, Transport Equipment, Buildings and structures (non-residential), and Research and Development. We construct a required rate for each of the industries at the 2 digit level defined in the NAF classification. However, unlike the NAF classification, that we have up to 20 different industries, there are only 11 industries classified within manufacturing within the EU KLEMS database. Any industry classification in EU KLEMS is just an aggregation of the 2 digit industry classification in NAF. Therefore there are industries within the NAF classification that will have the same required rate of return on capital.

For a type of capital $s$ and sector $b$, we define the the required rate of return $R_{s b}$ as:

$$
R_{s b}=\left(i^{D}-\mathbb{E}\left[\pi_{s b}\right]+\delta_{s b}\right),
$$

where $i^{D}$ is a the cost fo debt borrowing in financial markets, and $\pi_{s b}$ and $\delta_{s b}$ are, respectively, the inflation and depreciation rates of capital type $s$ in sector $b$.

Then we define the total expenditures on capital type $s$ in sector $b$ as:

$$
E_{s b}=R_{s b} P_{s b}^{K} K_{s b}
$$

[^34]where $P_{s b}^{K} K_{s b}$ is the nominal value of capital stock of type $s$. Summing over all types of capital within a sector we can obtain the total expenditures of capital of such sector:
$$
E_{b}=\sum_{s b} R_{s b} P_{s b}^{K} K_{s b}
$$

Multiplying and dividing by the total nominal value of capital stock we obtain the following decomposition:

$$
\sum_{s} R_{s b} P_{s b}^{K} K_{s b}=\underbrace{\sum_{s} \frac{P_{s b}^{K} K_{s b}}{\sum_{s^{\prime}} P_{s^{\prime} b}^{K} K_{s^{\prime} b}} R_{s b}}_{R_{b}} \underbrace{\sum_{s} P_{s b}^{K} K_{s b}}_{P^{K b} K_{b}}
$$

where the first term $R_{b}$ is the interest rate that we use in the model.

## E. 5 Amenities

In order to preform some counterfactuals we still need to compute other policy invariant parameters, or fundamentals, from the data. In particular we need to recover establishment-occupation amenities and TFPRs, while ensuring that in equilibrium the wages and labor allocations are the same as in the data.

Using the establishments labor supply (13), we can back out amenities, up to a constant:

$$
T_{i o}=\frac{s_{i o \mid m}}{w_{i o}^{\varepsilon_{b}}} \Phi_{m}
$$

The sub-market level $\Phi_{m}$ is a function of the amenities of all plants in $m$. We proceed by normalizing one particular local labor market. Note that the allocation of resources is independent from this normalization. We denote the local labor market that we normalize as 1 . The relative employment share of market $m$ with respect to the normalized one is: $\frac{L_{m}}{L_{1}}=\frac{\Phi_{m}^{\eta / \varepsilon_{b}}}{\Phi_{m}^{\eta / \varepsilon_{b}}} \Gamma_{b}$. The local labor market aggregate is then:

$$
\Phi_{m}=\left(\frac{L_{m}}{L_{1}} \frac{\Gamma_{1}}{\Gamma_{b}} \Phi_{1}^{\frac{\eta}{\varepsilon_{b^{\prime}}}}\right)^{\frac{\varepsilon_{b}}{\eta}}
$$

Substituting into the above we have that:

$$
T_{i o} \propto \frac{s_{i o \mid m}}{w_{i o}^{\varepsilon_{b}}}\left(\frac{L_{m}}{\Gamma_{b}}\right)^{\varepsilon_{b} / \eta}
$$

## F Empirical Evidence

Example of an economy with four local labor markets and four firms identified by color. Each firm is multilocation with plants at different local labor markets. The blue firm is affected by a mass layoff at the national level (in all the local markets where it is present). Natural experiment on $s_{i o \mid m}$ for non-blue establishments.

Figure 6: Local Labor Markets with and without shock


The treated establishments are the ones in local markets 1 and 2.
Figure 7: Treated Establishments


The first order condition for wages is:

$$
P_{b} \frac{\partial F}{\partial L_{i o}}=L_{i o}\left(w_{i o}\right) \frac{\partial w_{i o}}{\partial L_{i o}}+w_{i o}
$$

where the right hand side is the marginal cost $\left(\frac{\partial w_{i o} L_{i o}}{\partial L_{i o}}\right)$ when internalizing movements along the labor supply curve. Noting that $\frac{\partial w_{i o}}{\partial L_{i o}}=\frac{w_{i o}}{L_{i o}} \frac{1}{e_{i o}}$ is the inverse of the labor supply elasticity $e_{i o}$, the first order condition can be written as:

$$
P_{b} \frac{\partial F}{\partial L_{i o}}=w_{i o}\left(1+\frac{1}{e_{i o}}\right)
$$

When labor supply is infinitely elastic, the MRPL is equal to the wage. When $e_{i o}<\infty$ the wage will be below the MRPL. Panel (a) of Figure 8 shows equilibrium wages and employment when the firm acts as a price taker (PT) and when it exerts labor market power (MP).

When firms have labor market power and do not act strategically, their perceived elasticity is constant, $e_{i o}=e$. The last term above is therefore constant implying that conditional on a labor supply level, wages are independent to employment shares. When the perceived elasticity is a decreasing function of the employment share, shocks that increase employment share will move the marginal cost (MC) curve to the left. Panel (b) of Figure 8 gives an intuition of our instrument.

Figure 8: Instrument


## F. 1 Definition of Mass Layoff

Denote by $M L$ the set of firms with a national mass layoff. That is, firms with all the establishments suffering a mass layoff. We instrument the employment share of the establishments of firms not suffering the national mass layoff $j \notin M L$ by the exogenous event of a firm present at the local labor market having a negative shock. We restrict the analysis to non-shocked firms present in different commuting zones with at least one establishment in a sub-market where a competitor has suffered a mass layoff and another plant whose competitors do not belong to firms in ML.

Local labor markets where a mass-layoff has occurred will take a value of $D_{m, t}$ equal to $1 .{ }^{70}$ The first stage is:

$$
s_{i o \mid m, t}=\psi_{\mathbf{J}(i), o, t}+\delta_{\mathbf{N}(i)}+\gamma D_{m, t}+\epsilon_{i o, t}
$$

where as before, $\psi_{\mathbf{J}(i),, t}$ is a firm-occupation-year fixed effect and $\delta_{\mathbf{N}(i)}$ is a commuting zone fixed effect. Using the fitted values we consider the following model for the second stage:

$$
\begin{equation*}
\log \left(w_{i o, t}\right)=\psi_{\mathbf{J}(i), 0, t}+\delta_{\mathbf{N}(i)}+\alpha \widehat{s_{i o \mid m, t}}+u_{i o, t} \tag{52}
\end{equation*}
$$

Before generating the instrument, we need to identify the firms suffering from a mass layoff. Defining a cut-off value $\kappa$, we identify a firm-occupation $j \in L O$ if establishment-occupation employment at $t$ is less than $\kappa \%$ employment last year. The best instrument would be identifying firms that went bankrupt ( $\kappa=0$ ). Given that we cannot externally identify if a firm disappears because it went bankrupt or change identifiers keeping the number of competitors at the local market constant. There is a trade-off when choosing $\kappa$. On the one hand, a lower threshold leads to considering stronger negative shocks and the generated instrument would be cleaner. On the other hand, we would classify less firms as having a negative shock reducing the

[^35]number of events considered. This creates a bias-variance trade-off on the election of the threshold. Lacking a clear candidate for $\kappa$, we try with different cut-off values. ${ }^{71}$

## F. 2 Robustness Checks

Figure 9 shows robustness checks of the reduced form exercise. The former considers a different instrument for the employment shares and the latter is taking commuting zone-year fixed effects. The results in the main text are with commuting zone fixed effects.

Figure 9: Robustness


Note: This figures present the point estimates and $95 \%$ confidence bands of the OLS and IV exercises on the y-axis. The x-axis presents different thresholds $\kappa$ that define a mass layoff shock. In both cases we focus on non-affected competitors (not suffering a mass layoff shock). The instrument in Panel (a) is the presence of a mass layoff shock firm in the local labor market interacted with the employment share of the affected firm. Panel (b) presents the results with commuting zone-year fixed effects.

Instead of considering local labor markets with industries at the 3-digit level $h$ as in the baseline, they are defined at the 2-digit level $b$.

[^36]Figure 10: Robustness. Local Labor Market at 2-digit Industry


Note: This figure presents the point estimates and $95 \%$ confidence bands of the OLS and IV exercises on the $y$-axis. The $x$-axis presents different thresholds $\kappa$ that define a mass layoff shock. We focus on non-affected competitors (not suffering a mass layoff shock). The instrument is the presence of a mass layoff shock firm in the local labor market. The definition of local labor market is a combination of commuting zone, 2-digit industry and occupation. The difference with respect to Figure 8 is that the local labor market is at 2-digit rather than 3-digit industry.

## G Distributional and Efficiency Consequences

Here we illustrate the distributional and efficiency effects when the labor wedge $\lambda$ is simply a markdown $\mu$. Figure 11 illustrates the effect of labor market power on the distribution of value added into profits and wage payments. For simplicity, we illustrate with the case of a production function using only labor with a decreasing returns to scale technology. On the left panel, we have the case of perfect competition in the labor market where wages are equal to the marginal revenue product of labor and the firm earns quasi-rents generated from having decreasing returns. On the right panel, we illustrate the case with labor market power. Wages are below the marginal revenue product because the markdown $\mu$. This generates additional profits for the firm, reducing wage bill payments and therefore the labor share.

Figure 11: Distributional Consequences


Figure 12 shows the efficiency consequences due to the misallocation of resources. The left panel shows two firms with the same markdown. For simplicity we assume that all firms and local labor markets have the same amenities so workers being indifferent, all establishments will have the same wage in equilibrium.

With homogeneous markdowns, the marginal revenue products are equalized across establishments. In particular, firm B is more productive and in equilibrium $L_{B}>L_{A}$. On the right panel we show an example with heterogeneous markdowns. Firm B being more productive is more likely to have a higher employment share at the local labor market and therefore a more important markdown. That is, $\mu_{B}<\mu_{A}$. Wages being equalized for all the establishments $M R P L_{B}<M R P L_{A}$. We illustrate the extreme case where the distortion generated by labor market power flips the employment size of both firms and we have $L_{A}>L_{B}$.

Figure 12: Efficiency Consequences


The next Figure shows the baseline and counterfactual distribution of demeaned wages.

Figure 13: Wage Distribution


## H Alternative Production Function

In this section we denote the local labor market as in the main text. $m$ denotes the combinations between commuting zone, 3-digit industry and occupations. That is: $m=n \times h \times o$. We denote as a location $l$ the combinations of commuting zones and 3-digit industries $l=n \times h$.

Suppose that establishment $i$ produces using some generic capital $K_{i}$ and a labor composite $H_{i}$ of different
occupations:

$$
\begin{equation*}
y_{i}=\widetilde{A}_{i} K_{i}^{\alpha_{b}} H_{i}^{\beta_{b}}=\widetilde{A}_{i} K_{i}^{\alpha_{b}}\left(\prod_{o \in \mathcal{O}} L_{i o}^{\gamma_{0}}\right)^{\beta_{b}}, \quad \sum_{o} \gamma_{o}=1, \quad \alpha_{b}+\beta_{b} \leq 1 . \tag{53}
\end{equation*}
$$

The first order conditions are:

$$
\begin{aligned}
w_{i o} & =\beta_{b} \gamma_{o} \lambda\left(\mu_{i o} \varphi_{b}\right) P_{b} \frac{y_{i}}{L_{i o}} \\
R_{b} & =\alpha_{b} \widetilde{A}_{i} K_{i}^{\alpha_{b}-1} H_{i}^{\beta_{b}}
\end{aligned}
$$

Substituting the first order condition for capital into the production function, the wage first order condition becomes,

$$
w_{i o}=\beta_{b} \gamma_{o} \lambda\left(\mu_{i o} \varphi_{b}\right) A_{i} H_{i}^{1-\delta} L_{i o}^{-1} P_{b}^{\frac{1}{1-\alpha_{b}}}
$$

where we plugged the labor supply and used the definition of $\delta=1-\frac{\beta_{b}}{1-\alpha_{b}}$ from the main text and $A_{i}=$ $\widetilde{A}_{i}^{\frac{1}{1-\alpha_{b}}}\left(\frac{\alpha_{b}}{R_{b}}\right)^{\frac{\alpha_{b}}{1-\alpha_{b}}}$ as in the main text. Using those and solving for $L_{i o}$ we can write the labor composite $H_{i}$ as function of wages:

$$
H_{i}^{\delta}=P_{b}^{\frac{1}{1-\alpha_{b}}} \prod_{o \in \mathcal{O}} \beta_{b} \gamma_{o} \lambda\left(\mu_{i o}, \varphi_{b}\right) w_{i o}^{-1}
$$

Substituting the wage first order condition with the labor supply (13) into this,

$$
\begin{aligned}
H_{i}^{1+\varepsilon_{b} \delta} & =P_{b}^{\frac{\varepsilon_{b}}{1-\alpha_{b}}} \prod_{o \in \mathcal{O}}\left(\beta_{b} \gamma_{o} \lambda\left(\mu_{i o}, \varphi_{b}\right) A_{i}\left(T_{i o} \Gamma_{b}^{\eta}\right)^{1 / \varepsilon_{b}}\right)^{\varepsilon_{b} \gamma_{o}} \prod_{o \in \mathcal{O}}\left(\Phi_{m}^{1-\eta / \varepsilon_{b}} \frac{\Phi}{L}\right)^{-\gamma_{o}} \\
& =P_{b}^{\frac{\varepsilon_{b}}{1-\alpha_{b}}}\left(\beta_{b} \gamma A_{i}\right)^{\varepsilon_{b}} T_{i} \Gamma \prod_{o \in \mathcal{O}} \lambda\left(\mu_{i o}, \varphi_{b}\right)^{\varepsilon_{b} \gamma_{0}} \prod_{o \in \mathcal{O}}\left(\Phi_{m}^{1-\eta / \varepsilon_{b}} \frac{\Phi}{L}\right)^{-\gamma_{0}},
\end{aligned}
$$

where $\Upsilon \equiv \Pi_{o \in \mathcal{O}} \gamma_{0}, \Gamma \equiv \prod_{o \in \mathcal{O}} \Gamma_{b}^{\eta}$ and $T_{i} \equiv \prod_{o \in \mathcal{O}} T_{i o}$. Plugging back into the wage equation and rearranging,

$$
\begin{align*}
w_{i o} & =\left[\lambda\left(\mu_{i o}, \varphi_{b}\right) \frac{\gamma_{o}}{T_{i o} \Gamma_{b}^{\eta}}\left(\beta_{b} A_{i}\right)^{\frac{1+\varepsilon_{b}}{1+\varepsilon_{b}}}\left(Y\left(T_{i} \Gamma\right)^{1 / \varepsilon_{b}}\right)^{\frac{\varepsilon_{b}(1-\delta)}{1+\varepsilon_{b} \delta}}\left(\prod_{o^{\prime} \in \mathcal{O}} \lambda\left(\mu_{i^{\prime}}, \varphi_{b}\right)^{\varepsilon_{b} \gamma_{o}^{\prime}}\right)^{\frac{1-\delta}{1+\varepsilon_{b} b^{\circ}}}\left(\prod_{o^{\prime} \in \mathcal{O}} \Phi_{m^{\prime}}^{\left(\eta / \varepsilon_{b}-1\right) \gamma_{o}^{\prime}}\right)^{\frac{1-\delta}{1+\varepsilon_{b} \delta}} \Phi_{m}^{1-\eta / \varepsilon_{b}}\right]^{\frac{1}{1+\varepsilon_{b}}}  \tag{54}\\
& \left(\frac{\Phi}{L}\right)^{\frac{1}{1+\varepsilon_{b}}} P_{b}^{1 / \chi}
\end{align*}
$$

with $\chi_{b}=\left(1-\alpha_{b}\right)\left(1+\varepsilon_{b} \delta\right)$. Define the following:

$$
\begin{aligned}
& c_{i o} \equiv \frac{\gamma_{o}}{T_{i o} \Gamma_{b}^{\eta}}\left(\beta_{b} A_{i}\right)^{\frac{1+\varepsilon_{b}}{1+\varepsilon_{b}}}\left(Y\left(T_{i} \Gamma\right)^{1 / \varepsilon_{b}}\right)^{\frac{\varepsilon_{b}(1-\delta)}{1+\varepsilon_{b} \delta}}, \\
& C_{l} \equiv \prod_{o^{\prime} \in \mathcal{O}}\left(\Phi_{m^{\prime}}^{\left(\eta / \varepsilon_{b}-1\right) \gamma_{o}}\right)^{\frac{\delta}{1+\varepsilon_{b} \delta}}\left(\frac{\Phi}{L}\right)^{\frac{1}{1+\varepsilon_{b}}}, \\
& F_{b} \equiv P_{b}^{1 / X},
\end{aligned}
$$

where $C_{l}$ is a location constant. Rearranging we have that:

$$
\begin{equation*}
w_{i o}=\left[\lambda\left(\mu_{i o}, \varphi_{b}\right) c_{i o}\left(\prod_{o^{\prime} \in \mathcal{O}} \lambda\left(\mu_{i 0^{\prime}}, \varphi_{b}\right)^{\varepsilon_{b} \gamma_{o}^{\prime}}\right)^{\frac{1-\delta}{1+\varepsilon_{b} b^{\circ}}} \frac{\Phi_{m}^{1-\eta / \varepsilon_{b}}}{\prod_{o^{\prime} \in \mathcal{O}} \Phi_{m^{\prime}}^{\left(1-\eta / \varepsilon_{b}\right) \gamma_{o}^{\prime}}}\right]^{\frac{1}{1+\varepsilon_{b}}} C_{l} F_{b} . \tag{55}
\end{equation*}
$$

The last system is equivalent to the one in (54) and has the benefit to being able to write the wages: $w_{i o}=$ $\widetilde{w}_{i o} C_{m} F_{b}$, where we want $\widetilde{w}_{i o}$ to be homogeneous of degree zero with respect constants to $m$ level. Note that the last term inside the brackets is homogeneous of degree zero with respect to location $l$ constants shared by all the occupations of a establishments. Then, defining $\widetilde{\Phi}_{m}=\sum_{i \in \mathcal{I}_{m}} T_{i o} w_{i o}^{\varepsilon_{b}}$, the establishment-occupation or normalized wage is:

$$
\begin{equation*}
\widetilde{w}_{i o} \equiv\left[\lambda\left(\mu_{i o}, \varphi_{b}\right) c_{i o}\left(\prod_{o^{\prime} \in \mathcal{O}} \lambda\left(\mu_{i o^{\prime}}, \varphi_{b}\right)^{\varepsilon_{b} \gamma_{o}^{\prime}}\right)^{\frac{1-\delta}{1+\varepsilon_{b}}} \frac{\widetilde{\Phi}_{m}^{1-\eta / \varepsilon_{b}}}{\prod_{o^{\prime} \in \mathcal{O}} \widetilde{\Phi}_{m^{\prime}}^{\left(1-\eta / \varepsilon_{b}\right) \gamma_{o}^{\prime}}}\right]^{\frac{1}{1+\varepsilon_{b}}} \tag{56}
\end{equation*}
$$

$\widetilde{w}_{i o}$ is homogeneous of degree zero with respect to location $l$ constants shared by all occupations. This property, allows to solve for the normalized wages of every location $l$ (combinations of commuting zone $n$ and sub-industry $h$ combinations) independently and then recover the aggregate constants. Aggregating (56) and solving for $\widetilde{\Phi}_{m}$,

$$
\widetilde{\Phi}_{m}=\left[\frac{\sum_{i \in I_{m}}\left(\lambda\left(\mu_{i o}, \varphi_{b}\right) c_{i o} T_{i o}^{\frac{1+\varepsilon_{b}}{\varepsilon_{b}}} \prod_{o^{\prime} \in \mathcal{O}} \lambda\left(\mu_{i 0^{\prime}}, \varphi_{b}\right)^{\varepsilon_{b} \gamma_{o}^{\prime}}\right)^{\frac{1-\delta}{1+\varepsilon_{b_{b}}}}}{\prod_{o^{\prime} \in \mathcal{O}} \widetilde{\Phi}_{m^{\prime}}^{\left(1-\eta / \varepsilon_{b}\right) \gamma_{o}^{\prime}}}\right]
$$

Taking first all to the power $\left(1-\eta / \varepsilon_{b}\right) \gamma_{o}$ and taking the product,

$$
\mathcal{L}_{l} \equiv \prod_{o^{\prime} \in \mathcal{O}} \widetilde{\Phi}_{m^{\prime}}^{\left(1-\eta / \varepsilon_{b}\right) \gamma_{o}^{\prime}}=\prod_{o^{\prime} \in \mathcal{O}}\left[\sum_{i \in I_{m}}\left(\lambda\left(\mu_{i o}, \varphi_{b}\right) c_{i o} T_{i o}^{\frac{1+\varepsilon_{b}}{\varepsilon_{b}}} \prod_{o^{\prime} \in \mathcal{O}} \lambda\left(\mu_{i o^{\prime}}, \varphi_{b}\right)^{\varepsilon_{b} \gamma_{o}^{\prime}}\right)^{\frac{1-\delta}{1+\varepsilon_{b} \delta}}\right]^{\gamma_{o^{\prime}} \frac{\varepsilon_{b}-\eta}{1+\varepsilon_{b}-\eta}},
$$

which recovers all the constants inside $\widetilde{w}_{m}$.
In order to prove the existence and uniqueness of the solution of the system (56), define $\widehat{w}_{i o}$ as:

$$
\begin{align*}
& \widehat{w}_{i o}=\left[\lambda\left(\mu_{i o}, \varphi_{b}\right)\left(\prod_{o^{\prime} \in \mathcal{O}} \lambda\left(\mu_{i o^{\prime}}, \varphi_{b}\right)^{\varepsilon_{b} \gamma_{o}^{\prime}}\right)^{\frac{1-\delta}{1+\varepsilon_{b}}}\right]^{\frac{1}{1+\varepsilon_{b}}} c_{i o}^{\frac{1}{1+\varepsilon_{b}}} \\
& w_{i o}=\widehat{w}_{i o}\left[\frac{\widetilde{\Phi}_{m}^{1-\eta / \varepsilon_{b}}}{\mathcal{L}_{l}}\right]^{\frac{1}{1+\varepsilon_{b}}} C_{l} F_{b}=\widehat{w}_{i o} z_{l}=\widetilde{w}_{i o} C_{l} F_{b} . \tag{57}
\end{align*}
$$

We can show that the system formed by (57) has a solution and is unique.
Proposition 3. For given parameters $0 \leq \alpha_{b}, \beta_{b}<1,1<\eta<\varepsilon_{b}, 0 \leq \delta \leq 1$, transformed price $F_{b}$, constants $C_{l}, \widetilde{\Phi}_{m}$, $\mathcal{L}_{l}$ and non-negative vectors of productivities $\left\{A_{i}\right\}_{i \in m}$ and amenities $\left\{T_{i o}\right\}_{i o \in m}$, there exists a unique vector of wages $\left\{w_{i o}\right\}_{i o \in I_{m}}$ for every location l (combination of commuting zone $n$ and sub-industry $h$ ) that solves the system formed by (57).

Sketch of the proof. For existence, first note that $\lambda\left(\mu_{i o}, \varphi_{b}\right) \in\left[\left(1-\varphi_{b}\right) \frac{\eta}{1+\eta}+\varphi_{b} \frac{1}{1-\delta},\left(1-\varphi_{b}\right) \frac{\varepsilon_{b}}{1+\varepsilon_{b}}+\varphi_{b} \frac{1}{1-\delta}\right], \forall i, o$. Define a vector $\mathbf{w}$ with wage of all the occupation-establishments at location $l, \mathbf{w} \equiv\left\{w_{11}, w_{12}, \ldots, w_{1 O}, \ldots, w_{I 1}, w_{I 2}, \ldots, w_{I O}\right\}$.
Taking for now the elements of $z_{l}$ as constants. The system to solve is: $f_{i o}(\mathbf{w})=\widehat{w}_{i 0} z_{l}$. We have that

$$
\begin{aligned}
\mathbf{w} \in \mathcal{C} & \equiv\left[\left(\left(1-\varphi_{b}\right) \frac{\eta}{1+\eta}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\eta \delta}} c_{11}^{\frac{1}{1+\varepsilon_{b}}} z_{l 1}\left(\left(1-\varphi_{b}\right) \frac{\varepsilon_{b}}{1+\varepsilon_{b}}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\eta \delta}} c_{11}^{\frac{1}{1+\varepsilon_{b}}} z_{l 1}\right] \\
& \times \ldots \times\left[\left(\left(1-\varphi_{b}\right) \frac{\eta}{1+\eta}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\eta \delta}} c_{I O}^{\frac{1}{1+\varepsilon_{b}}} z_{l O},\left(\left(1-\varphi_{b}\right) \frac{\varepsilon_{b}}{1+\varepsilon_{b}}+\varphi_{b} \frac{1}{1-\delta}\right)^{\frac{1}{1+\eta \delta}} c_{I O}^{\frac{1}{1+\varepsilon_{b}}} z_{l O}\right]
\end{aligned}
$$

The system $f_{i o}$ is continuous on wages and maps into itself on $\mathcal{C}$. The last set being a compact set we can apply Brower's fixed point theorem.

For uniqueness, once the product of the wedges is substituted, $\widehat{w}_{i 0}$ is:

$$
\widehat{w}_{i o}=\left[\lambda\left(\mu_{i o}, \varphi_{b}\right) c_{i o} \prod_{o^{\prime} \in \mathcal{O}}\left(w_{i o^{\prime}} c_{i o}^{-\frac{1}{1+\varepsilon_{b}}}\right)^{\gamma_{o}^{\prime} \varepsilon_{b}(1-\delta)}\right]^{\frac{1}{1+\varepsilon_{b}}}
$$

Define the function $g_{i o}(\mathbf{w})=f_{i o}(\mathbf{w})-w_{i o}$. Gross substitution is fulfilled if $\frac{\partial g_{i o}(\mathbf{w})}{\partial w_{j o}}>0, \forall j \neq i$ with $j \in \mathcal{I}_{l}$ and $\frac{\partial g_{i o}(\mathbf{w})}{\partial w_{i 0^{\prime}}}, \forall o^{\prime}$. Gross substitution resumes to taking the partial derivatives of $\widehat{w}_{i o}$ which are positive by similar reasoning as in the main proof. Finally, $\widehat{w}_{i o}$ is homogeneous of degree $\frac{\varepsilon_{b}}{1+\varepsilon_{b}}(1-\delta)<1$. Therefore the solution to the system (57) exists and is unique.

Finally, the model can be aggregated up to the industry level following similar steps as in the baseline. Steps to write the industry model are in Appendix A.5.

## I Pass Through

Table 18: Pass Through of $Z$

|  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Industry Code | Industry Name | $\epsilon_{Z}^{W}$ PT | $\widehat{\beta}_{b}^{Z}$ | Diff | $\mathrm{SE} \widehat{\beta}_{b}^{Z}$ |
| 15 | Food | 0.933 | 0.890 | 0.043 | 0.000 |
| 17 | Textile | 0.940 | 0.916 | 0.024 | 0.000 |
| 18 | Clothing | 0.943 | 0.925 | 0.018 | 0.000 |
| 19 | Leather | 0.918 | 0.842 | 0.076 | 0.000 |
| 20 | Wood | 0.939 | 0.888 | 0.052 | 0.000 |
| 21 | Paper | 0.885 | 0.835 | 0.050 | 0.000 |
| 22 | Printing | 0.939 | 0.914 | 0.025 | 0.000 |
| 24 | Chemical | 0.879 | 0.720 | 0.159 | 0.000 |
| 25 | Plastic | 0.904 | 0.856 | 0.048 | 0.000 |
| 26 | Other Minerals | 0.935 | 0.887 | 0.048 | 0.000 |
| 27 | Metallurgy | 0.862 | 0.777 | 0.085 | 0.001 |
| 28 | Metals | 0.951 | 0.932 | 0.019 | 0.000 |
| 29 | Machines and Equipments | 0.915 | 0.861 | 0.054 | 0.000 |
| 30 | Office Machinery | 0.876 | 0.760 | 0.116 | 0.001 |
| 31 | Electrical Equipment | 0.886 | 0.848 | 0.039 | 0.000 |
| 32 | Telecommunications | 0.869 | 0.840 | 0.029 | 0.000 |
| 33 | Optical Equipment | 0.925 | 0.894 | 0.031 | 0.000 |
| 34 | Transport | 0.853 | 0.802 | 0.051 | 0.000 |
| 35 | Other Transport | 0.871 | 0.788 | 0.083 | 0.000 |
| 36 | Furniture | 0.938 | 0.909 | 0.029 | 0.000 |

Notes: This table presents the estimation results of equation (30) in Column (4) $\widehat{\beta}_{b}^{Z}$ and its comparison to the pass through without the labor wedges in Column (3) $\epsilon_{Z}^{W}$ PT. Diff in Column (5) shows the difference between the pass thorough without the wedges and the estimated one and $S E \widehat{\beta}_{b}^{Z}$ in Column (6) presents the standard error of the estimated parameters $\widehat{\beta}_{b}^{Z}$.


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    ${ }^{\dagger}$ Azkarate-Askasua (JMP, corresponding author): miren.askasua@gmail.com; Zerecero: miguel.zerecero@tse-fr.eu.

[^1]:    ${ }^{1}$ See for example Berger et al. (2019), Jarosch et al. (2019), Benmelech et al. (2018) among others.
    ${ }^{2}$ French labor market is characterized by having low unionization rates but high coverage of collective agreements. This is due to the institutional setting of the labor market that empowers union representation depending on the firm size. Section 3.4 provides more detail on the French institutional setting.
    ${ }^{3}$ The Herfindahl-Hirschman Index is defined as the sum of the squares of employment shares.
    ${ }^{4}$ This corresponds to a reduction of roughly 1000 euros (at 2015 prices) per year if we pass from the first to the third quartile of the employment share distribution.

[^2]:    ${ }^{5}$ The intuition behind this is that after solving for wages for given industry and economy-wide constants, we can fully characterize the allocation of labor and capital within each industry. This fact, combined with the information about the establishment-level fundamentals, allows us to aggregate the model at the industry level with corresponding industry-level fundamentals.

[^3]:    ${ }^{6}$ To see the notion behind Identification through Heteroskedasticity, consider the following system: $y=\alpha x+u$ and $x=\beta y+v$, with $\operatorname{var}(\epsilon) \equiv \sigma_{\epsilon}$ and $\operatorname{cov}(u, v)=0$. The system is under-identified as the variance-covariance matrix of $(x, y)$ yields three moments ( $\sigma_{x}, \sigma_{y}$ and $\operatorname{cov}(x, y))$ while we have to solve for four unknowns: $\left(\alpha, \beta, \sigma_{u}, \sigma_{v}\right)$. Now suppose we can split the data into two sub-samples with the same parameters $(\alpha, \beta)$ but different variances. Now the two sub-samples give us $3+3=6$ data moments with only six unknowns: the two parameters $(\alpha, \beta)$ and the four variances of structural errors. This system is identified under the additional assumption that the variances $\sigma_{u}^{2}, \sigma_{v}^{2}$ are different across sub-samples.

[^4]:    ${ }^{7}$ Costinot and Rodríguez-Clare (2014) refer to this method as "exact hat algebra". They use this approach to compute welfare effects of trade liberalizations using easily accessible macroeconomic data.

[^5]:    ${ }^{8}$ Before 1994 the wage data was imputed and after 2007 the industry classification (APE) is not consistent with previous versions. On the contrary, the classification change between the 1993 and 2003 codes are consistent at the 3-digit level.
    ${ }^{9}$ The sources are https://www.insee.fr/fr/information/2114596 and https://www.insee.fr/fr/statistiques/serie/ 001643154 respectively.
    ${ }^{10}$ The classification is very similar to the one in Caliendo et al. (2015). We group together their first two categories (firm owners receiving a wage and top management positions) into top management because the distinction between the two was not stable in 2002 .
    ${ }^{11}$ The multilocation definition is occupation specific. A firm can have both monolocation and multilocation occupations.

[^6]:    Notes: $N_{h}$ is the number of establishments per 3-digit industry $h, L_{h}$ is total employment of $h, \bar{w}_{h}$ is the average establishment wage of $h, L S_{h}$ is the labor share and $K S_{h}$ is the capital share. We calibrate the interest rate following Barkai (2016). All the nominal variables are in thousands of constant 2015 euros.

[^7]:    ${ }^{12}$ The Herfindahl of local labor market $m$ ranges from the inverse of the number of competitors $\left(1 / N_{m}\right)$ if all the establishments have the same shares to 1 . A local labor market can have a HHI of almost one if one establishment has virtually all the employment.

[^8]:    ${ }^{13}$ The HHI index at market $m$ and year $t$ is: $\sum_{i \in \mathcal{I}_{m}} s_{i o \mid m}^{2}$ where shares at the market are accounted as shares of full time equivalent employees and $\mathcal{I}_{m}$ is the set of all firms in the sub-market $m$. The sub-industry concentration index $\overline{H H I}_{h t}$ is:

    $$
    \overline{H H I}_{h t}=\frac{1}{\left|\mathcal{M}_{h}\right|} \sum_{m \in \mathcal{M}_{h}} H H I_{m t} \frac{L_{m t}}{L_{h t}}
    $$

    where $\left|\mathcal{M}_{h}\right|$ is the number of local labor markets that belong to $h, L_{m}$ is the local labor market employment and $L_{h}$ is the 3-digit industry employment.

[^9]:    ${ }^{14}$ See Appendix F for a graphical illustration of the identification.
    ${ }^{15} \mathrm{~A}$ standard value in the literature is $\kappa=70 \%$. That is a $30 \%$ loss of employment.
    ${ }^{16}$ We are restricting to firms classified as not having a mass layoff. The regression sample therefore changes depending on $\kappa$ which is why the OLS estimates change slightly with $\kappa$.
    ${ }^{17}$ Details of the point estimates and confidence bands are in Appendix F.

[^10]:    ${ }^{18}$ This computation is done taking the employment share differences between the percentile 75 and 25 from Table 1 for the median wage. The analogous computation with the average wage gives a wage reduction of roughly 1300 euros.
    ${ }^{19}$ That is, a local labor market is defined as a combination between commuting zone, 2-digit industry and occupation.

[^11]:    ${ }^{20}$ Article in The Economist 'Why French unions are so strong' The Economist.
    ${ }^{21}$ Source OECD data https:/ /stats.oecd.org/Index.aspx?DataSetCode=TUD. Unionization rate is also denoted as union density.
    ${ }^{22}$ The source of collective bargaining agreements is the OECD as for unionization rates.
    ${ }^{23}$ Several collective agreements can coexist at a given establishment.
    ${ }^{24}$ Source DARES.
    ${ }^{25}$ The Appendix of Caliendo et al. (2015) provide a comprehensive summary of size related legal requirements in France.
    ${ }^{26}$ The prevalence of wage bargaining was $44 \%$ for establishments with 11 employees or more.

[^12]:    ${ }^{27}$ It is not important whether the entrepreneurs own capital or not. As it is a small open economy, the rental rate of capital is fixed and entrepreneurs rent capital from abroad until the marginal product is equal to the cost.

[^13]:    ${ }^{28}$ The solution and characterization of the model are in Section 4.4.
    ${ }^{29} F_{b}=P_{b}^{\frac{1}{\chi_{b}}}, \chi_{b}=\left(1-\alpha_{b}\right)\left(1+\varepsilon_{b} \delta\right)$ is the transformed industry price.

[^14]:    ${ }^{30}$ Similar to Atkeson and Burstein (2008), this type of behavior could be rationalized either by assuming a myopic behavior of the establishment or by having a continuous of local labor markets.
    ${ }^{31}$ Appendix A derives this expression.

[^15]:    ${ }^{32}$ Appendix $G$ provides an illustration of the distributional and efficiency consequences.
    ${ }^{33}$ The industry constant $\mu_{b}=\frac{\varepsilon_{b}}{\varepsilon_{b}+1}$ drives down the wages. If labor supply is endogenous, workers' decision between consumption $c$ and leisure $l$ would be distorted. Denote by $w$ the wage under monopsonistic competition and by $\tilde{w}$ the wage under competitive labor market. Worker's maximization under endogenous labor supply leads the marginal rate of substitution to be equal to the wage rate. $w<\tilde{w}$ and therefore $M R S_{c, l} \equiv \frac{u_{l}}{u_{c}}=w<\tilde{w}$. Meaning that workers would supply less labor than in the perfectly competitive case.
    ${ }^{34}$ The last part $\frac{1}{1-\delta}$ is a markup only under the assumption of decreasing returns to scale. That is, when $\delta>0$.

[^16]:    ${ }^{35} B$ is the number of different 2-digit industries.

[^17]:    ${ }^{36}$ Details are in Appendix E.4.
    ${ }^{37}$ This is derived in Appendix A.

[^18]:    ${ }^{38}$ We could in principle also do the reverse if the occupation specific value added were observed in the data.
    ${ }^{39}$ Table 14 in Appendix D. 3 provides details of industry estimates.

[^19]:    ${ }^{40}$ See Jolivet et al. (2006) for a comparison of French mobility against the U.S.
    ${ }^{41}$ The correlation between average per industry firm size and our estimated bargaining power is 0.31 .
    ${ }^{42}$ This is an employment weighted average of the industry estimates. The direct average of industry bargaining powers is 0.41 .

[^20]:    ${ }^{43}$ For example, Hsieh and Klenow (2009) conduct a counterfactual where they remove distortions at the firm level and compute the productivity gains at the industry level. The productivity gains are a result of factors of production reallocating to more productive firms within each industry. This allows them to compute a partial equilibrium effect on total factor productivity, i.e. keeping the production factors constant across industries. A general equilibrium effect on total factor productivity takes into account, not only the reallocation of inputs within, but also across industries. They can't do this as they can only identify relative productivity differences within each industry while normalizing average differences across industries. For more details, see equation (19) and the discussion below in their paper.
    ${ }^{44}$ Revenue Total Factor Productivities are defined as $P P_{b} A_{i o}$. With some abuse of notation, we name the transformed revenue total factor productivities $P F_{b}^{1+\varepsilon_{b} \delta} A_{i o}$ as TFPRs. Given that one cannot observe industry prices $P_{b}$, backing out productivities $A_{i o}$ from the data requires performing some normalizations to get rid of industry prices.
    ${ }^{45}$ Solving the counterfactuals in level as stated in Section 4 would require to back out the productivities. It would be possible to do so by making some additional normalizations per industry. For example, one could assume that the minimum physical productivity (or

[^21]:    Total Factor Productivity, TFP) is constant across industries and get rid of industry relative prices by normalizing the minimum TFP per industry.
    ${ }^{46}$ Appendix A provides the steps for the computation of the relative counterfactuals.

[^22]:    ${ }^{47}$ The derivation of the theoretical labor share is in Appendix A.5.

[^23]:    ${ }^{48}$ As the across local labor market elasticity $\eta$ being smaller than 1 , the expected value of the Fréchet distribution is not defined. We therefore can only compute the median and the mode of the worker welfare.
    ${ }^{49}$ The blank spaces correspond to code changes of certain municipalities after 2007.
    ${ }^{50}$ Another potential reason is the differential in the amenities. The reduction of manufacturing labor in the big cities could be magnified if they have in general worse amenities. We leave this analysis to future work.

[^24]:    ${ }^{51}$ Note that $\Delta Y=\widehat{Y}-1 \approx \ln \widehat{Y}$. The decomposition is with respect to $\ln \widehat{Y}$. The share of the gains that come from productivity (Sh. Prod) is simply $\frac{\sum_{b \in \mathcal{B}} \theta_{b} \ln \hat{Z}_{b}}{\ln Y}$. Each row from Columns 3 to 5 sums up to 1 .

[^25]:    ${ }^{52}$ We consider urban the 10 biggest commuting zones: Paris, Marseille, Lyon, Toulouse, Nantes, and the Paris surrounding, BoulogneBillancourt, Creteil, Montreuil, Saint-Denis and Argenteuil. Rural are the rest of the commuting zones.

[^26]:    ${ }^{53}$ Details on the theoretical model with endogenous participation are in Appendix B.

[^27]:    ${ }^{54}$ Following the steps described in Appendix B.2, we can solve for the counterfactuals solving first the normalized wages and then for industry prices.

[^28]:    ${ }^{55}$ The construction details of the rental rate of capital or the required rate are in Appendix E.4.

[^29]:    ${ }^{56}$ The degree of homogeneity of $h_{i o}(\mathbf{w})=w_{i o}$ is 1 .

[^30]:    ${ }^{57}$ Also note that even if we would have available some valid instruments, we would only be able to identify $\delta$ and $\eta$ but not $\varepsilon_{b}$.
    ${ }^{58}$ Of course we could have a more stringent identification assumption that would leave us with an overidentified system, for example, that all covariances are equal to zero. As an additional exercise we also estimated the parameters following a different identification strategy: we assume that the covariances of the structural errors were the same among all the occupational groups. This gives us a system with one overidentification restriction. The point estimates using this assumption and the one we mentioned above are pretty similar.

[^31]:    ${ }^{59}$ It can be the case that the solution does not exist. For example, given values of $\beta_{b}, \varepsilon_{b}$ and $\eta$, even with $\varphi_{b}=1$ the labor share generated by the model is too small to the one in the data. This does not happen with our data.

[^32]:    ${ }^{60}$ We only use the Financial units (FIN) and Other units (TAB) tables and exclude Public administration (APU).
    ${ }^{61}$ The profiling of big groups consolidates legal units into economic units. In 2001 the Peugeot-Citroën PSA was treated, Renault in 2003 and the group Accor in 2005. This implies the definition of new economic entities and would therefore lead to the creation of new firm identifiers. Given the potential impact of big establishments in local labor markets we opted to maintain them.
    ${ }^{62}$ We consider a missing firm identifier (SIREN) also if the identifier equals to zero for all the 9 digits.

[^33]:    ${ }^{63}$ Nominal variables are expressed in constant 2015 euros.
    ${ }^{64}$ Data from 1994 and 1995 do not have commuting zone information. We therefore impute it using correspondence tables between city code and commuting zone. A city code has 5 digits coming from the department and city. Some commuting zone codes beyond the 2 missing years were modified or cleaned. City codes (commune codes) of Paris, Marseille and Lyon were divided into different arrondissements. We assign them codes 75056,13055 and 69123 respectively. Then we proceed to the cleaning of commuting zones by assigning to the non existing codes the one corresponding to the city where the establishment is located. We get rid of non matched or missing commuting zone codes. We aggregate the data coming from Postes at the commuting zone level after this cleaning.
    ${ }^{65}$ We get rid of wage per capita outliers by truncating the sample at the $0.5 \%$ below and $99.5 \%$.
    ${ }^{66}$ We follow the advise of the French statistical instiute (INSEEE) in using net value added to perform comparisons across industries.

[^34]:    ${ }^{67}$ For firms declaring at the BIC-BRN regime (TYPIMPO $=1$ ) we only take SALTRAI .
    ${ }^{68}$ Occupations with first digit 1 and 7 are excluded. They constituted less than $0.05 \%$ of the matched sample.
    ${ }^{69}$ City codes are the concatenation of department (DEP) and city (COM).

[^35]:    ${ }^{70} \mathrm{~A}$ firm $j$ at occupation $o$ is hit by a negative shock if $\mathbb{1}\left\{L_{i o, t} / L_{i o, t-1}<\kappa \forall i\right.$ where $\left.\mathbf{J}(i), t=j\right\}=1$. A local labor market is identified as shocked $D_{m, t}=1$ if at least one establishment at the local market belongs to a firm in $M L$.

[^36]:    ${ }^{71} \mathrm{~A}$ standard value in the literature is $\kappa=70 \%$. That is a $30 \%$ lost of employment.

